# ASSESSING THE CONTENT VALIDITY OF TEACHERS' REPORTS OF CONTENT COVERAGE AND ITS RELATIONSHIP 

## TO STUDENT ACHIEVEMENT

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Many conceptual and analytical studies have been conducted to improve the validity of subject matter tests and the instructional sensitivity of psychometric and statistical methods used to analyze, interpret, and report test data in largescale achievement testing (Burstein, 1990a, 1990b; Burstein, Aschbacher, Chen, Li, \& Qi, 1986; Cole, 1988; Gold, 1990; Harnish, 1983; Linn, 1983; Muthen, 1989; Muthen, Kao, \& Burstein, 1988; Porter, 1989; Schmidt, 1983). Generally, there are multiple, systematic factors that contribute to student performance as measured by an instructional assessment at a given point in time. The factors such as student ability, topic exposure, and methods of instructional exposure that affect performance have to be considered in designing, analyzing and reporting tests (Burstein, 1990b; Burstein et al.,1986; Leinhardt, 1983; Leinhardt \& Seewald, 1981; Muthen et al., 1988; Yoon, Burstein, Gold, Chen, \& Kim, 1990).

As achievement tests have become influential in policy decisions, the degree of overlap between the content tested and the content taught has increased in importance (Airasian \& Madaus, 1983; Leinhardt \& Seewald, 1981). Students' exposure to different subject matter and the way in which subject matter has been covered will affect students' performance on tests. Therefore, how well achievement test items reflect student knowledge and the content of instruction are clearly of interest (Harnish \& Linn, 19811. Content coverage is considered especially important in state-by-state comparisons with increased concern about fairness of the comparisons due to differential learning opportunities across states or districts (Linn, 1983).

The purposes of the present study are (a) to investigate the validity of teachers' reports of students' instructional experiences (content exposure or coverage) and content validity of a given course by examining the consistency of reported content coverage for teachers across two consecutive years (1988 \& 1989), and (b) to examine the sensitivity of the test to instruction by linking student performance patterns to instructional experiences of students as possible corroborating evidence of their relationship. The results of earlier attempts validating teachers' reports of content coverage were reported earlier (Yoon, et al., 1990). This study refined the procedures from the earlier work by looking at each teacher's report of content coverage and relating it to his/her students' performance on each item.

## Data

The data used in this study came from the Mathematics Diagnostic Testing Program (MDTP). Under this project, the University of California and California State University systems have developed a series of four diagnostic tests (Algebra Readiness, Elementary Algebra, Intermediate Algebra, and Pre-calculus) to be used voluntarily in middle and secondary schools in California in an effort to improve secondary school mathematics. MDTP also offers teachers the opportunity to obtain student-level diagnostic performance data through the administration of one of a variety of examinations.

In this study, analyses are based on teacher and student data from approximately 300 sections ( 176 sections, 3 distlicts, 8 schools in 1988, and 112 sections, 3 districts, 10 schools in 1989) of mathematics spanning courses in Prealgebra, Math A, Math B (special to California schools as an alternative route to Algebra I), Algebra I, and Geometry. The analyses in this study are based on data from the Algebra Readiness and the Elementary Algebra examinations administered during the 1988 and 1989 school years. Each of these tests consists of 50 multiple-choice items administered during a SO-minute class period. There are approximately 2000 examinees and 20 teachers for both tests considered per year after matching by teacher and course for 1988 and 1989.

## Instrumentation

In addition to the achievement data in the study, classroom teachers responded to a questionnaire about their coverage of mathematics topics presented in each of the classrooms that were administered the diagnostic test. The response options for each mathematics topic on the questionnaire were examined, and patterns of teachers' responses on content coverage were evaluated and classified.
n our instrumentation, teachers were presented with different math topics and were asked to indicate how these topics are covered in each mathematics course they teach, using the following set of response options:

1. NEW - Taught as new content
2. EXTENDED - Reviewed and extended
3. REVIEW - Reviewed only
4. ASSUMED - Assumed as prerequisite knowledge and neither taught nor reviewed
5. TAUGHT LATER - Taught later in the school curriculum
6. NOT IN CURRICULUM- Not in the school curriculum
7. DON'T KNOW - Not taught now and don't know if in school curriculum

The seven response alternatives are adapted from Opportunity to Learn questions and topic-specific teacher questionnaires used in the Second International Mathematics Study. $1_{1}$ The questionnaire included topics which were identified as included in any of the four tests developed by MDTP or in the secondary school mathematics grid developed as part of an earlier study of the content validity of MDTP tests (Burstein et al., 1986). Thus the questionnaire was expected to span the course material for college-preparatory secondary school mathematics, necessitating an extensive list of topics ( 97 topics classified into 12 distinct subgroups): integers (4 topics); fractions, decimal, ratio, proportion, and percent (14); exponents, radicals, rational expression and square roots (14); polynomials (12); algebraic equations (11); inequalities (3); rational expressions (4); probability and statistics (2); geometry (15); absolute value (2); functions (10); and trigonometry (6).

If there was more than 80 percent consensus among teachers or each teacher across peliods in a specific topic category (for a specific course), the topic was assigned one of the following categories: CORE (New + Extended), PRIOR (Reviewed + Assumed), NOT TAUGHT (Taught later + Not in curriculum + Don't know). These auxiliary data were used to validate the substantive interpretation of the multidimensional structure of the test and the effect of

[^0]differential learning on student performance indicated by the current analyses of the achievement data.

## Methods and Techniques

The study relates patterns of teachers' content coverage responses with students' performance on the diagnostic math achievement tests. The first set of analyses with the teacher data investigated how consistently and how differently

1. the same teacher teaching the same course across years in 1988 and 1989 (results shown in Figure 1 and Tables A-1 and A-2 in Appendix A);
2. the same teacher teaching a different course in 1988 (Figure 2 and Table B-1 in Appendix B); or
3. the same teacher teaching a different course in 1989 (Figure 2 and Table B-2 in Appendix B).

The same teacher teaching a different course in different years (i.e., teaching Algebra I in 1988 and Geometry in 1989) also was analyzed, but since the results were similar to results for patterns 2 and 3 above, those results will not be presented here. Figure 1 shows the plot of topics with content coverage by courses for the same course and the same teacher for two consecutive years. The notations for the courses are: L (Lower than Pre-algebra), M (Math A), P (Prealgebra), A (Algebra I) and G (Geometry). Figure 2 shows the plot of topics with content coverage by courses for the same teacher teaching different courses across two years. The notation for the courses are: PG (a teacher taught both Prealgebra and Geometry in the same year), MA (Math A and Algebra I), LM (Lower than Pre-algebra and Math A), MG (Math A and Geometry), and AG (Algebra I and Geometry).

Evidence that reported content coverage patterns are similar across years may suggest that the chosen means of collecting such data has functioned as expected under the "steady state" curricular conditions prevalent in participating
schools. A representative sample of the results is shown in Tables A-1 to B-2 in Appendices A and B. The notations for these tables are as follows:

1. CC: Taught as CORE across years
2. PP: Taught as PRIOR across years
3. NN: NOT TAUGHT across years
4. CP: Taught as CORE in 1988 and as PRIOR in 1989
5. CN: Taught as CORE in 1988 and NOT TAUGHT in 1989
6. PC: Taught as PRIOR in 1988 and as CORE in 1989
7. PN: Taught as PRIOR in 1988 and NOT TAUGHT in 1989
8. NC: NOT TAUGHT in 1988 and taught as CORE in 1989
9. NP: NOT TAUGHT in 1988 and taught as PRIOR in 1989

The second set of analyses relates the teacher topic coverage response data to student performance at the item level. The differences in year 1 (1988) and year 2 (1989) p-values at the item level were calculated, and these differences were compared to differences in teachers' reported coverage of topics across the two years. These analyses show how consistently each teacher covered a course topic across years and, if not consistent, whether the lack of consistency systematically affects students' performance on MDTP test items measuring a given topic. Performance on test items in a given topic area should be consistent with teachers' report of coverage of these topics. The MDTP Algebra Readiness and Elementary Algebra tests, the two tests administered to students in the course types, were considered here. Students enrolled in Lower than Pre-algebra, Math A, Math B, or Pre-algebra took the MDTP Algebra Readiness test, and students enrolled in Algebra I or Geometry took the Elementary Algebra test. The results of pooled p-values across classes and teachers using the Algebra Readiness Test and Elementary Algebra Test are shown in Figure 3, and the results for individual teachers teaching the same course across years are shown Tables C-1 to C-5 in Appendix C.

## Results

## Topic Coverage Patterns

The results in Figures 1 and 2 provide evidence on the validity of teachers' responses on content coverage for a given course. The results of teacher content coverage by the same teacher teaching the same course across years (i.e., the same course taught by the same teacher in 1988 and 1989) are summarized in Figure 1, which shows the plot of topics with content coverage by courses. (More detailed results, including item content, are presented in Tables A-1 and A-2 in Appendix A.)

The results in Figure 1 show that 71 percent of topics were claimed to have been covered consistently in different levels of courses across two years. In the category CC (taught as CORE both in 1988 and 1989), 30 percent of topics were covered as CORE consistently across courses in both years, which implies that topics were mostly covered as new topics or reviewed and extended across courses. The number of topics taught as CORE in each course increased as the course level went up; about 20 topics were taught as CORE in Lower than Prealgebra while about 36 topics in Pre-algebra and about 40 topics in Algebra I were taught as CORE for two consecutive years. However, the number of topics taught as CORE in Geometry is relatively small (about 12 topics), which is reasonable because most topics taught as CORE in lower level courses were covered as PRIOR in Geometry. As shown in the category PP, about 33 topics were covered in Geometry as PRIOR while less than 10 topics were covered in Algebra I as PRIOR. Only a few topics were covered as PRIOR in Lower than Pre-algebra and Pre-algebra courses, as expected. In the category of NN about 66 topics were not taught in Lower than Pre-algebra, and the number of topics covered as NOT

TAUGHT went down considerably in Algebra I and Geometry. The deviations in consistency in the catego~ies of CP, CN, PC, PN, NC and NP may be due to changes in school or district curriculum policies or differences in class composition across years. These valiations may also depend on the specificity
and clarity of topic descriptions as well as on individual differences among teachers in their use of the response scale.

In Algebra I, with the exception of teacher T15 (detailed results are shown in Table A-2 in Appendix A), teachers covered topics for each course consistently across years. Topic coverage in Algebra I concentrates on the traditional core of introductory algebra (exponents, polynomials, algebraic equations, inequalities, rational expressions, absolute value). In Geometry, many more topics were covered as PRIOR compared to Algebra I, and the number of topics covered as CORE across years decreased considerably from Algebra I to Geometry as shown in Figure 1. Topics such as "Pythagorean Theorem," "perimeter and area of triangles," and "volume of cubes, cylinders," were covered as CORE; otherwise, topics covered as CORE in Algebra I were covered as PRIOR in Geometry. The idiosyncrasy of plots in the categories of CP, CN, PN and PC in Algebra I and Geometry occurs because teacher T15 taught an "advanced" class in 1988 and a "typical" class in 1989. This implies that studentst instructional experiences may be affected by class types.

Figure 2 shows the results of teachers' responses on content coverage across courses for two consecutive years. The results reported in Tables B-1 and B-2 in Appendix B show content coverages of 97 topics by the same teacher who taught different courses in 1988 or in 1989. These results show how the same topics were covered in low (i.e., lower than Pre-algebra) and high (i.e., Algebra I) levels of classes and how consistently a teacher covered topics in different courses across years. About 22 percent of topics were covered as CORE across courses such as Math A and Algebra I, Lower than Pre-algebra and Pre-algebra, and Algebra I and Geometry. About 31 percent of topics were NOT TAUGHT across courses, which was the same percentage as in Figure 1. These results support the results of consistent content coverage across years in Figure 1. As expected, the categories of CP and NC showed a reasonable transition in content coverage across courses.

In the category of CP , there was a big transition in content coverage from Algebra I to Geometry. About 60 topics were covered consistently as CORE in Algebra I and as PRIOR in Geometry by the same teacher across years. In this category all the lower level courses were compared with higher courses which showed a logical expectation of content coverage across courses. Similarly, the category of NC shows that 19 percent of topics across courses were covered as NC, and lower level courses compared with higher level courses.

The categories of CN, PC and PN clearly provide other evidence of validity of teachers' responses on content coverage by showing almost zero percent of topic coverage in these categories across lower level and higher level courses. There was almost no topic covered as PRIOR in Math A and as CORE in Algebra I, or as PRIOR in Pre-algebra and as CORE in Geometry. These results strongly support the validity of teachers' responses on content coverage in a given course. Topics taught differently across courses are "finding sum of interior angles," "isosceles and equilateral triangles," and "congruent triangles," taught as CORE in Prealgebra, as PRIOR in Algebra I, but NOT TAUGHT in Lower than Pre-algebra.

Overall, the results above showed that the prevalence and type of coverage of topics were consistent with their curricular sequence across years. Patterns were consistent with logical expectations for the topic within a given course across years and across teachers; therefore, cross-validation of teachers' responses on content coverage in a specific topic category (for a specific course) was successful.

## Relationships with Performance

The p-value differences between 1988 and 1989 at the item level for classes taught by the same teacher in successive years and the relationship of these differences to differences in teachers' reported coverage of topics are reported in Figure 3 and Tables C-1 to C-5 in Appendix C. These results show the evidence of content validity of test items by analyzing what was taught at secondary school mathematics and what was tested. Furthermore, content coverage of test item topics was related to students' performance on the Algebra Readiness Test and Elementary Algebra Test.

Content coverage reports of test item topics in Tables C-1 to C-5 validated the content validity of test items in Algebra Readiness Test and Elementary Algebra Test by showing a consistent content coverage on the test item topics; topics which were claimed to be taught were most likely tested in both tests, and this validates the content validity of test items.

P-value difference distributions of students' performance on the Algebra Readiness Test and Elementary Algebra Test are shown in Figure 3. When topics
were taught consistently across years as in the category of CC, p-values do not seem to vary across years. However, there were some deviations in p-values when topics were taught differently across years. For example, there was a pvalue mean difference of .04 when topics were covered as CORE and as PRIOR, and a .05 difference when topics were NOT TAUGHT in 1988 and covered as CORE in 1989.

However, these results are not convincing since these $p$-value differences are the average p-value differences across topics. When $p$-value differences were considered for each topic, some topics were relatively more sensitive to content coverage than others. For example, the topics "exponents with integral exponent," "order and comparison of fractions," and "perimeter and area of triangles and squares" showed relatively large p-value differences greater than .20. These topics were taught as CORE in 1988 and as PRIOR in 1989. In Math A, the topics "simplification of a rational expression" and "multiplication and division of fractions" showed relatively large p-value differences greater than . 13 . These topics were covered as CORE in 1988 and as PRIOR in 1989. These topics are sensitive to content coverage and to an effect of different content coverage on students' performance. In Pre-algebra, the topic "location of points in coordinate plane" showed a p-value difference of .15, and it was NOT TAUGHT in 1988 and taught as CORE in 1989. This topic was sensitive to content coverage, which clearly shows that exposure to a topic influences students' performance. The topics "basic operations with signed number" and "addition and subtraction of decimals" showed p-value differences but were not sensitive to content coverage, which implies that relatively easy topics do not seem to be influenced as much as fairly hard topics. In Algebra I, the topic "Pythagorean Theorem and special triangle" also seems to be sensitive to content coverage, showing a p-value difference of .12; it was NOT TAUGHT in 1988 and taught as CORE in 1989. The topics "algebra operation of literal symbol," "circumference and area of circle," "addition and subtraction of square roots" and "solving quadratic equation by factoring" also provided evidence of the effect of content coverage by showing very low p-values and small p-value differences less than .05 ; these topics were NOT TAUGHT across years. These results are shown in Tables C1 to C5.

## Implication

We considered the validity of teachers' responses on students' instructional experiences (content coverage) and viewed student test performance as supporting evidence. The patterns of responses were potentially realistic portrayals of coverage for different courses and topics at certain levels of specificity. This study provided an insight into the functioning of teachers' questionnaire responses about content coverage by examining and monitoring instructional practices.

Since the effect of content coverage is sensitive to the level of item difficulty, analyzing $p$-value differences as a function of the level of item difficulty, teachers' characteristics and content coverage might be interesting. Because teachers responded to the questionnaire without looking at the test items in this study, taking consideration of item difficulty in an analysis would also be worthwhile.

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Figure 1. Plot of Topics with Content Coverage by Courses (Teachers' responses of content coverage for the same course for two consecutive years)

L. Lower than Pre-algetra
A: Algebral
M: Math A
P: Pro-algebra
G: Geometry

Figure 2. Plot of Topics with Content Coverage by Courses (Teachers' responses of content coverage for the different courses for two consecutive years)


MA: Math A in 1988 and Algebra I in 1989
PG: Pre-algebra in 1988 and Geomotry in 1989
AG: Algebra I in 1988 and Geometry in 1989
L.P: Lower than Pro-algebra in 1988 and Pre-algetra in 1989

MG: Math A in 1988 and Geometry in 1989
LM: Lower than Pre-algebra in 1988 and Math A in 1989

Figure 3. P-value Difference Distributions of Students' Performance on Algebra ReadinessTest and Elementary Algebra Test


CONTENT

TABLE A-1 1988/1989 TEACHER CONTENT COVERAGE BY SAME TEACHER SAME COURSES ACROSS YEARS
(Algebra Readiness Test)


TABLE A-1 (continued)

| ITEMS COURSE: |  | LOWER THAN PRE-ALCEBRA |  |  | MATHA |  | PRE-ALGEBRA |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | T16 | T17 | T18 | T1 | T3 | T5 | T8 | T12 | T14 | T20 |
| 51 GENERATING EQUATIONS FROM DESCR. | * | NN | NN | NN | CC | CC | CC | CC | CN | NN | CP |
| 52 'SOLV. EQUA. FROM FACTORED FORM | , | N | NN | NN | NN | NN | NC | NN | N | NN | $N \mathrm{P}$ |
| 53 '50L.VING QUAD.EQUAT'BY FACTORING |  | NN | NN | NN | NN | NN | NC | NN | NN | NN | NP |
| 54 'SOLV. QUAD. EQUA. BY QUADRATIC |  | NN | NN | NN | NN | NN | NC | NN | NN | NN | NP |
| 55 GRAPHS OF QUADRATIC RELATIONS |  | NN | NN | NV | NC | NV | NC | NN | NN | NN | N |
| 56 ONE UNKNOWN WITH NUM. COEFFI. |  | NN | N | NN | CC | CN | CC | CC | CN | NV | CP |
| 57 'SOLUT, OF QUADRATIC INEQUALITIES |  | NN | NN | NN | NC | NV | CC | NN | CN | NN | N |
| 58 'GRAPFITNG LIN, INEQ, IN ONE UNKNO' |  | NN | NN | NN | CC | CN | CC | CC | CC | NN | N |
| 59 'SIMPLIF. OF A RATIONAL EXPRE. |  | NN | NN | NN | CC | CN | CC | CC | NC | NN | CP |
| 60 EVALUATION OF A RATIONAL EXPRE. |  | NN | NN | NN | CC | CC | CC | CC | NC | NN | CP |
| 61 'ADD. \& SUB. OF RATIONAL EXPRE. | * | N | NN | NN | CC | CN | CC | CC | NC | NN | CP |
| $62^{\circ} \mathrm{MUL}$ \& DIV. OF RATIONAL EXPRE. | , | NN | NN | NN | CC | NN | CC | CC | NC | NN | CP |
| 63 PROBABLUTY | , | CC | CN | NN | CC | CC | NN | NN | CC | NN | NN |
| 64 DESCRIPTIVE STATISTICS | , | CC | CN | NN | NC | CC | NN | NN | CC | NN | NN |
| 65 GRAPH READING | , | CC | CC | NN | CC | CN | CC | CC | CC | NC | CP |
| $66^{\prime}$ LOCATI. OF POINTS IN CORD. PLANE' | , | CC | cc | NN | CC | CN | CC | CC | CC | NC | CP |
| 67 DISTANCE BET. TWO POINTS IN COR. | , | CC | CC | NN | NC | NN | CC | CC | CC | NC | NC |
| 68 PERLMETER \& AREA OF TRLANGLES,SQ | , | CC | CC | CC | CC | CN | CC | CC | CC | OC | CC |
| 69 'CIRCUMFERENCE \& AREA OF CIRCLE | , | CN | CC | NC | CC | CN | CC | CC | CC | CC | CC |
| 70 'VOL OF CUBES, CYLINDERS,RECTAN. | , | NN | CC | NC | CC | NN | CC | NC | CC | NN | NC |
| 71 FINDING SUM OFINTERIOR ANGLES | , | CN | CC | NN | NC | NC | NN | NC | CC | CC | NC |
| $727505 C E L E S$ \& EQUILATERAL. TRIANGLE | , | CN | CC | NN | NC | NC | NC | NC | CN | OC | NC |
| 73 'APPLIC., CONGRUENT TRIANGLES | , | CN | CC | NN | NC | NN | NC | N N | CN | CC | NC |
| 74 'APPLLC, SIMPLE TRLANGLES | , | CN | CC | NN | NC | NN | NC | NN | CN | CC | NC |
| 75 'PYTHAGOREANTHEOREM \& SPECI. TR. | , | NN | NC | NN | NC | NC | CC | NN | CC | NC | NC |
| 76 PARALLELISM \& PERPENDICULARITY | , | NN | CC | NN | NN | NC | NN | NN | CN | CC | NC |
| 77 PROOFS(FORMAL DEDUCTIVE DEMONST, |  | NN | NN | NN | NN | NN | NN | NN | NN | NN | NC |
| 78 TRANSFORMATIONS(TRANSLATION. | , | NN | NN | NN | NN | NN | NN | NC | NN | NN | NN |
| 79 'VECTORS | , | NN | N | NN | NN | NN | NN | NN | NN | NN | NN |
| 80 'SIMPLIF. \& EVALU. OF EXPRESS. | , | NN | NC | NN | CC | NN | CC | CC | CN | NN | NP |
| 81 SOLUTION OF EQUATIONS |  | NN | NC | NN | NC | NN | CC | NN | CN | NN | NP |
| 82 FUNCT. CONCEPT \& USE OF NOTATIOX | , | NN | NN | NN | CC | CN | CN | NN | NN | NN | CN |
| 83 FUNCT. EVALUATION USTNG SUBSTIT. | , | NN | N | NN | OC | CN | CN | NN | NN | NN | CN |
| 84 COMPOSITION OP FUNCTION | , | NN | NN | NN | NN | NN | CN | NN | NN | NN | NN |
| 85 GRAPHING OF FUNCTION | , | NN | NN | NN | NN | N | CN | NN | NN | NN | NN |
| 85 NUMERICAL FUNCTICNAL EVALUATION | ' | NN | N | NN | NN | CN | NN | NN | NN | NN | NN |
| 87 SUBSTTIUTING LITERAL EXPRESS. | , | NN | NN | NN | NN | N | NN | NN | NN | NN | NN |
| 88 DEFINITION, LAWS \& RULES | ' | NN | N | NN | NN | NN | NN | NN | NN | NN | NeV |
| 89 TNVERSE RELATION BET, LOG, \& EXP | , | NN | N | NN | NN | N | NN | NN | NN | NN | NN |
| 90 SOLUTION OF LOG. AND EXP. FUNCT. | ' | NN | N | NN | NN | N | NN | NN | NN | NN | NN |
| 91 GRAPFHING OF LOG. AND EXP, FUNCT, | , | NN | N | NN | NN | N | NN | NN | NN | NN | N N |
| 92 FIND. ALGEBRAIC EXPRESS | , | NN | N | NN | NN | NN | NN | NN | NN | NN | NC |
| 93 DESCRIB. VARIATIONS OF FUNCTION | , | NN | N | NN | N | N | NN | NN | NN | NN | NC |
| 94 'FIND, SIDE LENGTHS IN SPEC.TRIA.' | - | NN | NN | NN | NC | NN | NN | NN | NN | NN | NC |
| 95 GRAPHLNG TRIGONOMETRIC FUNCTIONS |  | NN | N | NN | N | NN | NN | N | NN | NN | NN |
| $95^{\text {R REDUCING TRIGONOMETRIC EXPRE. }}$ | , | NN | NN | NN | NN | NN | NN | NN | NN | NN | NN |
| 97 PROOF OF TRIGONOMETRIC IDENITIIE | , | NeN | N | NN | NN | NN | NN | NN | NN | NN | NN |

TABLE A-2 1989/1989 TEACHER CONTENT COVERAGE BY SAME TEACHER SAME COURSES ACROSS YEARS
(Elementary Algebra Test)


TABLE A-2 (contimoed)

| COURSE: ALGERRAI |  |  |  |  |  |  |  | GEOMETRY |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ITEMS TEACHER: | T4 | T10 | T11 | T13 | T14 | T15 | T19 | T4 | T7 | 79 | T15 |
| 51 GENERATING EQUATIONS FROM DESCR.' | CC | NC | CC | CC | CC | CP | CC | PP | PP | CC | PC |
| 52 'SOLV. EQUA. FROM FACTORED FORM ' | CC | CC | NC | CC | NN | CP | CC | PP | PN | PC | PN |
| 53 'SOL.VING QUAD.EQUAT.BY FACTORING ' | CC | CC | NC | CC | NN | CP | CC | PP | PN | CC | PN |
| 54 SOLV. QUAD. EQUA. BY QUADRATIC ' | CC | CC | NC | CN | NN | CP | CC | PP | PN | NN | PN |
| 55 GRAPHS OF QUADRATIC RELATIONS | CC | CC | NN | NN | NN | CP | CC | PP | PN | NN | PN |
| 56 ONE UNKNOWN WTTH NUM. COEFFI. | CC | CC | CC | CC | CC | CP | CC | PP | PN | PP | PN |
| 57 'SOLUT, OF QUADRATIC INEQUALITIES | CC | CC | CC | CN | NN | CP | CC | PP | PN | NN | PN |
| 58 'GRAPFING LIN. INEQ IN ONE UNKNO | CC | CC | CN | CN | CN | CP | cc | PP | PN | PP | PN |
| 59 'SBMPLIF. Of A RATIONAL EXPRE. | CC | CC | CC | CC | CC | CP | CC | PP | PN | PP | PC |
| 60 EVALUATION OF A RATIONAL EXPRE | CC | CC | CC | CC | CC | CC | CC | PP | PN | PP | PC |
| 61 'ADD. \& SUB. OF RATIONAL EXPRE, | CC | CC | CC | CC | CC | CP | cc | PP | PN | PP | PC |
| 62 MUL \& DIV. OF RATIONAL EXPRE. | CC | CC | CC | CC | CC | CP | CC | PP | PN | PP | PC |
| 63 PROBABLLTY | NC | NN | CN | NN | NN | CC | NN | NN | NN | NN | CC |
| 64 DESCRIPTIVE STATISTICS | NC | NN | NN | NW | NN | CC | N | NN | NN | NV | ${ }_{\text {CC }}$ |
| 65 GRAPH READING | CC | PC | CN | NN | CN | CP | CN | PC | CN | Pp | OC |
| $66^{\circ}$ LOCATI. OF POINTS IN CORD. PLANE | CC | PC | CN | NN | CN | CP | CC | PC | CC | PC | -C |
| 67 DISTANCE BET. TWO POINTS IN COR. | CC | PC | CN | NN | CC | CC | CC | PC | CC | CC | CN |
| 68 PERIMETER \& AREA OF TRLANGLES,SQ | CC | PC | CP | NC | CP | CP | PC | CC | CC | CC | - ${ }^{\text {C }}$ |
| 69 'CIRCUMFERENCE \& AREA OF CIRCLE | NN | PP | CP | NC | PP | CP | NC | CC | CC | CC | CC |
| T0 'VOL OF CUBES, CYLINDERS,RECTAN, | N | PP | CP | NN | NN | CP | NN | CC | CC | CC | OC |
| 71 FINDING SUM OF INTERJOR ANGLLES | NC | PP | NN | NC | CP | NP | NN | CC | CC | CC | CN |
| 72 ISOSCELES \& EQUILATERAL TRLANGLE | NC | PP | NN | NC | PP | NP | NN | CC | CC | CC | CN |
| 73 'APPLIC. . CONGRUENT TRLANGLES | NC | PP | NN | NN | PP | NP | NN | CC | CC | CC | CN |
| 74 'APPLIC. . SIMPLE TRIANGLES | N | PP | N | NN | PP | NP | NN | CC | CC | CC | CN |
| 75 PYTHAGOREAN THEOREM \& SPECL TR. | NC | PP | CN | NC | NN | NP | NN | CC | CC | CC | CN |
| 76 PARALLELISM \& PERPENDICULARITY | NC | PP | CN | NN | PN | NP | NC | CC | CC | CC | CN |
| 77 PROOFS(FORMAL DEDUCTIVE DEMONST: | NC | PN | N | NN | NN | NP | NN | CC | CC | CC | CN |
| T8 TRANSFORMATIONS(TRANSLATION. " | N | PN | N | NN | NN | NP | NN | NN | CN | NC | CN |
| 79 VECTORS | NN | PN | NN | NN | NN | NP | NN | NN | CN | NN | CN |
| 50 SIMPLIF. \& EVALU. OF EXPRESS. | OC | NC | ${ }_{\text {CC }}$ | CC | NN | NP | NN | PP | NN | PP | CC |
| 81 SOLUTION OF EQUATIONS | CC | NC | CC | CC | CC | CP | CC | PP | NN | NN | CC |
| R2 FUNCT, CONCEFT \& USE OF NOTATION | CC | CC | CN | CN | NN | CC | NC | PP | NN | NP | PC |
| 83 FUNCT. EVALUATION USING SUBSTTT. | OC | CC | CN | NN | NN | CC | NC | PP | NN | NN | PC |
| 84 COMPOSTIION OF FUNCTION | NC | CC | CN | NN | NN | CC | NC | NP | NN | NN | PC |
| 85 GRAPHING OF FUNCTION | NC | OC | CN | NN | N | NP | NN | NP | NN | NC | PC |
| 86 NUMERICAL FUNCTIONAL EVALUATION ' | NN | CC | N | N | NN | NP | NN | NN | NN | NN | CN |
| 87 SUBSTITUTING LITERAL EXPRESS. | NN | CC | N | NN | N | NP | NN | NN | NN | NN | CN |
| 88 DEFINITION, LAWS \& RULES | NN | CC | N | NN | NN | NP | NN | NN | NN | NN | CN |
| 89 TNVERSE RELATION BET, LOG. \& EXP | NN | CC | N | NN | NN | NP | NN | NN | NN | NN | CN |
| 90 SOLUTION OF LOG. AND EXP. FUNCT. | NN | CC | N | N | N | NP | NN | NN | NN | NN | CN |
| 91 GRAPHING OF LOG. AND EXP. FUNCT. | NN | CC | N | NN | NN | NP | NN | NN | NN | NN | CN |
| 92 FIND. ALGEBRAIC EXPRESS | NN | CN | N | N | NN | NP | NN | NN | NN | NN | CN |
| 93 DESCRIB. VARIATIONS OF FUNCTION | NN | CN | N | NN | NN | NP | NN | NN | NN | NN | CN |
| 94 FIND, SIDE LENGTHS LN SPEC.TRLA. | NN | CN | NN | NN | NN | NP | NN | CN | NN | NC | CN |
| 95 GRAPHING TRIGONOMETRIC FUNCTIONS' | NN | CN | N | N | N | NP | NN | N | NN | NN | CN |
| 96 REDUCING TRIOONOMETRIC EXPRE. | NN | CN | NN | NN | NN | NP | NN | NN | NN | NN | CN |
| 97 PROOF OF TRICONOMEIRIC IDENITTIE | NN | CN | NN | N | N | NP | N | NN | NN | NN | CN |

TABLE B-1
TEACHER CONTENT COVERAGE BY SAME TEACHER DIFFERENT COURSES 1988

| COURSE: | MATHA /ALCEBRAI | $\begin{aligned} & \text { ALGERRA } \\ & \text { GEOM } \end{aligned}$ | LOWER <br> THAN <br> PRE-ALG <br> APRE-ALG | MATHA GEOM | $\begin{aligned} & \text { PRE-ALG } \\ & \text { GEOM } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ITEMS TEACHER: | T1 | T4 | TS | T7 | T8 |
| 1 BASIC OPERATIONS WTTH SICNED ND.' | CC | CP | CC | CP | CP |
| 2 TRIME FACTORIZATION | CC | CP | CC | CP | CP |
| 3 FINDING DISTANCES ONNUMBER LINE | CC | CC | CC | CP | CP |
| 4 USING DEFLNITION OP DIVISIBILTY' | CC | CC | CC | CP | CP |
| 5 'ADD \& SUB. OF FRACTIONS | CC | CP | CC | CP | CP |
| 6 MUL, \& DIV, OF FRACTIONS' | OC | CP | CC | CP | CP |
| 7 ORDER \& COMPARISON OF FRACTIONS | CC | CP | CC | CP | CP |
| 8 STMPLF, OF COMPLEX FRACTIONS | CC | CP | CC | CP | CP |
| 9 "ADD \& SUB OF DECIMALS' | CP | CP | CC | CP | CP |
| 10 MUL \& DIV. OF DECIMALS | CP | CP | OC | CP | CP |
| $11^{\prime}$ ESTIMATION \& APPROXIMATION' | CP | CP | CC | CP | CP |
| 12 'CONV, BET. FRACTIONS \& DECTMALS' | CP | CP | CC | CP | CP |
| $13^{\circ} \mathrm{CONV}, \mathrm{BET}$, FRACTIONS \& PERCENT | CP | CP | CC | CP | CP |
| 14 COMPUT. WITH DECI \& FRAC, ROUND | CP | CP | CC | $C P$ | CP |
| 15 COMPUTATICN OF PERCENT | CC | CP | CC | CP | CC |
| 16 'CONCEPT OF PROPORTION' | CC | CC | CC | CP | CC |
| 17 COMPUTATION OF PROPORTIONS' | CC | CC | CC | CP | CC |
| 18 'APPLIC. OF RATIO OR PROPORTIONS' | CC | CC | CC | CP | CC |
| 19 'APPLIC. LAWS OP EXPONENTS' | CC | CP | NC | CP | NC |
| 20 'POWERS OF 10 \& SCIENTIFIC NOTAT:' | CC | CP | NC | NP | NN |
| 21 'EXPONENT. WITHINTEGRAL EXTONEN.' | CC | CP | NC | NP | NN |
| 22 SQ ROOT OF PERFECT SQUARES' | CC | CC | CC | NP | CC |
| 23 SIMPLIFICATION OF SQ. ROOTS | CC | OC | CC | NP | CC |
| 24 'ADD, \& SUB, OF SQ, ROOTS' | CC | CC | NC | NP | CC |
| 25 MUL \& DIV. OF SQ. ROOTS' | CC | CC | NC | NP | CC |
| 26 'CONV, BET, RADICALS \& RAT, EXPO.' | NC | CP | NC | NC | NN |
| 27 RATIONALIZ OF NUMERA \& DENOML.* | NC | CP | NC | NC | NC |
| 28 'ADD. AND SUB. OF RADICAL EXPRE, | NC | CP | NC | NC | NC |
| 29 NUM. CALCU. W/ EXPONENTS \& RAD.' | NC | CP | NC | NC | NC |
| 30 'ALGE. CALCU, W/ EXPONENTS \& RAD.' | NC | CP | NC | NC | N |
| 31 'FACTORING \& SIMPLI. ALCE, EXPRE,' | NC | CP | NC | NC | N |
| 32 'ESTIM. \& APPROXI, WITH RADICALS.' | NC | CP | NC | NC | NC |
| 33 'ALGE OPERATION OF LITERAL SYMBOL' | CC | CP | NC | NP | CC |
| 34 'SIMPLIF. OF POLYNO. BY GROUPING.' | NC | CP | NC | NP | CC |
| 35 'ADD. \& SUB. OF POLYNOMIALS' | ${ }_{\text {CC }}$ | CP | NC | NP | ${ }_{\text {CC }}$ |
| 36 EVALUATION OF A POL YNOMLAL (1/2)' | CC | CP | NC | NP | CC |
| 37 MUL OF MONOMIAL WITH A POLYNO. | $\mathrm{CC}^{\text {c }}$ | CP | NC | NP | NC |
| 38 'MUL OF TWO BENOMLALS' | NC | CP | NC | NP | NC |
| 39 'DIVISION OF POLYNOMIALS' | CC | CP | NC | NP | NC |
| 40 'SQUARING A BENOMLAL' | NC | CP | NC | NP | NC |
| 41 'FACTOR. POLYNOMIALS' | NC | CP | NC | NP | NC |
| 42 'FACTOR. TRINOMIAL OVER INTEGERS' | NC | CP | NC | NP | NC |
| 43 'FACTOR. PERFECT SQ. TRINOMIALS' | NC | CP | NC | NP | NC |
| 44 'SIMPLF, OF COMPLEX NUMBERS' | NC | CP | NC | NP | NC |
| 45 ONE UNKNOWN WITH NUM. COEFFI, | CC | CP | CC | NP | CC |
| 46 ONE UNKNOWN WITH LIT. COEPF.' | CC | CP | CC | NP | OC |
| 47 'SIMPLE LN, EQUA. IN ONE UNKNOWN' | CC | CP | CC | NP | CC |
| 48 TWOUNKNOWN BY ELIMINATION' | NC | CP | NC | NP | CC |
| 49 TWO UNKNOWN BY SUBSTTTUTION | NC | CP | NC | NP | CC |
| 50 'APPLICATION OP EQUATIONS' | NC | CP | NC | NP | CC |

TABLE B-1 (continoed)

| COURSE: | MATHA /ALGEBRAI | ALOEBRA GEOM | LOWER <br> THAN PRE-ALO /PRE-ALG | MATHA GBOM | PRE-ALG /GEOM |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ITEMS TEACHER: | T1 | T4 | T5 | T7 | T8 |
| 51 GENERATING EQUATIONS PROM DESCR.' | CC | CP | NC | NP | CC |
| 52 'SOLV, EQUA. FROM FACTORED FORM' | NC | CP | NN | NP | NC |
| 53 SOLVING QUAD.EQUAT.BY FACTORING' | NC | CP | NN | NP | NC |
| 54 'SOLV, QUAD, EQUA BY QUADRATIC' | NC | CP | NN | NP | NC |
| 55 'GRAPHE OF QUADRATIC RELATIONS' | NC | CP | N | NP | NC |
| 56 ONE UNKNOWN WITH NUM. COEFF.' | CC | CP | NC | NP | CC |
| 57 'SOLUT. OF QUADRATIC INEQUALITES' | NC | CP | NC | NP | NC |
| 58 'GRAPFING LN, RNEQ. IN ONE UNKNO' | CC | CP | NC | NP | CC |
| 59 'SBMPLIF. OF A RATIONAL EXPRE' | NC | CP | NC | NP | $\bigcirc$ |
| 60 EVALUATIONOF A RATIONAL EXPRE - | CC | CP | NC | NP | $\mathrm{CC}^{\text {c }}$ |
| 61 'ADD. \& SUB. OF RATIONAL EXPRE.' | ${ }_{\circ}^{\text {CC }}$ | CP | NC | NP | CC |
| 62 MUL \& DIV, OF RATIONAL. EXPRE.' | $\mathrm{CC}^{\text {c }}$ | CP | NC | NP. | OC |
| 63 PROBABILITY | CC | NN | N | NN | N |
| 64 'DESCRIPITVE STATISTICS' | NC | NN | N | NN | N |
| 65 GRAPH READING' | $\bigcirc$ | CP | $\mathrm{CC}^{\text {C }}$ | NC | CC |
| 66 'LOCATL, OF POINTS IN CORD. PLANE' | OC | CP | OC | NC | $\mathrm{CC}^{\text {c }}$ |
| 67 DISTANCE BET. TWO POINTS IN COR.' | NC | CP | NC | NC | CC |
| 68 PERIMETER \& AREA OF TRIANGLES, SQ' | CC | CC | OC | NC | OC |
| 69 CIRCUMFERENCE \& AREA OF CIRCLE | CC | NC | CC | NC | CC |
| T0 VOL OF CUBES, CYLINDERS, RECTAN.' | CC | NC | $\mathrm{OC}^{\text {C }}$ | NC | NC |
| 71 'FINDING SUM OFINTERIOR ANGLES | N | NC | NN | NC | NC |
| T2 TSOSCELES \& EQUILATERAL TRIANGLE' | N | NC | N | NC | $\cdots \mathrm{NC}$ |
| 73 'APPLIC, CONGRUENT TRIANGLES' | NN | NC | NN | NC | NC |
| 34 'APPLIC. , SIMPLE TRLANGLES' | N | NC | NN | NC | $\cdots \mathrm{NC}$ |
| 75 PYTHAGOREAN THEOREM \& SPECI, TR.' | NC | NC | CC | nc | NC |
| 76 PARALLELISM \& PERPENDICULARITY' | NC | NC | NN | NC | NC |
| 77 PRCOFS(FORMAL DEDUCTIVE DEMONST.' | NN | NC | NN | NC | NC |
| T8 TRANSFORMATIONS(TRANSLATION:' | N | NN | N | NC | N |
| 79 'VECTORS' | NN | NN | NN | NC | NN |
| 50 SIMPLIF, \& EVALU, OF EXPRESS: | OC | CP | NC | NN | CC |
| 81 SOLUTIONOF EQUATIONS | $\mathrm{NC}^{\text {a }}$ | CP | NC | NN | NC |
| \$2 FUNCT, CONCEPT \& USE OF NOTATION | CC | CP | NC | NN | NN |
| 83 FUNCT. EVALUATION USING SUBSTIT:* | CC | CP | NC | NN | NN |
| 84 COMPOSITION OF FUNCTION | NN | NN | NC | N | NN |
| 85 GRAPHING OF FUNCTION | NC | NN | NC | N | NN |
| 85 NUMERXCAL FUNCTIONALEVALUATION' | NN | NN | NN | NN | NN |
| 87 SUBSTITUTING LITERAL EXPRESS.' | NN | NN | NN | N | N |
| 88 DEFINTTION, LAWS \& RULES | NN | NN | NN | N | NN |
| 89 TNVERSE RELATION BET. LOG. \& EXP | NN | NN | NN | N | NN |
| 90 SOLUTION OF LOG. AND EXP. FUNCT: | NN | N | NN | N | NN |
| 91 GR.APHING OF LOG. AND EXP. FUNCT.' | NN | NN | NN | NN | NN |
| 92 'FIND. ALGEBR AIC EXPRESS' | NN | N | NN | N | NC |
| 93 DESCRIB, VARIATIONS OF FUNCTION ${ }^{\text {' }}$ | NN | NN | NN | N | NC |
| 94 'FIND. SIDE LENGTHS IN SPECTRIA:' | NN | NC | NN | N | NC |
| 95 GRAPHINGTRIGONOMETRIC FUNCTIONS' | NN | NN | NN | NN | NN |
| 96 'REDUCING TRIGONOMEIRIC EXPRE.' | NN | N | NN | N | NN |
| 97. PROOF OFTRIGONOMEIRIC IDENTITIE' | NN | NN | NN | NN | NN |

TABLE B-2

| COURSE: | $\begin{aligned} & \text { LOWER } \\ & \text { THAN } \\ & \text { PRE-ALCI } \\ & \text { MATHA } \end{aligned}$ | ALGI GEOMETRY | LOWER <br> THAN <br> PRE-ALG <br> /PRE-ALG | LOWER <br> THAN <br> PRE-ALS <br> /PREALG <br> /ALGI |
| :---: | :---: | :---: | :---: | :---: |
| ITEMS TEACHER: | T3 | T4 | T12 | T14 |
| 1 BASIC OPERATIONS WITH SIGNED NO.' | OC | CP | NC | NCP |
| 2 PRIME FACTORIZATION' | CC | CP | CC | CCP |
| 3 FINDING DISTANCES ONNUMBER LINE' | CC | CP | PP | NCP |
| 4 USING DEFINTION OF DIVISIBLITY' | CC | CP | PP | CCP |
| 5 'ADD. \& SUB. OF FRACTIONS' | PP | CP | CP | CCP |
| 6 'MUL \& DIV. OF FRACTIONS | PP | CP | CP | ССР |
| 7 ORDER \& COMPARISON OF FRACTIONS' | PP | CP | CP | CCP |
| 8 'SBMPLE.OFCOMPLEX FRACTIONS' | PP | CP | CP | CCP |
| 9 'ADD \& SUB OP DECIMALS | PP | CP | CP | CCP |
| 10 'MUL \& DIV, OF DECIMALS' | PP | CP | CC | CCP |
| 11 ESTIMATION \& APPROXIMATION | PP | CP | CC | CCP |
| 12 'CONV, BET, FRACTIONS \& DECIMALS' | PP | CP | CC | CCP |
| 13 CONV. BET. FRACTIONS \& PERCENT | PP | CP | CC | CCP |
| 14 COMPUT. WTTH DECI \& FRAC, ROUND | PP | CP | CC | CCP |
| 15 COMPUTATION OF PERCENT | PP | CP | CC | CCP |
| 16 CONCEPT OF PROPORTION | PP | CP | CC | CCP |
| $17^{\prime}$ COMPUTATION OF PROPORTIONS | PP | CP | CC | CCP |
| 18 'APPLIC. OF RATIO OR PROPORTIONS | PP | CP | CC | CCP |
| 19'APPLLC. LAWS OF EXPONENTS' | CC | CP | CC | NOC |
| 20 POWERS OF 10 \& SCIENTIFIC NOTAT: | CC | CP | CC | NCC |
| 21 EXPONENT, WTTH INTEGRAL EXPONEN.' | CC | CP | NN | NOC |
| 22 SQ. ROOT OF PERFECT SQUARES' | NN | CC | NN | NCN |
| 23 SIMPLIFICATION OF SQ ROOTS' | N | CC | NN | NNN |
| 24 'ADD. \& SUB. OF SQ ROOTS' | N | CC | NN | NNN |
| 25 'MUL S DIV, OF SQ, ROOTS' | N | CC | N | NNN |
| 26 CONV. BET. RADICALS \& RAT. EXPO." | N | CP | NN | NNN |
| 27 'RATIONALIZ OF NUMERA. \& DENOMI.' | N | CP | NN | MNN |
| 28 'ADD. AND SUB. OP RADICAL EXPRE.' | N | CP | NN | NWN |
| 29 'NUM. CALCU, W/ EXPONENTS \& RAD.' | NN | CP | NN | NNN |
| 30 'ALGE CALCU. W/EXPONENTS \& RAD.' | N | CP | NN | NW |
| 31. 'FACTORING \& SIMPLI. ALGE EXPRE.' | NN | CP | NN | NNN |
| 32 'ESTMM. \& APPROXI WITH RADICALS.' | N | CP | NC | NWN |
| 33 'ALGE OPERATION OF LITERALSYMBCL'' | N | CP | NN | NOC |
| 34 'SIMPLIP, OF POLYNO. BY GROUPING,' | N | CP | NN | NCC |
| 35 'ADD, \& SUB. OF POLYNOMIALS' | N | CP | N | NNC |
| 36 EVALUATION OF A POLYNOMIAL(1/8)', | N | CP | NN | NCC |
| 37 MUL OF MONOMIAL. WITH A POLYNO.' | N | CP | NN | NNC |
| 38 'MUL OF TWO BINOMIALS' | NN | CP | NN | NNC |
| 39 'DIVISION OF POLYNOMIALS' | NN | CP | NN | NNC |
| 40 'SQUARING A BINOMIAL' | NN | CP | NN | NNC |
| 41 'FACTOR. POLYNOMIALS' | NN | CP | NN | NNC |
| $42^{\text {FACACTOR. TRINOMIAL OVER INTEGERS' }}$ | NN | CP | NN | NNC |
| 43 'FACTOR. PERFECT SQ. TRINOMLALS ' | N | CP | NN | NNC |
| 44 'SIMPLIF, OF COMPLEX NUMBERS' | NN | CP | NC | NNN |
| $45^{\circ}$ ONE UNKNOWN WITH NUM. COEFFL.' | CC | CP | CC | NNC |
| 46 ONE UNKNOWN WTIH LTT, COEFF.' | NN | CP | CC | NNC |
| 47 'SIMPLE LIN. EQUA IN ONE UNKNOWN' | CC | CP | CN | NNC |
| 48 TWO UNKNOWN BY ELIMINATION | NN | CP | N | NNN |
| 49 TWO UNKNOWN BY SUBSTITUTICN | NN | ${ }_{C P}$ | NN | NON |
| 50'APPLICATION OF EQUATIONS' | CC | CP | NC | NNC |

TABLE B-2 (continued)

| COURSE: | LOWER <br> THAN PRE-ALG/ MATHA | ALGI/ GEOMETRY | LOWER <br> THAN <br> PRE-ALG <br> /PRE-ALG | LOWER <br> THAN PRE-ALG fPREALG /ALGI |
| :---: | :---: | :---: | :---: | :---: |
| ITEMS TEACHER: | T3 | T4 | T12 | T14 |
| 51 'GENERATING BQUATIONS FROM DESCR.' | CC | CP | NN | NWN |
| 52 'SOLV. EQUA. FROM FACTORED PORM' | NN | CP | NN | NWN |
| 53 'SOLVINGQUAD.EQUAT.BY FACTORING' | NN | CP | NN | NWN |
| 54 'SOLV. QUAD. EQUA. BY QUADRATIC' | NN | CP | NN | $\mathrm{N} N \mathrm{~N}$ |
| 55 ORAPHS OFQUADRATIC RELATIONS | NN | CP | NN | NNC |
| 56 'ONE UNKNOWN WTTH NUM. COEFFL' | NN | CP | NN | NNN |
| 57 'SOL.UT. OF QUADRATIC INEQUALITIES | NN | CP | NC | NNN |
| 58 'GRAPPIING LIN, INEQ INONE UNKNO' | NN | CP | NC | NNC |
| 59 'SLMPLF. OF A RATIONAL EXPRE.' | CC | CP | NC | NNC |
| 60 'EVALUATION OF A RATIONAL EXPRE. ${ }^{\text {a }}$ | CC | CP | NC | NNC |
| 61 'ADD, \& SUB, OF RATIONAL EXPRE.' | NN | CP | NC | NNC |
| 62 MUL \& DIV. OF RATIONAL EXPRE. | NN | CP | NC | NNN |
| 63 PROBABILITY' | CC | CN | CC | NWN |
| 64 DESCRIPTIVE STATISTICS | CC | CN | CC | NNN |
| 65 GRAPH READING | N | CC | CC | NCN |
| 66 LOCATL. OF POINTS IN CORD. PLANE | NN | CC | CC | NCN |
| 67 DISTANCE BET. TWO PORNTS IN COR.' | N | CC | CC | NCC |
| 68 'PERIMETER \& AREA OF TRIANGLES,SQ | NN | CC | CC | CCP |
| 69 CIRCUMPERENCE \& AREA OP CIRCLE | N | NC | CC | CCP |
| 70 'VOL OF CUBES, CYLINDERSRECTAN:' | NN | NC | CC | $\mathrm{N} N \mathrm{~N}$ |
| 71 'FINDING SUM OP ENTERIOR ANGLES' | CC | CC | NC | NCP |
| 72 TSOSCELES \& EQUILATERAL TRIANGLE' | CC | CC | NN | NCP |
| 73 'APPLIC., CONGRUENT TRIANGLES' | NN | CC | NN | NCP |
| 74 'APPLLC., SIMPLE TRLANGLES | NN | NC | NN | NCP |
| 75 'PYTHACOREAN THEOREM \& SPECI TR,' | CC | CC | NC | NCN |
| 76 'PARALLELISM \& PERPENDICULARITY' | CC | CC | NN | NCN |
| 77 'PROOFS(FORMAL DEDUCTIVE DEMONST: | NN | CC | NN | NNN |
| 78 TRANSFORMATIONS(TRANSLATION.' | NN | NN | NN | NON |
| 79 'VECTORS' | NN | NN | NN | NNN |
| 80 SIMPLIF. \& EVALU. OF EXPRESS.' | N | CP | NN | NNC |
| 81 SOLUTION OF EQUATIONS | NN | CP | NN | NNC |
| 82 FUNCT. CONCEPT 2 USE OF NOTATION | NN | CP | NN | NNN |
| 83 'FUNCT, EVALUATION USING SUBSTIT:' | NN | CP | NN | NNN |
| 84 'COMPOSTTION OF FUNCTION' | NN | CP | NN | NNN |
| 85 'GRAPHING OF FUNCTION' | NN | CP | NN | NNN |
| 86 NUMERLCAL FUNCTIONALEVALUATION | NN | NN | NN | NNN |
| 87 'SUBSTITUTING LITERAL EXPRESS.' | NN | NN | NN | NNN |
| 88 'DEFINITION, LAWS \& RULES' | NN | N | NN | NNN |
| 89 'INVERSE RELATION BET, LOG, \& EXP' | NN | NN | NN | NNN |
| 90 'SOLUTTON OP LOG. AND EXP. FUNCT.' | N | NN | NN | NNN |
| 91 'GRAPHING OF LOG. AND EXP. FUNCT.' | N | NN | NN | NWN |
| 92 FIND. ALGEARAIC EXPRESS' | NN | NN | NN | NNN |
| 93 DESCRIB. VARIATIONS OF FUNCTION* | NN | NN | NN | NNN |
| 94 'FIND. SIDE LENGTHS IN SPEC.TRIA.' | N | NC | NN | NWN |
| 95 GRAPHING TRIGONOMETRIC FUNCTIONS' | N | NN | NN | NNN |
| 96 'REDUCING TRIGONOMETRIC EXPRE.' | NN | NN | NN | NWN |
| 97 'PROOF OF TRIGONOMETRIC IDENITIIE | NN | NN | NN | NN |

TABLE C- 1
algebra readiness test math a (TEACHER p) p.values

| HEMS | 1988 | 1989 | '88-'89 | CONTENT COVERACE |
| :---: | :---: | :---: | :---: | :---: |
| 1 'ADD. \& SUB OF DECIMALS' | . 346 | . 451 | -. 105 | CP |
| 2. 'MUL \& DIV. OF FRACTIONS' | . 404 | . 549 | -. 145 | CP |
| 3. 'ADD. \& SUB OP DECIMALS' | . 596 | . 569 | . 027 | CP |
| 4. EVALUATION OF A POLYNOMLAL(1/2)' | . 481 | . 549 | -. 068 | CC |
| 5. BASIC OPERATIONS WITH SIGNED NO.' | . 654 | . 735 | -. 081 | CP |
| 6. GRAPH READING' | . 173 | . 245 | -. 072 | CC |
| 7. BASIC OPERATIONS WITH SIGNED NO:' | . 404 | . 520 | -. 116 | CP |
| 8. 'BASIC OPERATIONS WITH SIGNED NO.' | . 654 | . 686 | -. 032 | CP |
| 9. FINDING DISTANCES ON NUMBER LINE' | . 462 | . 520 | -. 058 | CC |
| 10.COMPUTATION OF PERCENT | . 365 | . 431 | -. 066 | CP |
| 11 MUL \& DIV, OF FRACTIONS | . 385 | . 431 | -. 046 | CP |
| 12 PRIME FACTORIZATION' | . 250 | . 186 | . 064 | CC |
| 13 'ONE UNKNOWN WTTH NUM. COEFFF.' | . 481 | . 569 | -. 088 | CC |
| 14 'ONE UNKNOWN WTTH NUM. COEFFL' | . 538 | . 578 | -. 040 | CC |
| 15 EVAL.UATION OF A PCLYNOMIAL $(1 / 2)$ | 538 | . 588 | -. 050 | CC |
| 16 MUL \& DIV. OF FRACTIONS | . 250 | . 363 | - 113 | CP |
| 17 MUL \& DIV, OP DECIMALS' | 519 | . 490 | . 029 | CP |
| 18.'ADD. \& SUB. OF FRACTIONS' | . 250 | . 179 | . 074 | CP |
| 19 MUL \& DIV, OF FRACTIONS | - 327 | . 275 | . 052 | CP |
| 20 PRIME FACTORIZATION' | . 385 | . 353 | . 032 | CC |
| 21 BASIC OPERATIONS WITH SIGNED NO.' | . 173 | . 173 | . 026 | CP |
| 22 EASIC OPERATIONS WITH SIGNED NO.' | . 231 | . 255 | -.,024 | CP |
| 23 SQ. ROOT OF PERFECT SQUARES' | . 231 | . 294 | -. 063 | CC |
| 24 EVALUATION OF A POLYNOMIAL $(1 / 2 \gamma$ | . 269 | . 245 | . 024 | CC |
| 25 MUL \& DIV. OF DECBMALS | . 346 | . 431 | -.085 | CP |
| 26 CONV, BET. FRACTIONS \& PERCENT | . 308 | . 245 | . 063 | CP |
| 27 BASIC OPERATIONS WITH SIGNED NQ' | .192 | . 333 | - 141 | CP |
| 28 'SIMPLIF, OF A RATIONAL EXPRE' | . 423 | . 324 | . 099 | NC |
| $29^{\prime} \mathrm{MUL}$ \& DIV. OF FRACTIONS' | . 365 | . 235 | . 130 | CP |
| 30 'APPLIC. OF RATIO OR PROPORTIONS' | . 288 | . 314 | -. 026 | CC |
| 31 'SIMPLIF. OF COMPLEX FRACTIONS' | .192 | . 373 | - 181 | CP |
| 32'ESTIMATION \& APPROXIMATION' | . 404 | . 500 | -. 096 | CP |
| 33 'ALGE OPERATION OF LITERAL SYMBCL' | . 135 | . 127 | ,008 | CC |
| 34 EXPONENT, WTTH INTEGRAL. EXPONEN." | . 231 | . 118 | . 113 | CC |
| 35 FINDING DISTANCES ON NUMBER LINE' | . 231 | . 314 | -.,083 | CC |
| 36.'LOCATI, OF PORNTS IN CORD. PLANE' | . 212 | 373 | -. 161 | CC |
| 37.ORDER \& COMPARISON OF FRACTIONS | . 173 | . 147 | .026 | CP |
| 38.PERIMETER \& AREA OF TRIANGLES, SQ | . 288 | . 284 | . 004 | CC |
| 39.PYTHAGOREAN THEOREM \& SPECL. TR.' | .096 | . 216 | $-.120$ | NC |
| 40.POWERS OF 10 \& SCIENTIFIC NOTAT:' | . 231 | 324 | -. 093 | CC |
| 41.ORDER \& COMPARISON OF FRACIIONS | . 231 | . 284 | -.,053 | CP |
| 42:ADD. \& SUB, OF FRACTIONS' | . 058 | . 098 | -. 040 | CP |
| 43.'ADD. \& SUB. OF FRACTIONS' | .038 | .118 | -,080 | CP |
| 44.COMPUTATION OF PERCENT | . 115 | . 147 | -. 032 | CP |
| 45.COMPUT. WITH DECI \& FRAC, ROUND.' | . 269 | . 196 | . 073 | CP |
| 46.'CIRCUMFERENCE \& AREA OF CIRCLE | . 115 | . 147 | -. 032 | CC |
| 47.'BASIC OPERATIONS WITH SICNED NO.' | . 212 | . 255 | -,.043 | CP |
| 48.SQ, ROOT OF PERFECT SQUARES | . 096 | . 137 | -. 041 | CC |
| 49.PERIMETER \& AREA OF TRIANGLES, SQ' | .115 | . 167 | -,052 | CC |
| 50,'APPLIC, SIMPLE TRLANGLES' | .173 | . 147 | . 026 | NC |

TABLE C-2
ALGEBRA READINESS TEST PRE-ALGEBRA (TEACHER 14) P-VALUES

| TIEMS | 1988 | 1989 | '88-'89 | CONTENT COVERAGE |
| :---: | :---: | :---: | :---: | :---: |
| 1 'ADD. \& SUB OF DECIMALS' | . 455 | . 600 | -. 145 | CC |
| 2. 'MUL \& DIV. OF FRACTIONS' | . 782 | . 800 | -. 018 | OC |
| 3. 'ADD, \& SUB OF DECIMALS' | . 764 | . 711 | . 053 | CC |
| 4. EVALUATION OF A POLYNOMIAL(1/2)' | . 527 | . 600 | -. 073 | NC |
| 5. BASIC OPERATIONS WITH SIGNED NO.' | . 800 | . 844 | -. 044 | OC |
| 6. 'GRAPHI READING' | . 327 | . 244 | .083 | NC |
| 7. BASIC OPERATIONS WITH SIGNED NO.' | . 436 | . 644 | -. 208 | CC |
| 8. BASIC OPERATMONS WTIH SICNED NO.' | . 636 | . 667 | -. 031 | OC |
| 9. FINDING DISTANCES CNNUMBER LINE | . 600 | . 689 | -. 089 | NC |
| 10.COMPUTATION OF PERCENT | . 545 | . 467 | . 078 | CC |
| 11 MUL. \& DIV, OP FRACTIONS | . 709 | . 622 | . 087 | CC |
| 12 PRIME FACTORIZATION' | . 455 | . 489 | -. 034 | OC |
| 13 CNE UNKNOWN WITH NUM. COEFF.' | . 709 | . 644 | . 065 | NN |
| 14 'ONE UNKNOWN WTTH NUM. COEFFL' | . 600 | . 733 | -. 133 | N |
| 15 EVALUATION OF A PCLIYNOMIALL (1/2) | . 564 | . 667 | -. 103 | NC |
| 16 MUL \& DIV, OF FRACTIONS | . 345 | . 356 | -.,011 | CC |
| 17 MUL \& DIV, OF DECIMALS' | . 527 | . 600 | -. 073 | CC |
| 18.'ADD. \& SUB. OF FRACTIONS' | . 364 | . 400 | -. 036 | CC |
| 19 MUL \& DIV, OF FRACTIONS' | . 400 | . 333 | . 067 | OC |
| 20 PRLME FACTORIZATION | . 600 | . 644 | -. 044 | CC |
| 21 'BASIC OPERATIONS WITH SIGNED NO," | . 364 | . 289 | . 075 | CC |
| 22 BASIC OPERATIONS WITH SIGNED NO." | . 291 | . 244 | . 047 | CC |
| 23 'SQ, ROOT OF PERFECT SQUARES' | . 164 | . 267 | -. 103 | NC |
| 24 EVALUATION OF A POLYNOMIAL (1/2) | . 291 | . 200 | . 091 | NC |
| 25 MUL \& DIV, OF DECIMALS | . 236 | . 378 | -. 142 | CC |
| 26 'CONV.BET. FRACTIONS \& PERCENT' | . 764 | . 711 | . 053 | CC |
| 27 'BASIC OPERATIONS WITH SIGNED NO,' | . 309 | . 356 | -. 047 | CC |
| 28 \$DMPLIF. OF A RATIONAL EXPRE.' | . 364 | . 289 | . 075 | NN |
| 29 MUL \& DIV, OF FRACTIONS* | . 273 | . 244 | .029 | CC |
| 30 'APPLIC. OF RATIO OR PROPORTIONS" | . 309 | . 444 | -. 135 | CC |
| 31 SIMPLIF, OF COMPLEX FRACTIONS' | . 236 | . 333 | -. 097 | CC |
| 32. ESTIMATION \& APPROXIMATION | 364 | . 467 | -. 103 | CC |
| 33 'ALGE OPERATION OF LTERAL SYMBOL' | . 073 | . 044 | . 029 | CC |
| 34 'EXPONENT. WITH INTEGRAL EXPONEN.' | . 145 | . 244 | -. 099 | NC |
| 35 'FINDCNG DISTANCES ONNUMBER LINE' | . 273 | . 378 | -. 105 | NC |
| 36. 10 CATI. OF POINTS IN CORD, PLANE' | . 182 | . 333 | -. 151 | NC |
| 37.ORDER \& COMPARISON OF FRACTIONS' | . 164 | . 200 | -. 036 | CC |
| 38.PERIMETER \& AREA OF'TRIANGLES, SQ' | . 218 | . 200 | . 018 | CC |
| 39.PYTHAGOREAN THEOREM \& SPECI. TR.' | . 200 | . 133 | . 140 | CC |
| 40.POWERS OF 10 \& SCIENTIFIC NOTAT.' | . 273 | . 133 | -. 093 | CC |
| 41. ORDER \& COMPARISON OF FRACTIONS' | . 145 | . 044 | . 101 | CC |
| 42'ADD. \& SUB. OF FRACTIONS' | . 055 | . 133 | -. 078 | CC |
| 43.'ADD, \& SUB. OF FRACTIONS' | . 036 | .067 | -.,031 | CC |
| 44.COMPUTATION OF PERCENT | . 073 | . 044 | . 029 | CC |
| 45. COMPUT, WTIH DECI \& FRAC, ROUND;' | . 182 | . 178 | . 004 | CC |
| 46.CIRCUMFERENCE \& AREA OP CIRCLE' | . 073 | . 067 | .006 | CC |
| 47,BASIC OPERATIONS WITH SIGNED ND.' | .055 | . 111 | -.056 | CC |
| 48. 'SQ. ROOT OF PERFECT SQUARES' | . 073 | . 044 | . 029 | NC |
| 49.PERIMETER \& AREA OF TRLANGLES, SQ | . 055 | . 044 | . 011 | OC |
| S0'APPLIC. SIMPLE TRIANGLES' | . 073 | ,044 | . 029 | OC |

TABLE C-3
ALGEBRA READINESS TEST LOWER THAN PRE-ALGEBRA (TEACHER 17) P-VALUES

| ITEMS |  | 1988 | 1989 | '88-'89 | CONTENT COVERAGE |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 'ADD. \& SUB OF DECIMALS |  | . 400 | - 368 | 0032 | CP |
| 2. 'MUL \& DIV, OF FRactions |  | ,600 | . 588 | . 012 | CP |
| 3. 'ADD. \& SUB OF DECLMALS |  | . 360 | . 485 | -. 125 | CP |
| 4, 'EVALUATION OF A PCE YNOMIAL $[1 / 2$ ) |  | . 320 | . 375 | -.,055 | N |
| 5. 'BASIC OPERATIONS WITH SIGNED NO.' |  | . 600 | . 684 | -. 084 | CC |
| 6. 'GRAPH READING' |  | . 160 | . 184 | -. 024 | CC |
| 7. 'BASIC OPERATIONS WITH SIGNED NO.' |  | . 320 | . 588 | . 172 | CC |
| 8. 'BASIC OPERATIONS WITH SIGNED NO.' |  | . 760 | . 667 | -. 031 | CC |
| 9. 'RINDING DISTANCES ONNUMBER LINE' |  | . 400 | . 493 | -. 093 | CC |
| 10.COMPUTATION OF PERCENT |  | . 760 | . 449 | 311 | CP |
| 11 'MUL. \& DIV. OF FRACTIONS' |  | . 560 | . 390 | . 170 | CP |
| 12 PRIME FACTORIZATION |  | . 520 | . 316 | .204 | CC |
| 13 ONE UNKNOWN WITH NUM. COEFFI, |  | . 480 | . 529 | -.,049 | NN |
| 14 ONE UNKNOWN WITH NUM. COEFPI.' |  | . 640 | . 537 | . 103 | NN |
| 15 'EVALUATION OF A POLYNOMIAL(1/2) |  | . 400 | . 500 | -. 100 | NN |
| 16 'MUL. \& DIV. OF FRACTIONS' |  | . 200 | . 279 | -. 079 | CP |
| 17 MUL \& DIV. OF DECIMALS |  | . 320 | . 485 | -. 165 | CP |
| 18.'ADD. \& SUB. OF FRACTIONS' | * | . 240 | . 309 | -. 069 | CP |
| 19 'MUL \& DIV, OF FRACTIONS' |  | . 400 | . 360 | . 040 | CP |
| 20 PRIME FACTORIZATION |  | . 560 | . 485 | . 075 | CC |
| 21 BASIC OPERATIONS WITH SIGNED NO.' |  | . 320 | . 250 | . 070 | CC |
| 22 'BASIC OPERATION5 WITH SIGNED NO:' |  | . 200 | . 228 | . 028 | OC |
| 23 'SQ. ROOT OF PERFECT SQUARES |  | . 080 | . 279 | -. 199 | NC |
| 24 EVALUATION OF A POLYNOMLALC(1/2) |  | . 280 | . 272 | . 008 | NN |
| 25 'MUL \& DIV. OF DECIMALS |  | . 360 | . 404 | -. 044 | CP |
| $26^{\prime}$ CONV, BET. FRACTIONS \& PERCENT |  | . 480 | . 441 | . 039 | ${ }_{\text {CP }}$ |
| 27 'BASIC OPERATIONS WITH SIGNED NO.' |  | . 240 | . 287 | -. 047 | CC |
| 28 'SIMPLIF, OF A RATIONAL EXPRE:' |  | . 280 | . 382 | - 102 | N |
| $29^{\prime} \mathrm{MUL}$. \& DIV. OF FRACTIONS' |  | . 200 | . 346 | -. 146 | CP |
| 30 'APPLIC, OF RATIO OR PROPORTIONS' |  | . 360 | . 287 | . 073 | PP |
| 31 'SLMPLF. OF COMPLEX FRACTIONS' |  | . 240 | . 316 | -. 076 | CP |
| 32.ESTIMATION\& APPROXIMATION |  | . 280 | . 419 | -. 139 | CC |
| 33 'ALGE OPERATION OF LITERAL SYMBOL' |  | . 120 | . 074 | . 046 | NN |
| 34 'EXPONENT. WITH INTEGRAL EXPONEN'' |  | . 200 | . 478 | -. 278 | CP |
| 35 'FINDING DISTANCES ON NUMBER LINE' |  | . 320 | . 221 | . 099 | CC |
| 36.'LOCATL OF POONTS IN CORD. PLANE |  | . 320 | . 316 | . 004 | CC |
| 37.ORDER \& COMPARISON OF FRACTIONS' |  | . 320 | . 169 | . 151 | CP |
| 38.PERIMETER \& AREA OF TRIANCLLES, SQ |  | . 240 | . 338 | -. 098 | CC |
| 39.'PYTHAGOREAN THEOREM \& SPECL. TR.' |  | . 160 | . 206 | -. 046 | NC |
| 40,POWERS OF 10 \& SCIENTIFIC NOTAT: |  | . 280 | . 368 | -. 088 | CP |
| 41:'ORDER \& COMPARISON OF FRACTIONS' |  | . 080 | . 287 | -. 207 | CP |
| 42.'ADD. \& SUE. OF FRACTIONS' |  | . 040 | . 162 | -. 122 | CP |
| 43.'ADD. \& SUB. OF FRACTIONS' |  | . 000 | . 096 | .. 096 | CP |
| 44.COMPUTATION OF PERCENT |  | . 080 | . 118 | -. 038 | ${ }_{\text {CP }}$ |
| 45, COMPUT, WITH DECI \& FRAC, ROUND.' | * | . 120 | . 206 | -. 086 | CC |
| 46, CIRCUMFERENCE \& AREA OF CIRCLE' |  | . 080 | . 103 | -. 023 | CC |
| 47.'BASIC OPERATIONS WTTH SIGNED NO,' |  | . 080 | . 272 | -. 192 | OC |
| 48.SQ. ROOT OF PERFECT SQUARES' |  | . 080 | . 125 | -. 044 | NC |
| 49.'PERIMETER \& AREA OF TRIANGLES, SQ' |  | . 000 | . 169 | -. 169 | CC |
| 50.'APPLIC, SIMPLE TRLANGLES' |  | . 080 | . 213 | -. 133 | CC |

TABLE C-4
ELEMENTARY ALGEBRA TEST ALGEBRA I (TEACHER 4) P-VALUES

| ITEMS | 1988 | 1989 | '88-'89 | CONIENT COVERAGE |
| :---: | :---: | :---: | :---: | :---: |
| 1 'SDMPLIF. OF POLYNO. BY GROUPING' | . 963 | 1.000 | -.,037 | CC |
| 2. CONV, BET. FRACTICNS \& DECIMALS' | . 963 | . 950 | . 013 | CC |
| 3. 'ESTIM. \& APPROXI, WITH RADICALS.' | . 407 | . 500 | -, 193 | CC |
| 4, 'EXPONENT. WITH INTEGRAL EXPONEN.' | . 741 | . 700 | . 041 | CC |
| 5. 'ADD \& SUB OF DECTMALS' | . 827 | . 700 | . 127 | CP |
| 6. 'SQUARING A BINOMIAL' | . 914 | . 800 | . 114 | CC |
| 7. TSOSCELES \& EQUILATERAL TRIANGLE | . 420 | . 300 | . 120 | NC |
| 8. EXPONENT. WTIH INTEGRAL EXPONEN.' | . 531 | . 550 | . .019 | CC |
| 9. LOCATL OF POINTS IN CORD. PLANE | . 563 | . 900 | . 063 | CC |
| 10.'SMMPLF, OF A RATIONAL EXPRE. | . 642 | -550 | . 092 | CC |
| 11 'SOLV. EQUA. FROM FACTORED FORM' | . 679 | . 500 | . 179 | CC |
| 12 MUL OF MONOMIAL WTTH A POLYNO. | . 864 | . 700 | . 164 | CC |
| 13 'FACTOR. TRINOMLALOVER INTEGERS' | . 815 | . 750 | . 065 | CC |
| 14 ONE UNKNOWN WITH NUM. COEFFI.' | . 901 | . 700 | . 201 | CC |
| 15 'EVALUATION OF A POLYNOMIAL(1/29) | . 963 | 1.000 | -.,037 | CC |
| 16 'TWO UNKNOWN BY ELIMINATION' | . 654 | . 800 | -. 146 | CC |
| 17 'SQ ROOT OF PERFECT SQUARES | . 852 | . 600 | . 252 | CC |
| 18.PYTHAGOREAN THEOREM \& SPECI. TR." | . 580 | . 700 | -. 120 | NC |
| 19 'MUL, \& DIV, OF FRACTIONS' | . 679 | . 600 | .079 | CC |
| 20 'GRAPHING LIN. INEQ, IN ONE UNKNOWN' | . 963 | . 900 | . 063 | CC |
| 21 COMPPUTATION OPPERCENT | . 457 | . 600 | -. 143 | CC |
| 22 'ADD. \& SUB. OF SQROOTS' | . 864 | . 800 | . 054 | ${ }^{\circ} \mathrm{C}$ |
| 23 'FACTOR PERFECT SQ. TRINOMIALS' | . 901 | . 800 | . 101 | CC |
| 24 'MUL, \& DIV, OF SQ, ROOTS' | . 778 | . 700 | .078 | ${ }_{\text {cc }}$ |
| 25 'APPLICATION OP EQUATIONS | . 864 | . 950 | . .086 | CC |
| $26^{\prime}$ ONE UNKNOWN WITH NUM. COEFFI.' | . 728 | . 750 | -. 022 | ${ }^{\text {CC }}$ |
| 27 'EVALUATKON OF RATIONAL EXPRE.' | . 926 | 1.000 | .. 074 | CC |
| 28 'SIMPLF, OF SQUARE ROOTS' | . 901 | . 900 | . 001 | ${ }_{\mathrm{Cl}}^{\mathrm{CC}}$ |
| $29^{\prime} \mathrm{ADD}$, \& SUB. OF POL.YNOMIALS' | . 741 | . 700 | . 041 | CC |
| 30 'SIMPLIF, OF RATIONAL EXPRE,' | . 753 | . 750 | . 003 | CC |
| 31 PERIMETER \& AREA OFTRLANGLES, SQ' | . 728 | . 750 | . .022 | OC |
| 32.PERIMETER \& AREA OF TRIANCLES, SQ' | . 309 | . 400 | -. 091 | CC |
| 33 'SLMPLIF. OF A RATIONAL EXPRE.' | . 753 | . 700 | 053 | CC |
| 34 'ONE UNKNOWN WTTH NUM, COEFFI.' | . 704 | . 550 | -. 154 | CC |
| 35 MUL \& DIV.OF RATIONAL EXPRE." | . 728 | . 550 | . 078 | CC |
| 36.ONE UNKNOWN WITH NUM. COEPF." | . 654 | . 600 | . 054 | CC |
| 37.TWO UNKNOWN BY SUBSTITUTION | . 827 | . 800 | . 027 | CC |
| 38.POWERS OF 10 \& SCIENTIFIC NOTAT: | . 765 | . 600 | . 165 | CC |
| 39.'SOLVING QUAD. EQUAT. BY FACTORING' | . 617 | . 600 | . 017 | CC |
| 40.ADD \& SUB. OFRATIONAL EXPRE.' | . 667 | . 450 | 217 | CC |
| 41. 'VOL. OF CUBES, CYLINDERS, RECTAN.' | . 469 | . 450 | . 019 | NN |
| 42.'APPLIC, SIMPLE TRIANGLES' | . 531 | . 500 | . 031 | NN |
| 43.FINDNG DISTANCES ONNUMBER LINE | . 272 | . 450 | -. 178 | OC |
| 44.ONE UNKNOWN WITH LTT, COEFFL' | .741 | . 550 | .191 | OC |
| 45.COMPUTATICN OP PROPORTIONS | .481 | . 400 | . 081 | CC |
| 46. CIRCUMFERENCE \& AREA OF CIRCLE' | . 198 | . 150 | . 048 | N |
| 47.SOLVING QUAD. EQUAT. BY FACTORING | . 519 | . 350 | . 169 | CC |
| 48.ONE UNKNOWN WITH NUM. COEFFL. | . 741 | . 500 | .241 | CC |
| 49, ONE UNKNOWN WITHNUM. COEFF. | .481 | .450 | .031 | CC |
| 50.3OLV, QUAD, EQUA. BY QUADRATIC | -506 | . 350 | . 156 | CC |

TABLE C-5
ELEMENTARY ALGEBRA TEST ALGEBRA I (TEACHER 14) P-VALUES

| ITEM5 | 1988 | 1989 | '89-90 | CONTENT COVERAGE |
| :---: | :---: | :---: | :---: | :---: |
| 1 'SIMPLIF, OF POLYNO, BY GROUPING' | . 542 | . 615 | -. 073 | CC |
| 2. CONV. BET. FRACTIONS \& DECTMALS | . 854 | . 692 | . 162 | PP |
| 3. 'ESTIM. \& APPROXL WTTH RADICALS.' | . 042 | . 038 | . 004 | NN |
| 4. EXPONENT. WITH INTEGRAL EXPONEN.' | . 312 | . 538 | $-.226$ | CC |
| 5. 'ADD, \& SUB OF DECIMALS' | . 312 | . 500 | -. 188 | PP |
| 6. 'SQUARING A BINOMIAL' | . 396 | . 654 | -. 258 | CC |
| 7. TSOSCELES \& EQUILATERAL TRIANGLE' | . 187 | . 231 | -. 044 | PP |
| 8. EXPONENT. WITH INTEGRAL EXPONEN.' | . 104 | . 000 | . 104 | CC |
| 9. LOCATI. OP POINTS IN CORD. PLANE | . 604 | .615 | -. 011 | CN |
| 10. SIMPLIF, OF A RATIONAL, EXPRE.' | . 437 | . 615 | -. 178 | CC |
| 11 SOLV. EQUA. FROM FACTORED FORM' | . 229 | . 577 | -. 348 | NN |
| 12 MUL OF MONOMIAL WITH A POLYNO. | . 625 | . 577 | . 048 | CC |
| 13 'FACTOR. TRINOMIALOVER INTECERS' | . 437 | . 385 | ,052 | CC |
| 14 CNE UNKNOWN WTTH NUM. COEFFL' | . 437 | . 462 | -. 025 | CC |
| 15 EVALUATION OF A PCOYNOMLAL $(1 / 2 y$ | . 687 | . 615 | . 072 | PP |
| 16 TWO UNKNOWN BY ELIMINATION | . 083 | . 115 | -. 032 | CN |
| 17 SQ. ROOT OF PERFECT SQUARES' | . 271 | . 231 | . 040 | NN |
| 18.PYTHAGOREAN THEOREM \& SPECI. TR.' | . 562 | . 577 | -. 015 | NN |
| 19 MUL \& DIV. OF FRACTIONS' | . 229 | . 385 | -, 156 | PP |
| 20 GRAPHENG LIN.INEQ INONE UNKNOWN | 417 | . 462 | -.,045 | CN |
| 21 COMPUTATION OF PERCENT | . 146 | . 154 | -. 008 | CP |
| 22 'ADD, \& SUB, OF SQ.ROOTS | . 062 | . 077 | -. 015 | NN |
| 23 'FACTOR, PERFECT SQ, TRINOMIALS' | . 417 | . 846 | -. 429 | CC |
| 24 'MUL. \& DIV. OF SQ. ROOTS' | .167 | . 385 | -,218 | NN |
| 25 'APPLXCATION OF EQUATIONS' | . 417 | . 269 | . 148 | CC |
| 26 ONE UNKNOWN WITH NUM. COEFFL.' | . 146 | . 115 | . 031 | CC |
| 27 EVALUATION OF RATIONAL EXPRE.' | . 396 | . 538 | -. 142 | CC |
| 28 'SIMPLIP.OF SQUARE ROOTS' | . 0652 | . 154 | -.092 | NN |
| 29 'ADD, \& SUB, OF POLYNOMIALS' | . 167 | . 269 | - 102 | CC |
| 30 'SIMPLIF. OF RATIONAL EXPRE.' | . 354 | . 538 | -, 184 | CC |
| 31 PERIMETER \& AREA OF TRIANGLES, SQ | . 125 | . 346 | -. 221 | CP |
| 32.PERIMETER \& AREA OF TRIANGLES, SQ | . 229 | . 462 | -. 233 | CP |
| 33 'SIMPLIF, OF A RATIONAL EXPRE' | . 250 | . 346 | -. 096 | CC |
| 34 ONE UNKNOWN WITH NUM. COEFFL' | . 104 | . 077 | . 027 | CC |
| 35 'MUL \& DCV, Of RATIONAL EXPRE.' | . 271 | . 462 | -. 191 | CC |
| 36.ONE UNKNOWN WITH NUM. COEFFL.' | . 162 | . 077 | -.015 | CC |
| 37.TWO UNKNOWN BY SUBSTTIUTMON | . 104 | . 115 | -. 011 | CN |
| 38.'POWERS OF 10 \& SCIENTIFIC NOTAT:' | . 125 | . 346 | -. 221 | CC |
| 39.'SOLVING QUAD. EQUAT. BY FACTORING' | . 104 | . 192 | -. 088 | NN |
| 40:'ADD \& SUB. OF RATIONAL EXPRE' | . 042 | . 269 | -. 227 | CC |
| 41.VOL. OF CUBES, CYLINDERS, RECTAN.' | . 146 | . 308 | -. 162 | NN |
| 42.'APPLIC, SIMPLE TRLANGLES | . 229 | . 462 | -. 233 | PP |
| 43.'FINDING DISTANCES ONNUMBER LINE' | . 042 | . 077 | -. 035 | CP |
| 44.'ONE UNKNOWN WITH LTT, COEFFL.' | . 062 | . 115 | -. 053 | CC |
| 45,COMPUTATION OF PROPORTIONS' | . 021 | . 038 | -. 017 | CP |
| 46.CIRCUMFERENCE\& AREA OF CIRCLE | . 021 | . 038 | -. 017 | PP |
| 47,SOL.VING QUAD. EQUAT. BY FACTORING | . 104 | . 346 | -. 242 | NN |
| 48.ONE UNKNOWN WTTH NUM. COEFFL. | . 021 | . 308 | --287 | ${ }^{\text {CC }}$ |
| 49,ONE UNKNOWN WTTH NUM. COEFFL. | . 062 | . 385 | -. 323 | CC |
| 50.SOLV. QUAD. EQUA. BY QUADRATIC | . 021 | . 154 | --133 | NN |


[^0]:    1 These data are from a national sample of United States eighth-grade students' mathematics achievement tests conducted by IEA (International Association for the Evaluation of Educational Achievement) in 1981-1982.
    course topics have been covered across years and within the same year by each teacher. Teachers' content coverage for a specific course was analyzed by extending previous research (Yoon et al., 1990) to look at content coverage by:

