ASSESSING THE CONTENT VALIDITY OF TEACHERS' REPORTS OF CONTENT COVERAGE AND ITS RELATIONSHIP TO STUDENT ACHIEVEMENT

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Many conceptual and analytical studies have been conducted to improve the validity of subject matter tests and the instructional sensitivity of psychometric and statistical methods used to analyze, interpret, and report test data in largescale achievement testing (Burstein, 1990a, 1990b; Burstein, Aschbacher, Chen, Li, & Qi, 1986; Cole, 1988; Gold, 1990; Harnish, 1983; Linn, 1983; Muthen, 1989; Muthen, Kao, & Burstein, 1988; Porter, 1989; Schmidt, 1983). Generally, there are multiple, systematic factors that contribute to student performance as measured by an instructional assessment at a given point in time. The factors such as student ability, topic exposure, and methods of instructional exposure that affect performance have to be considered in designing, analyzing and reporting tests (Burstein, 1990b; Burstein et al.,1986; Leinhardt, 1983; Leinhardt & Seewald, 1981; Muthen et al., 1988; Yoon, Burstein, Gold, Chen, & Kim, 1990).

As achievement tests have become influential in policy decisions, the degree of overlap between the content tested and the content taught has increased in importance (Airasian & Madaus, 1983; Leinhardt & Seewald, 1981). Students' exposure to different subject matter and the way in which subject matter has been covered will affect students' performance on tests. Therefore, how well achievement test items reflect student knowledge and the content of instruction are clearly of interest (Harnish & Linn, 19811. Content coverage is considered especially important in state-by-state comparisons with increased concern about fairness of the comparisons due to differential learning opportunities across states or districts (Linn, 1983).

The purposes of the present study are (a) to investigate the validity of teachers' reports of students' instructional experiences (content exposure or coverage) and content validity of a given course by examining the consistency of reported content coverage for teachers across two consecutive years (1988 & 1989), and (b) to examine the sensitivity of the test to instruction by linking student performance patterns to instructional experiences of students as possible corroborating evidence of their relationship. The results of earlier attempts validating teachers' reports of content coverage were reported earlier (Yoon, et al., 1990). This study refined the procedures from the earlier work by looking at each teacher's report of content coverage and relating it to his/her students' performance on each item.

Data

The data used in this study came from the Mathematics Diagnostic Testing Program (MDTP). Under this project, the University of California and California State University systems have developed a series of four diagnostic tests (Algebra Readiness, Elementary Algebra, Intermediate Algebra, and Pre-calculus) to be used voluntarily in middle and secondary schools in California in an effort to improve secondary school mathematics. MDTP also offers teachers the opportunity to obtain student-level diagnostic performance data through the administration of one of a variety of examinations.

In this study, analyses are based on teacher and student data from approximately 300 sections (176 sections, 3 distlicts, 8 schools in 1988, and 112 sections, 3 districts, 10 schools in 1989) of mathematics spanning courses in Prealgebra, Math A, Math B (special to California schools as an alternative route to Algebra I), Algebra I, and Geometry. The analyses in this study are based on data from the Algebra Readiness and the Elementary Algebra examinations administered during the 1988 and 1989 school years. Each of these tests consists of 50 multiple-choice items administered during a SO-minute class period. There are approximately 2000 examinees and 20 teachers for both tests considered per year after matching by teacher and course for 1988 and 1989.

Instrumentation

In addition to the achievement data in the study, classroom teachers responded to a questionnaire about their coverage of mathematics topics presented in each of the classrooms that were administered the diagnostic test. The response options for each mathematics topic on the questionnaire were examined, and patterns of teachers' responses on content coverage were evaluated and classified.

n our instrumentation, teachers were presented with different math topics and were asked to indicate how these topics are covered in each mathematics course they teach, using the following set of response options:

- 1. NEW Taught as new content
- 2. EXTENDED Reviewed and extended
- 3. REVIEW Reviewed only
- 4. ASSUMED Assumed as prerequisite knowledge and neither taught nor reviewed
- 5. TAUGHT LATER Taught later in the school curriculum
- 6. NOT IN CURRICULUM- Not in the school curriculum
- 7. DON'T KNOW Not taught now and don't know if in school curriculum

The seven response alternatives are adapted from Opportunity to Learn questions and topic-specific teacher questionnaires used in the Second International Mathematics Study.1₁ The questionnaire included topics which were identified as included in any of the four tests developed by MDTP or in the secondary school mathematics grid developed as part of an earlier study of the content validity of MDTP tests (Burstein et al., 1986). Thus the questionnaire was expected to span the course material for college-preparatory secondary school mathematics, necessitating an extensive list of topics (97 topics classified into 12 distinct subgroups): integers (4 topics); fractions, decimal, ratio, proportion, and percent (14); exponents, radicals, rational expression and square roots (14); polynomials (12); algebraic equations (11); inequalities (3); rational expressions (4); probability and statistics (2); geometry (15); absolute value (2); functions (10); and trigonometry (6).

If there was more than 80 percent consensus among teachers or each teacher across peliods in a specific topic category (for a specific course), the topic was assigned one of the following categories: CORE (New + Extended), PRIOR (Reviewed + Assumed), NOT TAUGHT (Taught later + Not in curriculum + Don't know). These auxiliary data were used to validate the substantive interpretation of the multidimensional structure of the test and the effect of

 $_{
m 1}$ These data are from a national sample of United States eighth-grade students' mathematics achievement tests conducted by IEA (International Association for the Evaluation of Educational Achievement) in 1981-1982.

course topics have been covered across years and within the same year by each teacher. Teachers' content coverage for a specific course was analyzed by extending previous research (Yoon et al., 1990) to look at content coverage by:

differential learning on student performance indicated by the current analyses of the achievement data.

Methods and Techniques

The study relates patterns of teachers' content coverage responses with students' performance on the diagnostic math achievement tests. The first set of analyses with the teacher data investigated how consistently and how differently

- 1. the same teacher teaching the same course across years in 1988 and 1989 (results shown in Figure 1 and Tables A-1 and A-2 in Appendix A);
- 2. the same teacher teaching a different course in 1988 (Figure 2 and Table B-1 in Appendix B); or
- 3. the same teacher teaching a different course in 1989 (Figure 2 and Table B-2 in Appendix B).

The same teacher teaching a different course in different years (i.e., teaching Algebra I in 1988 and Geometry in 1989) also was analyzed, but since the results were similar to results for patterns 2 and 3 above, those results will not be presented here. Figure 1 shows the plot of topics with content coverage by courses for the same course and the same teacher for two consecutive years. The notations for the courses are: L (Lower than Pre-algebra), M (Math A), P (Prealgebra), A (Algebra I) and G (Geometry). Figure 2 shows the plot of topics with content coverage by courses for the same teacher teaching different courses across two years. The notation for the courses are: PG (a teacher taught both Prealgebra and Geometry in the same year), MA (Math A and Algebra I), LM (Lower than Pre-algebra and Math A), MG (Math A and Geometry), and AG (Algebra I and Geometry).

Evidence that reported content coverage patterns are similar across years may suggest that the chosen means of collecting such data has functioned as expected under the "steady state" curricular conditions prevalent in participating

schools. A representative sample of the results is shown in Tables A-1 to B-2 in Appendices A and B. The notations for these tables are as follows:

- 1. CC: Taught as CORE across years
- 2. PP: Taught as PRIOR across years
- 3. NN: NOT TAUGHT across years
- 4. CP: Taught as CORE in 1988 and as PRIOR in 1989
- 5. CN: Taught as CORE in 1988 and NOT TAUGHT in 1989
- 6. PC: Taught as PRIOR in 1988 and as CORE in 1989
- 7. PN: Taught as PRIOR in 1988 and NOT TAUGHT in 1989
- 8. NC: NOT TAUGHT in 1988 and taught as CORE in 1989
- 9. NP: NOT TAUGHT in 1988 and taught as PRIOR in 1989

The second set of analyses relates the teacher topic coverage response data to student performance at the item level. The differences in year 1 (1988) and year 2 (1989) p-values at the item level were calculated, and these differences were compared to differences in teachers' reported coverage of topics across the two years. These analyses show how consistently each teacher covered a course topic across years and, if not consistent, whether the lack of consistency systematically affects students' performance on MDTP test items measuring a given topic. Performance on test items in a given topic area should be consistent with teachers' report of coverage of these topics. The MDTP Algebra Readiness and Elementary Algebra tests, the two tests administered to students in the course types, were considered here. Students enrolled in Lower than Pre-algebra, Math A, Math B, or Pre-algebra took the MDTP Algebra Readiness test, and students enrolled in Algebra I or Geometry took the Elementary Algebra test. The results of pooled p-values across classes and teachers using the Algebra Readiness Test and Elementary Algebra Test are shown in Figure 3, and the results for individual teachers teaching the same course across years are shown Tables C-1 to C-5 in Appendix C.

Results

Topic Coverage Patterns

The results in Figures 1 and 2 provide evidence on the validity of teachers' responses on content coverage for a given course. The results of teacher content coverage by the same teacher teaching the same course across years (i.e., the same course taught by the same teacher in 1988 and 1989) are summarized in Figure 1, which shows the plot of topics with content coverage by courses. (More detailed results, including item content, are presented in Tables A-1 and A-2 in Appendix A.)

The results in Figure 1 show that 71 percent of topics were claimed to have been covered consistently in different levels of courses across two years. In the category CC (taught as CORE both in 1988 and 1989), 30 percent of topics were covered as CORE consistently across courses in both years, which implies that topics were mostly covered as new topics or reviewed and extended across courses. The number of topics taught as CORE in each course increased as the course level went up; about 20 topics were taught as CORE in Lower than Prealgebra while about 36 topics in Pre-algebra and about 40 topics in Algebra I were taught as CORE for two consecutive years. However, the number of topics taught as CORE in Geometry is relatively small (about 12 topics), which is reasonable because most topics taught as CORE in lower level courses were covered as PRIOR in Geometry. As shown in the category PP, about 33 topics were covered in Geometry as PRIOR while less than 10 topics were covered in Algebra I as PRIOR. Only a few topics were covered as PRIOR in Lower than Pre-algebra and Pre-algebra courses, as expected. In the category of NN about 66 topics were not taught in Lower than Pre-algebra, and the number of topics covered as NOT

TAUGHT went down considerably in Algebra I and Geometry. The deviations in consistency in the catego~ies of CP, CN, PC, PN, NC and NP may be due to changes in school or district curriculum policies or differences in class composition across years. These valiations may also depend on the specificity

and clarity of topic descriptions as well as on individual differences among teachers in their use of the response scale.

In Algebra I, with the exception of teacher T15 (detailed results are shown in Table A-2 in Appendix A), teachers covered topics for each course consistently across years. Topic coverage in Algebra I concentrates on the traditional core of introductory algebra (exponents, polynomials, algebraic equations, inequalities, rational expressions, absolute value). In Geometry, many more topics were covered as PRIOR compared to Algebra I, and the number of topics covered as CORE across years decreased considerably from Algebra I to Geometry as shown in Figure 1. Topics such as "Pythagorean Theorem," "perimeter and area of triangles," and "volume of cubes, cylinders," were covered as CORE; otherwise, topics covered as CORE in Algebra I were covered as PRIOR in Geometry. The idiosyncrasy of plots in the categories of CP, CN, PN and PC in Algebra I and Geometry occurs because teacher T15 taught an "advanced" class in 1988 and a "typical" class in 1989. This implies that studentst instructional experiences may be affected by class types.

Figure 2 shows the results of teachers' responses on content coverage across courses for two consecutive years. The results reported in Tables B-1 and B-2 in Appendix B show content coverages of 97 topics by the same teacher who taught different courses in 1988 or in 1989. These results show how the same topics were covered in low (i.e., lower than Pre-algebra) and high (i.e., Algebra I) levels of classes and how consistently a teacher covered topics in different courses across years. About 22 percent of topics were covered as CORE across courses such as Math A and Algebra I, Lower than Pre-algebra and Pre-algebra, and Algebra I and Geometry. About 31 percent of topics were NOT TAUGHT across courses, which was the same percentage as in Figure 1. These results support the results of consistent content coverage across years in Figure 1. As expected, the categories of CP and NC showed a reasonable transition in content coverage across courses.

In the category of CP, there was a big transition in content coverage from Algebra I to Geometry. About 60 topics were covered consistently as CORE in Algebra I and as PRIOR in Geometry by the same teacher across years. In this category all the lower level courses were compared with higher courses which showed a logical expectation of content coverage across courses. Similarly, the category of NC shows that 19 percent of topics across courses were covered as NC, and lower level courses compared with higher level courses.

The categories of CN, PC and PN clearly provide other evidence of validity of teachers' responses on content coverage by showing almost zero percent of topic coverage in these categories across lower level and higher level courses. There was almost no topic covered as PRIOR in Math A and as CORE in Algebra I, or as PRIOR in Pre-algebra and as CORE in Geometry. These results strongly support the validity of teachers' responses on content coverage in a given course. Topics taught differently across courses are "finding sum of interior angles," "isosceles and equilateral triangles," and "congruent triangles," taught as CORE in Prealgebra, as PRIOR in Algebra I, but NOT TAUGHT in Lower than Pre-algebra.

Overall, the results above showed that the prevalence and type of coverage of topics were consistent with their curricular sequence across years. Patterns were consistent with logical expectations for the topic within a given course across years and across teachers; therefore, cross-validation of teachers' responses on content coverage in a specific topic category (for a specific course) was successful.

Relationships with Performance

The p-value differences between 1988 and 1989 at the item level for classes taught by the same teacher in successive years and the relationship of these differences to differences in teachers' reported coverage of topics are reported in Figure 3 and Tables C-1 to C-5 in Appendix C. These results show the evidence of content validity of test items by analyzing what was taught at secondary school mathematics and what was tested. Furthermore, content coverage of test item topics was related to students' performance on the Algebra Readiness Test and Elementary Algebra Test.

Content coverage reports of test item topics in Tables C-1 to C-5 validated the content validity of test items in Algebra Readiness Test and Elementary Algebra Test by showing a consistent content coverage on the test item topics; topics which were claimed to be taught were most likely tested in both tests, and this validates the content validity of test items.

P-value difference distributions of students' performance on the Algebra Readiness Test and Elementary Algebra Test are shown in Figure 3. When topics were taught consistently across years as in the category of CC, p-values do not seem to vary across years. However, there were some deviations in p-values when topics were taught differently across years. For example, there was a pvalue mean difference of .04 when topics were covered as CORE and as PRIOR, and a .05 difference when topics were NOT TAUGHT in 1988 and covered as CORE in 1989.

However, these results are not convincing since these p-value differences are the average p-value differences across topics. When p-value differences were considered for each topic, some topics were relatively more sensitive to content coverage than others. For example, the topics "exponents with integral exponent," "order and comparison of fractions," and "perimeter and area of triangles and squares" showed relatively large p-value differences greater than .20. These topics were taught as CORE in 1988 and as PRIOR in 1989. In Math A, the topics "simplification of a rational expression" and "multiplication and division of fractions" showed relatively large p-value differences greater than .13. These topics were covered as CORE in 1988 and as PRIOR in 1989. These topics are sensitive to content coverage and to an effect of different content coverage on students' performance. In Pre-algebra, the topic "location of points in coordinate plane" showed a p-value difference of .15, and it was NOT TAUGHT in 1988 and taught as CORE in 1989. This topic was sensitive to content coverage, which clearly shows that exposure to a topic influences students' performance. The topics "basic operations with signed number" and "addition and subtraction of decimals" showed p-value differences but were not sensitive to content coverage, which implies that relatively easy topics do not seem to be influenced as much as fairly hard topics. In Algebra I, the topic "Pythagorean Theorem and special triangle" also seems to be sensitive to content coverage, showing a p-value difference of .12; it was NOT TAUGHT in 1988 and taught as CORE in 1989. The topics "algebra operation of literal symbol," "circumference and area of circle," "addition and subtraction of square roots" and "solving quadratic equation by factoring" also provided evidence of the effect of content coverage by showing very low p-values and small p-value differences less than .05; these topics were NOT TAUGHT across years. These results are shown in Tables C1 to C5.

Implication

We considered the validity of teachers' responses on students' instructional experiences (content coverage) and viewed student test performance as supporting evidence. The patterns of responses were potentially realistic portrayals of coverage for different courses and topics at certain levels of specificity. This study provided an insight into the functioning of teachers' questionnaire responses about content coverage by examining and monitoring instructional practices.

Since the effect of content coverage is sensitive to the level of item difficulty, analyzing p-value differences as a function of the level of item difficulty, teachers' characteristics and content coverage might be interesting. Because teachers responded to the questionnaire without looking at the test items in this study, taking consideration of item difficulty in an analysis would also be worthwhile.

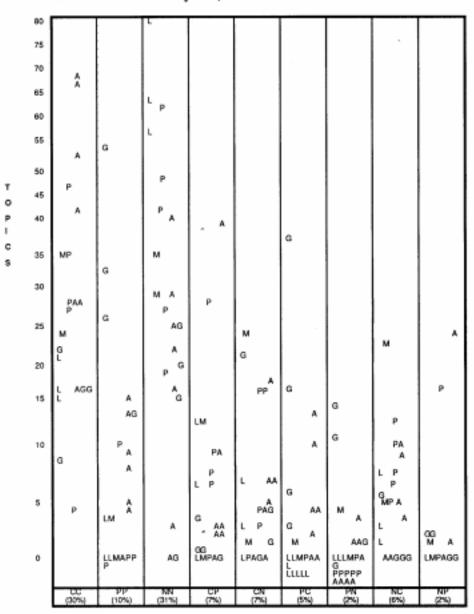
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Figure 1. Plot of Topics with Content Coverage by Courses (Teachers' responses of content coverage for the same course for two consecutive years)



Content Coverage

L: Lower than Pre-algebra M: Math A

A: Algebra I G: Geometry

P: Pre-algebra

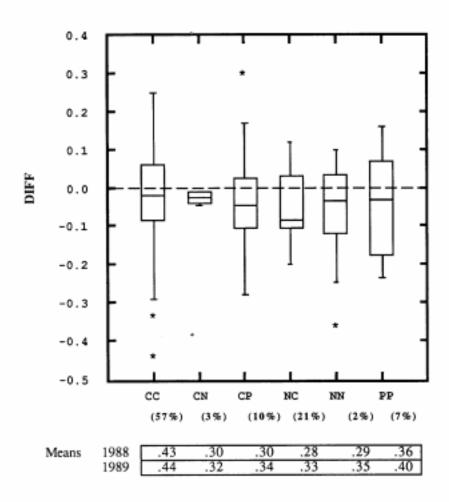
Figure 2. Plot of Topics with Content Coverage by Courses (Teachers' responses of content coverage for the different courses for two consecutive years)

		OC (22%)	PP (2%)	NN (31%)	CP (21%)	CN (1%)	PG LM PC (0%)	PN (0%)	NC (19%)	NP (4%)
	0	MG	MA AG LP MG PG		LP LM	MA AG LP MG PG LM	MA AG AG LP LP MG PG LM	MA AG AG LP LP MG PG LM	LM	MA AG AG LP LP MG LM
	5		AG LP		MA LP	AG LP			AG	
	10	AG			l				AG.	
	15	AG	LM	AG	PG				LP	
	20	LP LM		PG MG MA AG	мз				MG	
	25			LP						
8	30	PG LP							MA PG	
c	35									
P	40	MA							"	MG
T D	45								LP	
	50									
	55			LP						
	60					AG AG				
	65				LM					
	70									
	75									
	80									

Content Coverage

MA: Math A in 1988 and Algebra I in 1989
PG: Pre-algebra in 1988 and Geometry in 1989
AG: Algebra I in 1988 and Geometry in 1989
LP: Lower than Pre-algebra in 1988 and Pre-algebra in 1989
MG: Math A in 1988 and Geometry in 1989
LM: Lower than Pre-algebra in 1988 and Math A in 1989

Figure 3. P-value Difference Distributions of Students' Performance on Algebra ReadinessTest and Elementary Algebra Test



CONTENT

TABLE A-1 1988/1989 TEACHER CONTENT COVERAGE BY SAME TEACHER SAME COURSES ACROSS YEARS (Algebra Readiness Test)

	COURSE:		WER THE		MAT	ПНА		PRE	-ALGE	BRA	
ITEMS	TEACHER:	T16	T17	T18	Tı	Т3	T5	T8	T12	T14	T20
1 BASIC OPERATIONS WITH S	IGNED NO.	cc	cc	NN	СР	cc	CP	СС	СС	cc	CP
2 PRIME FACTORIZATION		CC	CC	NN	CC	CC	CC	CC	CC	CC	CP
3 FINDING DISTANCES ON NU	MBER LINE '	CC	CC	NN	CC	CC	CC	CC	CP	NC	CP
4 USING DEFINITION OF DIVI		CC	CC	NN	CC	CC	CP	CC	CP	CC	CP
5 'ADD, & SUB, OF FRACTION		CP	CP	CC	CP	CC	CP	CP	CP	CC	PP
6 MUL, & DIV, OF FRACTIONS		CP	CP	CC	CP	CC	CP	CP	CP	CC	PP
7 ORDER & COMPARISON OF		CP	CP	CC	CP	CC	CC	CP	CP	CC	PP
8 SIMPLIF, OF COMPLEX FRA		CP	CP	CC	CP	CC	CC	CP	CP	CC	CP
9 'ADD. & SUB OF DECIMALS	,	CP	CP	CC	CP	CC	CP	CP	CP	CC	PP
0 'MUL. & DIV. OF DECIMALS		CP	CP	CC	CP	CC	CP	CP	CC	CC	PP
1 ESTIMATION & APPROXIMA		CC	CC	CC	CP	NP	cc	CC	CC	CC	PP
2 CONV. BET. FRACTIONS &		CC	CP	CC	CP	CC	cc	CC	CC	CC	pp
3 CONV. BET. FRACTIONS &		CC	CP	CC	CP	CC	cc	CC	CC	CC	PP
4 COMPUT. WITH DECL & FR		CC	CC	CC	CP	CC	cc	CC	cc	CC	pp
5 COMPUTATION OF PERCEN		CC	CP	CC	CP	CC	cc	CC	CC	CC	PP
6 CONCEPT OF PROPORTION		cc	PP	CC	cc	PP	cc	CC	CC	CC	cc
7 COMPUTATION OF PROPOR		CC	PP	CC	cc	PP	cc	CC	CC	CC	CE
		cc	PP	cc	cc	PP	cc	CC	CC	CC	CE
18 'APPLIC, OF RATIO OR PROF		cc	CP	NN	cc	CC	cc	NN	CC	NC	CE
9 'APPLIC. LAWS OF EXPONE?		cc	CP	NN	cc	PC	cc	NN	cc	CC	CI
20 POWERS OF 10 & SCIENTIF		8	CP	NN	cc	NC	cc	NC	CN	NC	CE
21 EXPONENT. WITH INTEGRA		NC	NC	NN	cc	PN	cc	CC	CN	NC	cc
22 'SQ. ROOT OF PERFECT SQU		NN NN	NC	NN	cc	PN	cc	CC	CN	NN	NI
23 SIMPLIFICATION OF SQ. RO		NN NN	NC	NN NN	cc	PN	cc	CN	CN	NN	N
24 'ADD. & SUB. OF SQ. ROOTS							cc	CN	CN	NN	N
25 MUL. & DIV. OF SQ. ROOTS		NN	NC	NN	CN NN	PN NN	CP	NN	CN	NN	NN NN
26 CONV. BET. RADICALS & R		NN	NN	NN							
27 RATIONALIZ, OF NUMERA.		NN	NN	NN	NC	NN	CP	NN	NN	NN	N
28 'ADD. AND SUB, OF RADICA		NN	NN	NN	NN	NN	CN	NN	NN	NN	N.
29 NUM, CALCU, W/ EXPONEN		NN	NN	NN	NC	CN	cc	NN	NN	NN	NP.
30 'ALGE, CALCU, W/ EXPONE		NN	NN	NN	NN	CN	CP	NN	NN	NN	N
SI FACTORING & SIMPLI. ALC		NN	NN	NN	NC	CN	cc	NN	NN	NN	N
32 ESTIM. & APPROXI. WITH R		NN	NN	NN	NC	NN	cc	NN	NC	NN	N
3 'ALGE OPERATION OF LITER		CN	NN	NN	CC	CN	cc	cc	NN	CC	C
34 'SIMPLIF, OF POLYNO, BY O		NN	NN	NN	NC	CN	CN	cc	NN	NC	C
5 'ADD. & SUB, OF POLYNOM		NN	NN	NN	CC	CN	CN	CC	NN	NN	C
6 EVALUATION OF A POLYN		NN	NN	NN	cc	CN	CN	CC	NN	NC	CI
37 MUL, OF MONOMIAL WITH	A POLYNO.	NN	NN	NN	cc	CN	CN	NN	NN	NN	CI
88 'MUL, OF TWO BINOMIALS		NN	NN	NN	NC	CN	CN	NN	NN	NN	N
9 'DIVISION OF POLYNOMIAL	5	NN	NN	NN	CC	CN	CN	NN	NN	NN	N
40 SQUARING A BINOMIAL		NN	NN	NN	NC	CN	CN	NN	NN	NN	N
1 FACTOR, POLYNOMIALS		NN	NN	NN	NC	CN	CN	NN	NN	NN	CI
12 FACTOR, TRINOMIAL OVER		NN	NN	···NN	NN	CN	CN	NN	NN	NN	N
43 'FACTOR, PERFECT SQ, TRI		NN	NN	NN	NC	CN	CN	NN	NN	NN	N
44 'SIMPLIF, OF COMPLEX NU		NN	NN	NN	NN	NN	CN	NN	NC	NN	N
45 YONE UNKNOWN WITH NUM		NN	NN	NN	CC	CC	CC	CC	CC	NN	C
46 ONE UNKNOWN WITH LIT.	COEFFI. '	NN	NN	NN	CC	CC	CC	CC	CC	NN	N
47 'SIMPLE LIN. EQUA. IN ONE	UNKNOWN'	NN	NN	NN	CC	CC	CC	CC	CN	NN	C
48 TWO UNKNOWN BY ELIMIN	VATION '	NN	NN	NN	NN	NN	CC	CN	NN	NN	N
49 TWO UNKNOWN BY SUBST	TUTION .	NN	NN	NN	NN	NN	cc	CN	NN	NN	N
50 APPLICATION OF EQUATIO	a.re	NN	NN	NN	NN	CC	CC	CC	CC	NN	C

TABLE A-1 (continued)

	COURSE:		WER TE		MA	ΤΗΑ		PRE	E-ALGE	BRA	
ITEMS	TEACHER:	T16	T17	T18	Tl	T3	T5	T8	T12	T14	T2
1 'GENERATING EQUATIONS FRO	M DESCR.	NN	NN	NN	СС	сс	сс	сс	CN	NN	C
2 'SOLV, EQUA, FROM FACTORED		NN	NN	NN	NN	NN	NC	NN	NN	NN	N
SOLVING QUAD EQUAT BY FAC		NN	NN	NN	NN	NN	NC	NN	NN	NN	N
4 'SOLV, QUAD, EQUA, BY QUADE		NN	NN	NN	NN	NN	NC	NN	NN	NN	N
GRAPHS OF QUADRATIC RELAT		NN	NN	NN	NC	NN	NC	NN	NN	NN	Ñ
6 'ONE UNKNOWN WITH NUM, CO		NN	NN	NN	CC	CN	cc	CC	CN	NN	c
SOLUT, OF QUADRATIC INEQUA		NN	NN	NN	NC	NN	CC	NN	CN	NN	Ñ
GRAPHING LIN. INEO. IN ONE U		NN	NN	NN	cc	CN	cc	CC	CC	NN	N
9 'SIMPLIF, OF A RATIONAL EXPR		NN	NN	NN	CC	CN	CC	CC	NC	NN	c
EVALUATION OF A RATIONAL E	EXPRE.	NN	NN	NN	CC	CC	cc	CC	NC	NN	č
1 'ADD, & SUB, OF RATIONAL EXI	PRE.	NN	NN	NN	cc	CN	CC	CC	NC	NN	č
2 'MUL. & DIV. OF RATIONAL EXP		NN	NN	NN	CC	NN	CC	CC	NC	NN	Č
3 'PROBABILITY		CC	CN	NN	CC	CC	NN	NN	CC	NN	N
4 'DESCRIPTIVE STATISTICS		CC	CN	NN	NC	CC	NN	NN	CC	NN	N
5 GRAPH READING		CC	CC	NN	CC	CN	cc	CC	CC	NC	C
6 LOCATI, OF POINTS IN CORD. P.	LANE'	CC	CC	NN	cc	CN	CC	CC	CC	NC	C
DISTANCE BET. TWO POINTS IN	COR.	cc	CC	NN	NC	NN	cc	CC	CC	NC	N
PERIMETER & AREA OF TRIANG	GLES,SQ '	CC	CC	CC	CC	CN	cc	CC	CC	CC	C
9 'CIRCUMFERENCE & AREA OF O	IRCLE '	CN	CC	NC	CC	CN	CC	CC	CC	CC	C
O'VOL, OF CUBES, CYLINDERS, RI	ECTAN.	NN	CC	NC	cc	NN	cc	NC	CC	NN	N
1 FINDING SUM OF INTERIOR AND	GLES '	CN	CC	NN	NC	NC	NN	NC	CC	CC	N
2 TSOSCELES & EQUILATERAL TR	IANGLE '	CN	CC	NN	NC	NC	NC	NC	CN	CC	N
3 'APPLIC., CONGRUENT TRIANG	LES '	CN	CC	NN	NC	NN	NC	NN	CN	CC	N
4 'APPLIC., SIMPLE TRIANGLES	,	CN	CC	NN	NC	NN	NC	NN	CN	CC	N
5 PYTHAGOREAN THEOREM & SI	PECLTR.	NN	NC	NN	NC	NC	CC	NN	CC	NC	N
6 PARALLELISM & PERPENDICUL	ARITY	NN	CC	NN	NN	NC	NN	NN	CN	CC	N
7 PROOFS(FORMAL DEDUCTIVE I	DEMONST. '	NN	NN	NN	NN	NN	NN	NN	NN	NN	N
8 TRANSFORMATIONS(TRANSLA	TION.	NN	NN	NN	NN	NN	NN	NC	NN	NN	N
9 VECTORS		NN	NN	NN	NN	NN	NN	NN	NN	NN	N
0 'SIMPLIF. & EVALU. OF EXPRES	S.	NN	NC	NN	CC	NN	cc	CC	CN	NN	N
1 SOLUTION OF EQUATIONS		NN	NC	NN	NC	NN	cc	NN	CN	NN	N
2 FUNCT, CONCEPT & USE OF NO	TATION '	NN	NN	NN	CC	CN	CN	NN	NN	NN	C
3 FUNCT. EVALUATION USING SU	JBSTIT.	NN	NN	NN	CC	CN	CN	NN	NN	NN	C
4 COMPOSITION OF FUNCTION		NN	NN	NN	NN	NN	CN	NN	NN	NN	N
5 GRAPHING OF FUNCTION		NN	NN	NN	NN	NN	CN	NN	NN	NN	N
6 NUMERICAL FUNCTIONAL EVA		NN	NN	NN	NN	CN	NN	NN	NN	NN	N
SUBSTITUTING LITERAL EXPRE	SSS.	NN	NN	NN	NN	NN	NN	NN	NN	NN	N
B DEFINITION, LAWS & RULES	'	NN	NN	NN	NN	NN	NN	NN	NN	NN	N
INVERSE RELATION BET, LOG.		NN	NN	NN	NN	NN	NN	NN	NN	NN	N
SOLUTION OF LOG. AND EXP. F		NN	NN	NN	NN	NN	NN	NN	NN	NN	N
GRAPHING OF LOG. AND EXP. F	UNCT.	NN	NN	NN	NN	NN	NN	NN	NN	NN	N
2 FIND. ALGEBRAIC EXPRESS		NN	NN	NN	NN	NN	NN	NN	NN	NN	N
3 DESCRIB. VARIATIONS OF FUN		NN	NN	NN	NN	NN	NN	NN	NN	NN	N
FIND, SIDE LENGTHS IN SPEC.T		NN	NN	NN	NC	NN	'NN	NN	NN	NN	N
5 GRAPHING TRIGONOMETRIC FU		NN	NN	NN	NN	NN	NN	NN	NN	NN	N
6 REDUCING TRIGONOMETRIC E		NN	NN	NN	NN	NN	NN	NN	NN	NN	N
7 PROOF OF TRIGONOMETRIC ID:	ENTITIE '	NN	NN	NN I	NN	NN	NN	NN	NN	NN	N

TABLE A-2 1989/1989 TEACHER CONTENT COVERAGE BY SAME TEACHER SAME COURSES ACROSS YEARS (Elementary Algebra Test)

TTEMS	COURS	E:		Α.	LGEBR	ΑI				GBON	ŒTRY	
2 PRIME FACTIORIZATION CC	ITEMS TEACHE	R: T4	T10	T11	T13	T14	T15	T19	T4	T7	Т9	T15
STENDING DISTANCES ON NUMBER LINE CC	1 BASIC OPERATIONS WITH SIGNED NO.	· co	: cc	PC	PC	CP	СР	сс	PP	PP	PP	PC
4 'USING DEFINITION OF DIVISIBILITY	2 'PRIME FACTORIZATION	. co	cc cc		-	-	-		PP	-		
S ADD. & SUB. OF FRACTIONS	3 FINDING DISTANCES ON NUMBER LINE											
6 MUIL. & DIV. OF FRACTIONS CC CC PC PC PC PP PP PP PP PP PP PP PP	4 'USING DEFINITION OF DIVISIBILITY											
7 ORDER & COMPARISON OF FRACTIONS CC CC PC PC PC PP PP PP PP PP PP 8 SIMPLIF OF COMPLEX FRACTIONS CC CC CC PC PP PP CC PP PP CC PP PC PP PP											-	
8 SIMPLIF OF COMPLEX FRACTIONS CC CC PC PC PP PP PP PP PP 99 AND PP 99 P												
9 'ADD. & SUB OF DECIMALS CP CC PC PC PP PP PP PP PP PP PP PP PP P												
10 MUL. & DIV. OF DECIMALS												
TESTIMATION & APPROXIMATION												
12 CONV. BET. FRACTIONS & DECIMALS CC CC PP PC PP PP PP P											-	-
13 CONV. BET. FRACTIONS & PERCENT CC CP PP PC PP PP PP PP PP PP PP PP PP P												
14 COMPUT. WITH DECL & FRAC, ROUND. CC CC PP PC PC		-										
15 COMPUTATION OF PERCENT		_									-	
16 CONCEPT OF PROPORTION				PC	PP	CP	PP	CN	PP	PC	PP	PP
17 *COMPUTATION OF PROPORTIONS	10 00010 000100000000000000000000000000	· C	C CC	PC	PP	CP	PP	CC	CP	PC	CC	PP
19 APPLIC. LAWS OF EXPONENTS CC CC NC CC CC CC CC PP PC PP PC 20 'POWERS OF 10 & SCIENTIFIC NOTAT. CC CC NC CC CC CC CC CC CC CC PP PN PC 21 'EXPONEN. CC CC NC CC CC CC CC CC CC CC PP PN PC 22 'SQ. ROOT OF PERFECT SQUARES CC CC NC CC NN PC CC CC CC PP PP PP PC 23 'SIMPLIFICATION OF SQ. ROOTS CC CC NC CC NN PC CC CC PC P		. C	CP CP	PC	PP	CP	PP	CC	CP	PC	CC	PP
20 POWERS OF 10 & SCIENTIFIC NOTAT. CC CC NP CC CC CC CC CC CC PP PN PC 21 EXPONENT. WITH INTEGRAL EXPONEN. CC CC NC CC CC CC CC CC PP PP PP PC 22 'SQ. ROOT OF PERFECT SQUARES CC CC CC NN PC CC CC PP CC PC PC PC PC PC PC PC PC	18 'APPLIC, OF RATTO OR PROPORTIONS	, C	C CC		CP	CP	PP					
21 EXPONENT: WITH INTEGRAL EXPONEN. CC CC NC CC CC CC CC PP PP PP PC 22 'SQ. ROOT OF PERFECT SQUARES CC CC PP CC NN PC CC CC PC CC PC 23 'SIMPLIFICATION OF SQ. ROOTS CC CC NC CC NN PC CC CC PC CC PC 24 'ADD. & SUB. OF SQ. ROOTS CC CC NC CC NN PC CC CC PC CC PC C2 'S MUL. & DIV. OF SQ. ROOTS CC CC NC CC NN PC CC CC PP CC PC 25 'MUL. & DIV. OF SQ. ROOTS CC CC NC CC NN PC CC CC PP CC PC 26 'CONV. BET. RADICALS & RAT. EXPO. CC CC NC CC NN PC CC CC PP CC PC 26 'CONV. BET. RADICALS & RAT. EXPO. CC CC NC CC NN CC CN PP CC PC 27 'RATIONALIZ. OF NUMERA. & DENOMI. CC CC CN CC NN CC CC PP CC CC PN 28 'ADD. AND SUB. OF RADICAL EXPRE. CC CC CN CC NN CC CC PP CC CC PN 29 'NUM. CALCU. W/EXPONENTS & RAD. CC CC CN CC NN CC CC PP CC NP PN 30 'ALGE. CALCU. W/EXPONENTS & RAD. CC CC CN CN NN CC CC PP CC NP PN 31 'FACTORING & SIMPLI. ALGE. EXPRE. CC CC CN CN NN CC CC PP CC NP PN 32 'ESTIM. & APPROXI. WITH RADICALS. CC CC CN CN NN CC CC PP CC NP PN 33 'ALGE OPERATION OF LITERAL SYMBOL. CC CC CC CC CC CC CC CP CC PP PP PP PP	19 'APPLIC. LAWS OF EXPONENTS											
22 'SQ, ROOT OF PERFECT SQUARES			_									
23 'SIMPLIFICATION OF SQ. ROOTS												
24 'ADD. & SUB. OF SQ. ROOTS												-
25 MULL & DIV. OF SQ. ROOTS CC CC NC CC NN PC CC PP CC PC 26 CONV. BET. RADICALS & RAT. EXPO. CC CC CN CC NN CC CC PP CC PP 27 RATIONALIZ. OF NUMERA & DENOMI. CC CC CN CC NN CC CC PP CC CC PN 28 'ADD. AND SUB. OF RADICAL EXPRE. CC CC CN CC NN CC CC PP CC NN PN 29 NUM. CALCU. W/EXPONENTS & RAD. CC CC CN CC NN CC CN PP CC NN PN 30 'ALGE. CALCU. W/EXPONENTS & RAD. CC CC CN CC NN CC CN PP CC NN PN 31 'FACTORING & SIMPLI. ALGE. EXPRE. CC CC CN CN NN CC CN PP CC NN PN 32 'ESTIM. & APPROXI. WITH RADICALS. CC CC CN CN NN CC CC PP CN PP PC NN PN 33 'ALGE OPERATION OF LITERAL SYMBOL. CC CC CC CC CC CC CP PP PP PP PP PP 34 'SIMPLIF. OF POLYNO. BY GROUPING. CC CC CC CC CC CC CC CP CC PP PP PP PP P										-		
26 'CON', BET, RADICALS & RAT, EXPO. CC CC CN CC NN CC CC PP CC CC PN 27 'RATIONALIZ. OF NUMERA. & DENOMI. CC CC CN CC NN CC NN CC CC PP CC PN 28 'ADD. AND SUB, OF RADICAL EXPRE. CC CC CN CC NN CC CC PP CC PP CP NN PN 29 'NUM. CALCU. W/ EXPONENTS & RAD. CC CC CN CC NN CC CN PP CC NP PN 30 'ALGE, CALCU. W/ EXPONENTS & RAD. CC CC CN CC NN CC CN PP CC NP PN 31 'FACTORING & SIMPLI. ALGE, EXPRE. CC CC CN CN NN CC CN PP CC NN PN 32 'ESTIM. & APPROXI. WITH RADICALS. CC CC CN CN NN CC CN PP CN NC PN 33 'ALGE OPERATION OF LITERAL SYMBOL. CC CC CC CC CC CC CP CC PP PP PP PP PC 34 'SIMPLIF, OF POLYNO, BY GROUPING. CC CC CC CC CC CC CC CP CC PP PP PP PP		-										
27 'RATIONALIZ. OF NUMERA. & DENOMI. CC CC CN CC CN CC PP CC PN P P P P P P											_	-
28 'ADD, AND SUB, OF RADICAL EXPRE.												
29 NUM. CALCU. W/EXPONENTS & RAD. CC CC CN CC NN CC NN CC NP PC NN PN 30 'ALGE. CALCU. W/EXPONENTS & RAD. CC CC CN CN CN NN CC CN PP CC NN PN 31 'FACTORING & SIMPLI. ALGE. EXPRE. CC CC CN CN NN CC CN PP CC NN PN 32 'ESTIM. & APPROXI. WITH RADICALS. CC CC CN CN NN CC CN PP CC NC PN 33 'ALGE OPERATION OF LITERAL SYMBOL. CC CC CC CC CC CC CP CC PP PP PP PP PP P	# · · · · · · · · · · · · · · · · · · ·										-	
30 'ALGE. CALCU. W/ EXPONENTS & RAD. CC CC CN CN CN PP CC NN PN 31 'FACTORING & SIMPLI. ALGE. EXPRE. CC CC CN CN NN CC CN PP CC NC PN 32 'ESTIM. & APPROXI. WITH RADICALS. CC CC CN CN NN CC CC PP CN NC PN 32 'ESTIM. & APPROXI. WITH RADICALS. CC CC CC CN CN NN CC CC PP CN NC PN 33 'ALGE OPERATION OF LITERAL SYMBOL. CC CC CC CC CC CC CP CC PP PP PP PP PC 34 'SIMPLIF. OF POLYNO. BY GROUPING. CC CC CC CC CC CC CC CP CC PP PP PP PP												
31 FACTORING & SIMPLI, ALGE, EXPRE. CC CC CN CN NN CC CN PP CN NC PN 32 ESTIM. & APPROXI, WITH RADICALS. CC CC CN CN NN CC CC PP CN NC PN 33 'ALGE OPERATION OF LITERAL SYMBOL CC CC CC CC CC CC CC CP CC PP PP PP PP									PP			
32 ESTIM. & APPROXI. WITH RADICALS. CC CC CN CN NN CC CC PP PP PP PP PC 33 'ALGE OPERATION OF LITERAL SYMBOL CC CC CC CC CC CC CC CP CC PP PP PP PP									PP			
34 SIMPLIF, OF POLYNO, BY GROUPING. CC CC CC CC CC CP CC PP PP PP PP PC 35 ADD. & SUB. OF POLYNOMIALS CC CC CC CC CC CC CP CC PP PP PP PP PC 36 EVALUATION OF A POLYNOMIAL(1/2) CC CC CC CC CC CC CP CC PP PP PP PP PC PC		· O	C CC	CN	CN	NN	CC	CC	PP	CN	NC	PN
35 'ADD. & SUB. OF POLYNOMIALS	33 'ALGE OPERATION OF LITERAL SYMBOL	, a	C CC	CC	CC	CC		CC	PP	PP	PP	
36 EVALUATION OF A POLYNOMIAL(1/2) CC CC CC CC CC CP CC PP PP PP PC PC 37 MUL OF MONOMIAL WITH A POLYNO. CC CC CC CC CC CC CP CC PP PP PP PC 90 MILL OF TWO BINOMIALS CC CC CC CC CC CC CC CP CC PP PP PP PP	34 'SIMPLIF. OF POLYNO. BY GROUPING.											
37 MUL OF MONOMIAL WITH A POLYNO. CC CC CC CC CC CP CC PP PP PP PC 38 MUL OF TWO BINOMIALS CC CC CC CC CC CC CP CC PP PP PP PP PC 39 DIVISION OF POLYNOMIALS CC CC CC CC CC CC CP CC PP PP PP NN PN 40 SQUARING A BINOMIAL CC CC CC CC CC CC CC CP CC PP PP PP PP							-					
38 MUL OF TWO BINOMIALS CC CC CC CC CC CP CC PP PP PP PC 39 'DIVISION OF POLYNOMIALS CC CC CC CC CC CC CP CC PP PP NN PN 40 'SQUARING A BINOMIAL CC CC CC CC CC CC CC CP CC PP PP PP PP												
39 'DIVISION OF POLYNOMIALS CC CC CC CC CC CP CC PP PP NN PN 40 'SQUARING A BINOMIAL CCC CC CC CC CC CC CC CP CC PP PP PP PP							-					
40 SQUARING A BINOMIAL CC CC CC CC CC CP CC PP PP PP PC 41 FACTOR. POLYNOMIALS CC CC CC CC CC CC CP CC PP PP PP PC 42 FACTOR. TRINOMIAL OVER INTEGERS CC CC CC CC CC CC CP CC PP PP PP PC 43 FACTOR. PERFECT SQ. TRINOMIALS CC CC CC CC CC CP CC PP PP PP PC 44 SIMPLIF. OF COMPLEX NUMBERS CC CC CC CC CC CC CP CC PP PP PP NN PC 45 SIMPLIF. OF COMPLEX NUMBERS CC CC CC CC CC CC CC CP CC PP PP NN PC 45 ONE UNKNOWN WITH NUM. COEFFL CC CC CC CC CC CP CC PP PP PP NN PC 46 ONE UNKNOWN WITH LIT. COEFFL CC CC CC CC CP CC PP PP NN PC												
41 FACTOR, POLYNOMIALS CC CC CC CC CC CP CC PP PP PP PP PC 42 FACTOR, TRINOMIAL OVER INTEGERS CC CC CC CC CC CC CP CC PP PP PP PP PC 43 FACTOR, PERFECT SQ. TRINOMIALS CC CC CC CC CC CC CP CC PP PP PP PP PC 44 SIMPLIF, OF COMPLEX NUMBERS CC CC CC CC CC CC CP CC PP PP PP NN PC 45 ONE UNKNOWN WITH NUM. COEFFL CC CC CC CC CC CC CP CC PP PP PP NN PC PC CC ONE UNKNOWN WITH LIT. COEFFL CC CC CC CC CC CP CC PP PP PP NN PC PC CC ONE UNKNOWN WITH LIT. COEFFL CC CC CC CC CC CP CC PP PP PP NN PC PC CC ONE UNKNOWN WITH LIT. COEFFL CC CC CC CC CC CP CC PP PP PP NN PC PC CC ONE UNKNOWN WITH LIT. COEFFL												
42 FACTOR. TRINOMIAL OVER INTEGERS CC CC CC CC CC CP CC PP PP PP PC 43 FACTOR. PERFECT SQ. TRINOMIALS CC CC CC CC CC CC CP CC PP PP PP PC 44 SIMPLIF. OF COMPLEX NUMBERS CC CC CC CC CC CC CP CC PP PP PP NN PC 45 ONE UNKNOWN WITH NUM. COEFFL CC CC CC CC CC CP CC PP PP PP NN PC 46 ONE UNKNOWN WITH LIT. COEFFL CC CC CC CC CC CP CC PP PP NN PC				_	-							
43 FACTOR, PERFECT SQ. TRINOMIALS CC CC CC CC CC CP CC PP PP PP PC 44 SIMPLIF, OF COMPLEX NUMBERS CC CC CC CC CC CC CP CC PP PP NN PC 45 ONE UNKNOWN WITH NUM. COEFFL CC CC CC CC CC CP CC PP PP PP NN PC 46 ONE UNKNOWN WITH LIT. COEFFL CC CC CC CC CC CP CC PP PP NN PC				-	-		-	-				
44 SIMPLIF, OF COMPLEX NUMBERS CC CC CC CC CP CC PP PP NN PC 45 ONE UNKNOWN WITH NUM. COEFFL CC CC CC CC CC CP CC PP PP NN PC 46 ONE UNKNOWN WITH LIT. COEFFL CC CC CC CC CC CP CC PP PP NN PC												
45 ONE UNKNOWN WITH NUM. COEFFL CC CC CC CC CC CP CC PP PP PC PC 46 ONE UNKNOWN WITH LIT. COEFFL CC CC CC CC CC CP CC PP PP NN PC		_										
46 ONE UNKNOWN WITH LIT. COEFFI. CC CC CC CC CC CP CC PP PP NN PC								-				
	47 SIMPLE LIN. EQUA. IN ONE UNKNOWN	. 0		CC	CC	CC	CP	CC	PP	PP	PC	PC
48 TWO UNKNOWN BY ELIMINATION CC CC CC CC CN CP CC PP PP PP PC	48 TWO UNKNOWN BY ELIMINATION											
49 TWO UNKNOWN BY SUBSTITUTION CC CC CC CC CN CP CC PP PP PP PC												
50 APPLICATION OF EQUATIONS CC CC CC CC CC CP CC PP PP CC PC	50 'APPLICATION OF EQUATIONS	. с	c cc	cc	CC	CC	CP	CC	PP	PP	CC	PC

TABLE A-2 (continued)

	COURSE:			A	LGEBR/	ΑI				GEOM	ETRY	
ITEMS 7	TEACHER:	T4	T10	T11	T13	T14	T15	T19	T4	T 7	T9	T
GENERATING EQUATIONS FROM	M DESCR.	сс	NC	сс	сс	СС	СР	сс	PP	PP	СС	Р
SOLV. EQUA. FROM FACTORED		CC	CC	NC	CC	NN	CP	CC	PP	PN	PC	P
'SOLVING OUAD EQUAT BY FAC		CC	CC	NC	CC	NN	CP	CC	PP	PN	CC	Ī
SOLV. QUAD. BQUA. BY QUADR		CC	CC	NC	CN	NN	CP	CC	PP	PN	NN	i
GRAPHS OF QUADRATIC RELAT		CC	CC	NN	NN	NN	CP	CC	PP	PN	NN	i
ONE UNKNOWN WITH NUM, CO		CC	CC	CC	CC	CC	CP	CC	PP	PN	PP	1
SOLUT. OF QUADRATIC INEQUA		CC	CC	CC	CN	NN	CP	CC	PP	PN	NN	i
GRAPHING LIN. INEQ. IN ONE U		CC	CC	CN	CN	CN	CP	CC	PP	PN	PP	Ī
'SIMPLIF. OF A RATIONAL EXPR		CC	CC	CC	CC	CC	CP	CC	PP	PN	PP	F
EVALUATION OF A RATIONAL E		CC	CC	CC	CC	CC	CC	CC	PP	PN	PP	Ī
'ADD. & SUB. OF RATIONAL EXI		CC	CC	CC	CC	CC	CP	CC	PP	PN	PP	I
MUL. & DIV. OF RATIONAL EXP		CC	CC	CC	CC	CC	CP	CC	PP	PN	PP	- 1
PROBABILITY		NC	NN	CN	NN	NN	CC	NN	NN	NN	NN	- 0
DESCRIPTIVE STATISTICS		NC	NN	NN	NN	NN	CC	NN	NN	NN	NN	(
GRAPH READING		CC	PC	CN	NN	CN	CP	CN	PC	CN	PP	- (
LOCATI, OF POINTS IN CORD, P.	LANE '	CC	PC	CN	NN	CN	CP	CC	PC	CC	PC	- 0
'DISTANCE BET. TWO POINTS IN		CC	PC	CN	NN	CC	CC	CC	PC	CC	CC	- 0
PERIMETER & AREA OF TRIANG		CC	PC	CP	NC	CP	CP	PC	cc	CC	CC	- (
'CIRCUMFERENCE & AREA OF C		NN	PP	CP	NC	PP	CP	NC	CC	CC	CC	Ò
'VOL, OF CUBES, CYLINDERS, RI		NN	PP	CP	NN	NN	CP	NN	CC	CC	CC	- 0
FINDING SUM OF INTERIOR AND		NC	PP	NN	NC	CP	NP	NN	CC	CC	CC	- (
ISOSCELES & EQUILATERAL TR		NC	PP	NN	NC	PP	NP	NN	CC	CC	CC	-
'APPLIC., CONGRUENT TRIANG		NC	PP	NN	NN	PP	NP	NN	CC	CC	CC	(
'APPLIC. SIMPLE TRIANGLES		NN	PP	NN	NN	PP	NP	NN	CC	CC	CC	-
PYTHAGOREAN THEOREM & SI	PECLTR. 1	NC	PP	CN	NC	NN	NP	NN	CC	CC	CC	- 0
PARALLELISM & PERPENDICUL		NC	PP	CN	NN	PN	NP	NC	CC	CC	CC	-
PROOFS(FORMAL DEDUCTIVE)		NC	PN	NN	NN	NN	NP	NN	CC	CC	CC	- (
TRANSFORMATIONS(TRANSLA		NN	PN	NN	NN	NN	NP	NN	NN	CN	NC	- (
VECTORS		NN	PN	NN	NN	NN	NP	NN	NN	CN	NN	(
SIMPLIF. & EVALU, OF EXPRES	S. "	CC	NC	CC	CC	NN	NP	NN	PP	NN	PP	(
SOLUTION OF EQUATIONS		CC	NC	CC	CC	CC	CP	CC	PP	NN	NN	- (
FUNCT, CONCEPT & USE OF NO	TATION '	CC	CC	CN	CN	NN	CC	NC	PP	NN	NP	- 1
FUNCT. EVALUATION USING SU		CC	CC	CN	NN	NN	CC	NC	PP	NN	NN	1
COMPOSITION OF FUNCTION		NC	CC	CN	NN	NN	CC	NC	NP	NN	NN	- 1
GRAPHING OF FUNCTION		NC	CC	CN	NN	NN	NP	NN	NP	NN	NC	- 1
NUMERICAL FUNCTIONAL EVA	LUATION '	NN	CC	NN	NN	NN	NP	NN	NN	NN	NN	- (
SUBSTITUTING LITERAL EXPRE	ESS.	NN	CC	NN	NN	NN	NP	NN	NN	NN	NN	(
DEFINITION, LAWS & RULES		NN	CC	NN	NN	NN	NP	NN	NN	NN	NN	- (
INVERSE RELATION BET. LOG.	& EXP '	NN	CC	NN	NN	NN	NP	NN	NN	NN	NN	-
SOLUTION OF LOG. AND EXP. F		NN	CC	NN	NN	NN	NP	NN	NN	NN	NN	-
GRAPHING OF LOG. AND EXP. F		NN	CC	NN	NN	NN	NP	NN	NN	NN	NN	Ċ
FIND. ALGEBRAIC EXPRESS		NN:	CN	NN	NN	NN	NP	NN	NN	NN	NN	Ċ
DESCRIB. VARIATIONS OF FUN	CTION '	NN	CN	NN	NN	NN	NP	NN	NN	NN	NN	(
FIND. SIDE LENGTHS IN SPEC.T		NN	CN	NN	NN	NN	NP	NN	CN	NN	NC	Ċ
GRAPHING TRIGONOMETRIC F	UNCTIONS'	NN	CN	NN	NN	NN	NP	NN	NN	NN	NN	- (
REDUCING TRIGONOMETRIC E		NN	CN	NN	NN	NN	NP	NN	NN	NN	NN	Ċ
PROOF OF TRIGONOMETRIC IDE		NN	CN	NN	NN	NN	NP	NN	NN	NN	NN	Č

TABLE B-1
TEACHER CONTENT COVERAGE BY SAME TEACHER DIFFERENT COURSES 1988

	MATH A ALGEBRA I	ALGEBRA ,GEOM	THAN PRE-ALG /PRE-ALG	MATH A /GEOM	PRE-ALG /GEOM
ITEMS TEACHER:	T1	T4	T5	T7	Т8
1 BASIC OPERATIONS WITH SIGNED NO.' 2 PRIME FACTORIZATION' 3 FINDING DISTANCES ON NUMBER LINE 4 USING DEFINITION OF DIVISIBILITY' 5 'ADD. & SUB. OF FRACTIONS' 6 MUL. & DIV. OF FRACTIONS' 7 'ORDER & COMPARISON OF FRACTIONS' 8 SIMPLIF. OF COMPLEX FRACTIONS' 9 'ADD. & SUB OF DECIMALS' 10 'MUL. & DIV. OF DECIMALS' 11 'ESTIMATION & APPROXIMATION' 12 'CONV. BET. FRACTIONS & DECIMALS' 13 'CONV. BET. FRACTIONS & PERCENT' 14 'COMPUT. WITH DECI & FRAC, ROUND' 15 'COMPUTATION OF PERCENT' 16 'CONCEPT OF PROPORTION' 17 'COMPUTATION OF PERCENT' 16 'CONCEPT OF PROPORTION' 17 'COMPUTATION OF PROPORTIONS' 18 'APPLIC. LAWS OF EXPONENTS' 20 POWERS OF 10 & SCIENTIFIC NOTAT.' 21 'EXPONENT. WITH INTEGRAL EXPONEN.' 22 'SQ. ROOT OF PERFECT SQUARES' 23 'SIMPLIFICATION OF SQ. ROOTS' 24 'ADD. & SUB. OF SQ. ROOTS' 25 'MUL. & DIV. OF SQ. ROOTS' 25 'MUL. & DIV. OF SQ. ROOTS' 26 'CONV. BET. RADICALS & RAT. EXPO.' 27 'RATIONALIZ. OF NUMERA. & DENOMI.' 28 'ADD. AND SUB. OF FADICAL EXPRE.' 29 NUM. CALCU. W/ EXPONENTS & RAD.' 30 'ALGE. CALCU. W/ EXPONENTS & RAD.' 31 'FACTORING & SIMPLI. ALGE. EXPRE.' 22 'STIM. & APPROXI, WITH RADICALS.' 33 'ALGE OPERATION OF LITERAL SYMBOU' 34 'SIMPLIF. OF POLYNOMIALS' 35 'ADD. & SUB. OF POLYNOMIALS' 36 'EVALUATION OF A POLYNOMIALS' 37 'MUL. OF TWO BINOMIALS' 40 'SQUARING A BINOMIALS' 41 'FACTOR, POLYNOMIALS' 42 'FACTOR, PERFECT SQ. TRINOMIALS ' 44 'SIMPLIF. OF COMPLEX NUMBERS' 45 'FACTOR, PERFECT SQ. TRINOMIALS ' 46 'SIMPLIF. OF COMPLEX NUMBERS' 47 'FACTOR, PERFECT SQ. TRINOMIALS ' 48 'SIMPLIF. OF COMPLEX NUMBERS' 49 'FACTOR, PERFECT SQ. TRINOMIALS ' 49 'SUARING A BINOMIALS' 40 'SQUARING A BINOMIALS' 41 'FACTOR, PERFECT SQ. TRINOMIALS ' 42 'FACTOR, PERFECT SQ. TRINOMIALS ' 43 'SIMPLIF. OF COMPLEX NUMBERS' 44 'SIMPLIF. OF COMPLEX NUMBERS' 45 'CONE UNKNOWN WITH NUM. COEFFI.' 46 'ONE UNKNOWN WITH NUM. COEFFI.' 47 'SIMPLE LIN. EQUA. IN ONE UNKNOWN' 48 'TWO UNKNOWN BY SUBSTITUTION'	55555555555555555555555555555555555555	++++++++++++++++++++++++++++++++++++++	55 55 55 55 55 55 55 55 55 55 55 55 55		888888888888888888888888888888888888888

TABLE B-1 (continued)

	COURSE:	MATH A /ALGEBRA I	ALGEBRA /GEOM	LOWER THAN PRE-ALG /PRE-ALG	MATH A /GEOM	PRE-ALG /GEOM
ITEMS	TEACHER:	T1	T4	T5	T 7	Т8
51 'GENERATING EQUATIONS FROM D	ESCR.	cc	CP	NC	NP	сс
52 'SOLV. EQUA. FROM FACTORED FO		NC	CP	NN	NP	NC
53 SOLVING QUAD EQUAT BY FACTOR		NC	CP	NN	NP	NC
54 'SOLV, QUAD, EQUA, BY QUADRAT		NC	CP	NN	NP	NC
55 GRAPHS OF QUADRATIC RELATION		NC	CP	NN	NP	NC
56 YONE UNKNOWN WITH NUML COEFF		CC	CP	NC	NP	CC
57 'SOLUT, OF QUADRATIC INEQUALITY	TES'	NC	CP	NC	NP	NC
58 'GRAPHING LIN. INEQ. IN ONE UNK!		CC	CP	NC	NP	CC
59 'SIMPLIF. OF A RATIONAL EXPRE.'		NC	CP	NC	NP	cc
60 EVALUATION OF A RATIONAL EXP	RE."	CC	CP	NC	NP	CC
61 'ADD. & SUB. OF RATIONAL EXPRE		CC	CP	NC	NP	CC
62 'MUL, & DIV, OF RATIONAL EXPRE	<u>'</u>	CC	CP	NC	NP	CC
63 PROBABILITY		CC	NN	NN	NN	NN
64 'DESCRIPTIVE STATISTICS'		NC	NN	NN	NN	NN
65 'GRAPH READING'		cc	CP	CC	NC	cc
66 LOCATI, OF POINTS IN CORD, PLAN		cc	CP	CC	NC	CC
67 'DISTANCE BET, TWO POINTS IN CO		NC	CP	NC	NC	CC
68 PERIMETER & AREA OF TRIANGLE		cc	cc	cc	NC	cc
69 CIRCUMFERENCE & AREA OF CIRC		CC	NC	cc	NC	CC
70 VOL. OF CUBES, CYLINDERS, RECT		cc	NC	CC	NC	NC
71 'FINDING SUM OF INTERIOR ANGLE		NN	NC	NN	NC	NC
72 TSOSCELES & EQUILATERAL TRIAN		NN	NC	NN	NC	NC NC
73 'APPLIC., CONGRUENT TRIANGLES		NN	NC	NN	NC	NC
74 'APPLIC., SIMPLE TRIANGLES'		NN	NC	NN	NC	NC
75 PYTHAGOREAN THEOREM & SPEC		NC NC	NC NC	CC NN	NC NC	NC NC
76 PARALLELISM & PERPENDICULAR		NN	NC	NN	NC	NC NC
77 PROOFS (FORMAL DEDUCTIVE DEN 78 TRANSFORMATIONS (TRANSLATIO		NN	NN	NN	NC	NN
79 'VECTORS'	14.	NN	NN	NN	NC	NN
80 SIMPLIF, & EVALU, OF EXPRESS."		CC	CP	NC	NN	CC
81 'SOLUTION OF EQUATIONS'		NC	CP	NC	NN	NC
82 FUNCT, CONCEPT & USE OF NOTAT	TON	CC	CP	NC	NN	NN
83 FUNCT, EVALUATION USING SUBS		CC	CP	NC	NN	NN
84 'COMPOSITION OF FUNCTION'		NN	NN	NC	NN	NN
85 GRAPHING OF FUNCTION		NC	NN	NC	NN	NN
86 NUMERICAL FUNCTIONALEVALUA	TION	NN	NN	NN	NN	NN
87 SUBSTITUTING LITERAL EXPRESS.	1	NN	NN	NN	NN	NN
88 DEFINITION, LAWS & RULES'		NN	NN	NN	NN	NN
89 INVERSE RELATION BET. LOG. & E.	XP'	NN	NN	NN	NN	NN
90 SOLUTION OF LOG. AND EXP. FUNC		NN	NN	NN	NN	NN
91 'GRAPHING OF LOG. AND EXP. FUN		NN	NN	NN	NN	NN
92 'FIND, ALGEBRAIC EXPRESS'		NN	NN	NN	NN	NC
93 'DESCRIB. VARIATIONS OF FUNCTI	ON'	NN	NN	NN	NN	NC
94 'FIND, SIDE LENGTHS IN SPEC:TRIA	·.'	NN	NC	NN	NN	NC
95 GRAPHING TRIGONOMETRIC FUNC	TIONS'	NN	NN	NN	NN	NN
96 REDUCING TRIGONOMETRIC EXPR		NN	NN	NN	NN	NN
97. PROOF OF TRIGONOMETRIC IDEN	THE PARTY OF THE P	NN	NN	NN	NN	NN

TABLE B-2
TEACHER CONTENT COVERAGE BY SAME TEACHER DIFFERENT COURSES 1989

	COURSE:	LOWER THAN PRE-ALG/ MATH A	ALG I/ GEOMETRY	LOWER THAN PRE-ALG /PRE-ALG	LOWER THAN PRE-ALG /PREALG /ALG I
ITEMS	TEACHER:	Т3	T4	T12	T14
1 BASIC OPERATIONS WITH SIGNED IN 2 PRIME FACTORIZATION 3 FINDING DISTANCES ON NUMBER LI 4 USING DEFINITION OF DIVISIBILITY 5 'ADD. & SUB. OF FRACTIONS' 6 'MUL. & DIV. OF FRACTIONS' 7 'ORDER & COMPARISON OF FRACTIOS 9 'ADD. & SUB OF DECIMALS' 10 'MUL. & DIV. OF DECIMALS' 11 'ESTIMATION & APPROXIMATION 12 'CONV. BET. FRACTIONS & DECIMAL 13 'CONV. BET. FRACTIONS & DECIMAL 13 'CONV. BET. FRACTIONS & PERCENT 14 'COMPUT. WITH DECI & FRAC, ROUP 15 'COMPUT. WITH DECI & FRAC, ROUP 15 'COMPUTATION OF PROPORTION 17 'COMPUTATION OF PROPORTION 17 'COMPUTATION OF PROPORTION 19 'APPLIC. LAWS OF EXPONENTS' 20 'POWERS OF 10 & SCIENTIFIC NOTA' 21 'EXPONENT. WITH INTEGRAL EXPON 22 'SQ. ROOT OF PERFECT SQUARES' 23 'SIMPLIFICATION OF SQ. ROOTS' 24 'ADD. & SUB. OF SQ. ROOTS' 25 'MUL. & DIV. OF SQ. ROOTS' 26 'CONV. BET. RADICALS & RAT. EXP 27 'RATIONALIZ. OF NUMERA. & DENO 28 'ADD. AND SUB. OF RADICAL EXPRE 29 'NUM. CALCU. W/ EXPONENTS & RA 30 'ALGE. CALCU. W/ EXPONENTS & RA 31 'FACTORING & SIMPLI. ALGE. EXPRE 32 'ESTIM. & APPROXI. WITH RADICAL 33 'ALGE OPERATION OF LITERAL SYM 34 'SIMPLIF. OF POLYNOMIALS' 36 'EVALUATION OF A POLYNOMIALS' 36 'EVALUATION OF A POLYNOMIALS' 37 'MUL. OF TWO BINOMIALS' 39 'DIVISION OF POLYNOMIALS' 40 'SQUARING A BINOMIALS' 41 'FACTOR. POLYNOMIALS' 41 'FACTOR. TRINOMIAL OVER INTEGE	O.* NE' ONS' LS ' T' ND' S' T.* (EN.* O.* AD. E. S. BOL G. (72) NO. '	CC CC CPP PP PP PP PP PP PP PP PP CC CC	**************************************	**************************************	NCP CCP NCP CCP CCP CCP CCP CCP CCP CCP
43 FACTOR. PERFECT SQ. TRINOMIAL: 44 'SIMPLIF, OF COMPLEX NUMBERS' 45 'ONE UNKNOWN WITH NUM. COEFF. 46 'ONE UNKNOWN WITH LIT. COEFFL' 47 'SIMPLE LIN. EQUA. IN ONE UNKNOWN	r,	NN NN CC NN CC	CP CP CP CP CP	NN NC CC CC CN	NNC NNC NNC NNC
48 TWO UNKNOWN BY ELIMINATION 49 TWO UNKNOWN BY SUBSTITUTION 50 APPLICATION OF EQUATIONS		NN NN CC	CP CP CP	NN NN NC	NNN NNN NNC

TABLE B-2 (continued)

	COURSE:	LOWER THAN PRE-ALG/ MATH A	ALG I/ GEOMETRY	LOWER THAN PRE-ALG /PRE-ALG	IOWER THAN PRE-ALG /PREALG /ALG I
ITEMS	TEACHER:	Т3	T4	T12	T14
51 'GENERATING EQUATIONS FROM DE	escab.	сс	СР	NN	NNN
52 'SOLV, EQUA, FROM FACTORED FOR		NN	CP	NN	NNN
53 'SOLVING QUAD EQUAT BY FACTOR		NN	CP	NN	NNN
54 SOLV. QUAD. EQUA. BY QUADRATI		NN	CP	NN	NNN
55 GRAPHS OF QUADRATIC RELATION		NN	CP	NN	NNC
56 ONE UNKNOWN WITH NUM, COEFF		NN	CP	NN	NNN
57 'SOLUT. OF QUADRATIC INEQUALIT		NN	CP	NC	NNN
58 'GRAPHING LIN. INEO. IN ONE UNKN		NN	CP	NC	NNC
59 'SIMPLIF. OF A RATIONAL EXPRE.'		CC	CP	NC	NNC
60 EVALUATION OF A RATIONAL EXPR	E. '	CC	CP	NC	NNC
61 'ADD. & SUB. OF RATIONAL EXPRE.		NN	CP	NC	NNC
62 'MUL, & DIV. OF RATIONAL EXPRE.'		NN	CP	NC	NNN
63 PROBABILITY		CC	CN	CC	NNN
64 'DESCRIPTIVE STATISTICS'		CC	CN	CC	NNN
65 'GRAPH READING'		NN	CC	CC	NCN
66 LOCATI, OF POINTS IN CORD, PLAN	E.	NN	CC	CC	NCN
67 'DISTANCE BET, TWO POINTS IN CO	R.	NN	CC	CC	NCC
68 PERIMETER & AREA OF TRIANGLES		NN	CC	CC	CCP
69 'CIRCUMFERENCE & AREA OF CIRC	LE'	NN	NC	CC	CCP
70 'VOL, OF CUBES, CYLINDERS, RECT.	AN."	NN	NC	CC	NNN
71 'FINDING SUM OF INTERIOR ANGLE:	3'	CC	CC	NC	NCP
72 TSOSCELES & EQUILATERAL TRIANS	GLE.	CC	CC	NN	NCP
73 'APPLIC., CONGRUENT TRIANGLES'		NN	CC	NN	NCP
74 'APPLIC., SIMPLE TRIANGLES'		NN	NC	NN	NCP
75 'PYTHAGOREAN THEOREM & SPECI	TR.	CC	CC	NC	NCN
76 PARALLELISM & PERPENDICULARI	TY	CC	CC	NN	NCN
77 'PROOFS(FORMAL DEDUCTIVE DEM	ONST.	NN	CC	NN	NNN
78 TRANSFORMATIONS(TRANSLATIO)	N.'	NN	NN	NN	NNN
79 'VECTORS'		NN	NN	NN	NNN
80 'SIMPLIF, & EVALU, OF EXPRESS,'		NN	CP	NN	NNC
81 'SOLUTION OF EQUATIONS'		NN	CP	NN	NNC
82 FUNCT, CONCEPT & USE OF NOTAT		NN	CP	NN	NNN
83 FUNCT, EVALUATION USING SUBST	III.	NN	CP	NN	NNN
84 'COMPOSITION OF FUNCTION'		NN	CP	NN	NNN
85 'GRAPHING OF FUNCTION'		NN	CP	NN	NNN
86 NUMERICAL FUNCTIONALEVALUAT	TION"	NN	NN	NN	NNN
87 'SUBSTITUTING LITERAL EXPRESS.'		NN	NN	NN	NNN
88 DEFINITION, LAWS & RULES		NN	NN	NN	NNN
89 INVERSE RELATION BET. LOG. & EX		NN	NN	NN	NNN
90 'SOLUTION OF LOG. AND EXP. FUNC		NN	NN	NN	NNN
91 'GRAPHING OF LOG, AND EXP. FUNC	т.:	NN	NN	NN	NNN
92 FIND. ALGEBRAIC EXPRESS		NN	NN	NN	NNN
93 DESCRIB. VARIATIONS OF FUNCTIONS		NN	NN	NN	NNN
94 FIND. SIDE LENGTHS IN SPEC.TRIA.		NN	NC	NN	NNN
95 GRAPHING TRIGONOMETRIC FUNC		NN	NN	NN	NNN
96 'REDUCING TRIGONOMETRIC EXPR		NN	NN	NN	NNN
97 PROOF OF TRIGONOMETRIC IDENTI	THE	NN	NN	NN	NNN

TABLE C-1
ALGEBRA READINESS TEST MATH A (TEACHER 1) P-VALUES

ITEMS	1988	1989	'88-'89	CONTENT COVERAGE
1 'ADD, & SUB OF DECIMALS'	.346	.451	105	CP
2. 'MUL, & DIV. OF FRACTIONS'	.404	.549	145	CP
3. 'ADD, & SUB OF DECIMALS'	.596	.569	.027	CP
4. 'EVALUATION OF A POLYNOMIAL(1/2)'	.481	.549	068	CC
5. BASIC OPERATIONS WITH SIGNED NO.	.654	.735	081	CP
6. 'GRAPH READING'	.173	.245	072	CC
7. BASIC OPERATIONS WITH SIGNED NO.	.404	.520	116	CP
BASIC OPERATIONS WITH SIGNED NO.	.654	.686	032	CP
FINDING DISTANCES ON NUMBER LINE	.462	.520	058	CC
10. COMPUTATION OF PERCENT	.365	.431	066	CP
11 MUL, & DIV. OF FRACTIONS	.385	.431	046	CP
12 PRIME FACTORIZATION	.250	.186	.064	CC
13 'ONE UNKNOWN WITH NUM. COEFFI.'	.481	.569	088	CC
14 'ONE UNKNOWN WITH NUM, COEFFL'	.538	.578	040	CC
15 EVALUATION OF A POLYNOMIAL(1/2)	.538	.588	050	CC
16 MUL. & DIV. OF FRACTIONS	.250	.363	113	CP
17 MUL, & DIV. OF DECIMALS'	.519	.490	.029	CP
18.'ADD, & SUB, OF FRACTIONS'	.250	.179	.074	CP
19 MUL. & DIV. OF FRACTIONS	.327	.275	.052	CP
20 PRIME FACTORIZATION	.385	.353	.032	CP
21 BASIC OPERATIONS WITH SIGNED NO.	.173		.026	CP
22 BASIC OPERATIONS WITH SIGNED NO.	.231 .231	.255	063	CC
23 'SQ, ROOT OF PERFECT SQUARES' 24 'EVALUATION OF A POLYNOMIAL(1/2)'	.269	.245	.024	cc
25 'MUL, & DIV. OF DECIMALS'	.346	.431	085	CP
26 CONV. BET. FRACTIONS & PERCENT	.308	.245	.063	CP
27 BASIC OPERATIONS WITH SIGNED NO.	.192	.333	141	CP
28 SIMPLIF OF A RATIONAL EXPRE.	.423	.324	.099	NC
29 'MUL, & DIV, OF FRACTIONS"	.365	.235	.130	CP
30 'APPLIC. OF RATIO OR PROPORTIONS'	.288	.314	026	cc
31 'SIMPLIF, OF COMPLEX FRACTIONS'	.192	.373	181	CP
32. ESTIMATION & APPROXIMATION	.404	.500	096	CP
33 'ALGE OPERATION OF LITERAL SYMBOL'	.135	.127	.008	CC
34 EXPONENT, WITH INTEGRAL EXPONEN."	.231	.118	.113	CC
35 FINDING DISTANCES ON NUMBER LINE	.231	.314	083	cc
36.'LOCATI, OF POINTS IN CORD, PLANE'	.212	.373	161	CC
37. ORDER & COMPARISON OF FRACTIONS	.173	.147	.026	CP
38. PERIMETER & AREA OF TRIANGLES, SQ'	.288	.284	.004	CC
39. PYTHAGOREAN THEOREM & SPECI. TR.	.096	.216	120	NC
40. POWERS OF 10 & SCIENTIFIC NOTAT.	.231	.324	093	CC
41.'ORDER & COMPARISON OF FRACTIONS'	.231	.284	053	CP
42.'ADD. & SUB. OF FRACTIONS'	.058	.098	040	CP
43.'ADD. & SUB. OF FRACTIONS'	.038	.118	080	CP
44.'COMPUTATION OF PERCENT'	.115	.147	032	CP
45.'COMPUT. WITH DECL & FRAC, ROUND.'	.269	.196	.073	CP
46.'CIRCUMFERENCE & AREA OF CIRCLE"	.115	.147	032	CC
47. BASIC OPERATIONS WITH SIGNED NO.	.212	.255	043	CP
48.'SQ. ROOT OF PERFECT SQUARES'	.096	.137	041	CC
49. PERIMETER & AREA OF TRIANGLES, SQ	.115	.167	052	cc
50.'APPLIC., SIMPLE TRIANGLES'	.173	.147	.026	NC

TABLE C-2
ALGEBRA READINESS TEST PRE-ALGEBRA (TEACHER 14) P-VALUES

пемѕ	1988	1989	'88-'89	CONTENT
1 'ADD. & SUB OF DECIMALS'	.455	.600	145	cc
2. 'MUL. & DIV. OF FRACTIONS'	.782	.800	018	CC
3. 'ADD. & SUB OF DECIMALS'	.764	.711	.053	CC
4. 'EVALUATION OF A POLYNOMIAL(1/2)'	.527	.600	073	NC
5. BASIC OPERATIONS WITH SIGNED NO.	.800	.844	044	CC
6. 'GRAPH READING'	.327	.244	.083	NC
BASIC OPERATIONS WITH SIGNED NO.	.436	.644	208	CC
BASIC OPERATIONS WITH SIGNED NO.	.636	.667	031	CC
FINDING DISTANCES ON NUMBER LINE	.600	.689	089	NC
10.'COMPUTATION OF PERCENT	.545	.467	.078	CC
11 MUL. & DIV. OF FRACTIONS'	.709	.622	.087	CC
12 PRIME FACTORIZATION	.455	.489	034	CC
13 'ONE UNKNOWN WITH NUM. COEFFL'	.709	.644	.065	NN
14 'ONE UNKNOWN WITH NUM, COEFFI.'	.600	.733	133	NN
15 EVALUATION OF A POLYNOMIAL(1/2)	.564	.667	103	NC
16 MUL, & DIV. OF FRACTIONS	.345	.356	011	CC
17 MUL. & DIV. OF DECIMALS'	.527	.600	073	CC
18.'ADD. & SUB. OF FRACTIONS'	.364	.400	036	cc
19 MUL, & DIV. OF FRACTIONS'	.400	.333	.067	CC
20 PRIME FACTORIZATION	.600	.644	044	CC
21 BASIC OPERATIONS WITH SIGNED NO.	.364	.289	.075	CC
22 BASIC OPERATIONS WITH SIGNED NO."	.291	.244	.047	CC
23 'SQ. ROOT OF PERFECT SQUARES'	.164	.267	103	NC
24 EVALUATION OF A POLYNOMIAL(1/2)	.291	.200	.091	NC
25 'MUL, & DIV. OF DECIMALS'	.236	.378	142	CC
26 'CONV. BET. FRACTIONS & PERCENT'	.764	.711	.053	CC
27 BASIC OPERATIONS WITH SIGNED NO.	.309	.356	047	CC
28 'SIMPLIF, OF A RATIONAL EXPRE.'	.364	.289	.075	NN
29 MUL. & DIV. OF FRACTIONS*	.273	.244	.029	CC
30 'APPLIC. OF RATIO OR PROPORTIONS'	.309	.444	135	CC
31 'SIMPLIF, OF COMPLEX FRACTIONS'	.236	.333	097	cc
32. ESTIMATION & APPROXIMATION	.364	.467	103	CC
33 'ALGE OPERATION OF LITERAL SYMBOL'	.073	.044	.029	CC
34 EXPONENT, WITH INTEGRAL EXPONEN.	.145	.244	099	NC
35 FINDING DISTANCES ON NUMBER LINE	.273	.378	105	NC
36. LOCATI, OF POINTS IN CORD, PLANE	.182	.333	151	NC
37. ORDER & COMPARISON OF FRACTIONS	.164	.200	036	CC
38. PERIMETER & AREA OF TRIANGLES, SQ	.218	.200	.018	CC
39. PYTHAGOREAN THEOREM & SPECI. TR.	.200	.133	.140	cc
40. POWERS OF 10 & SCIENTIFIC NOTAT.	.273	.133	093	CC
41. ORDER & COMPARISON OF FRACTIONS	.145	.044	.101	cc
42.'ADD. & SUB. OF FRACTIONS'	.055	.133	078	CC
43.'ADD. & SUB. OF FRACTIONS'	.036	.067	031	cc
44. COMPUTATION OF PERCENT	.073	.044	.029	cc
45. COMPUT. WITH DECI & FRAC, ROUND.	.182	.178	.004	cc
46.'CIRCUMFERENCE & AREA OF CIRCLE'	.073	.067	.006	cc
47. BASIC OPERATIONS WITH SIGNED NO.	.055	.111	056	CC
48.'SQ, ROOT OF PERFECT SQUARES'	.073	.044	.029	NC
49. PERIMETER & AREA OF TRIANGLES, SQ	.055	.044	.011	CC
50. APPLIC., SIMPLE TRIANGLES'	.073	.044	.029	CC
50.'APPLIC., SIMPLE TRIANGLES'	.073	.044	.029	œ

TABLE C-3
ALGEBRA READINESS TEST LOWER THAN PRE-ALGEBRA (TEACHER 17) P-VALUES

ITEMS	1988	1989	'88-'89	CONTENT
1 'ADD. & SUB OF DECIMALS'	.400	.368	.032	CP
2. 'MUL, & DIV. OF FRACTIONS'	.600	588	.012	CP
3. 'ADD. & SUB OF DECIMALS'	.360	.485	125	CP
4. 'EVALUATION OF A POLYNOMIAL(1/2)'	.320	.375	055	NN
5. BASIC OPERATIONS WITH SIGNED NO.	.600	.684	084	CC
6. 'GRAPH READING'	.160	.184	024	CC
7. 'BASIC OPERATIONS WITH SIGNED NO.'	.320	.588	.172	CC
8. BASIC OPERATIONS WITH SIGNED NO.	.760	.667	031	CC
9. 'FINDING DISTANCES ON NUMBER LINE'	.400	.493	093	CC
10. COMPUTATION OF PERCENT	.760	.449	.311	CP
11 'MUL. & DIV. OF FRACTIONS'	.560	.390	.170	CP
12 'PRIME FACTORIZATION'	.520	.316	.204	CC
13 'ONE UNKNOWN WITH NUM. COEFFL'	.480	.529	049	NN
14 'ONE UNKNOWN WITH NUM, COEFFL'	.640	.537	.103	NN
15 'EVALUATION OF A POLYNOMIAL(1/2)'	.400	.500	100	NN
16 'MUL, & DIV, OF FRACTIONS'	.200	.279	079	CP
17 'MUL, & DIV. OF DECIMALS'	.320	.485	165	CP
18.'ADD. & SUB. OF FRACTIONS'	.240	.309	069	CP
19 'MUL, & DIV. OF FRACTIONS'	.400	.360	.040	CP
20 PRIME FACTORIZATION	.560	.485	.075	CC
21 BASIC OPERATIONS WITH SIGNED NO."	.320	.250	.070	CC
22 'BASIC OPERATIONS WITH SIGNED NO.'	.200	.228	.028	CC
23 'SQ. ROOT OF PERFECT SQUARES'	.080	.279	199	NC
24 'EVALUATION OF A POLYNOMIAL(1/2)'	.280	.272	.008	NN
25 'MUL, & DIV, OF DECIMALS'	.360	.404	044	CP
26 'CONV. BET. FRACTIONS & PERCENT'	.480	.441	.039	CP
27 'BASIC OPERATIONS WITH SIGNED NO."	.240	.287	047	CC
28 'SIMPLIF, OF A RATIONAL EXPRE.'	.280	.382	102	NN
29 'MUL, & DIV. OF FRACTIONS"	.200	.346	146	CP
30 'APPLIC. OF RATIO OR PROPORTIONS'	.360	.287	.073	PP
31 'SIMPLIF, OF COMPLEX FRACTIONS'	.240	.316	076	CP
32. ESTIMATION & APPROXIMATION	.280	.419	139	CC
33 'ALGE OPERATION OF LITERAL SYMBOL'	.120	.074	.046	NN
34 'EXPONENT, WITH INTEGRAL EXPONEN.'	.200	.478	278	CP
35 'FINDING DISTANCES ON NUMBER LINE'	.320	.221	.099	CC
36.'LOCATL OF POINTS IN CORD. PLANE"	.320	.316	.004	CC
37.'ORDER & COMPARISON OF FRACTIONS'	.320	.169	.151	CP
38. PERIMETER & AREA OF TRIANGLES, SQ'	.240	.338	098	CC
39. PYTHAGOREAN THEOREM & SPECT. TR."	.160	.206	046	NC
40. POWERS OF 10 & SCIENTIFIC NOTAT.	.280	.368	088	CP
41. ORDER & COMPARISON OF FRACTIONS'	.080	.287	207	CP
42, ADD. & SUB. OF FRACTIONS'	.040	.162	122	CP
43, ADD. & SUB. OF FRACTIONS	.000	.096	096	CP
44: COMPUTATION OF PERCENT	.080	.118	038	CP
45.'COMPUT, WITH DECI & FRAC, ROUND.' *	.120	.206	086	CC
46. CIRCUMFERENCE & AREA OF CIRCLE	.080	.103	023	CC
47. BASIC OPERATIONS WITH SIGNED NO.	.080	.272	192	CC
48.'SQ. ROOT OF PERFECT SQUARES'	.080	.125	045	NC
49. PERIMETER & AREA OF TRIANGLES, SQ'	.000	.169	169	CC
50. APPLIC, SIMPLE TRIANGLES	.080	.213	133	CC

TABLE C-4
ELEMENTARY ALGEBRA TEST ALGEBRA I (TEACHER 4) P-VALUES

ITEMS	1988	1989	'88-'89	CONTENT COVERAGE
1 'SIMPLIF, OF POLYNO, BY GROUPING'	.963	1.000	037	cc
2. 'CONV. BET. FRACTIONS & DECIMALS'	.963	.950	.013	CC
3. 'ESTIM, & APPROXI, WITH RADICALS.'	.407	.500	193	CC
4. 'EXPONENT, WITH INTEGRAL EXPONEN.'	.741	.700	.041	CC
5. 'ADD. & SUB OF DECIMALS'	.827	.700	.127	CP
6. 'SQUARING A BINOMIAL'	.914	.800	.114	CC
7. TSOSCELES & EQUILATERAL TRIANGLE	.420	.300	.120	NC
8. EXPONENT. WITH INTEGRAL EXPONEN."	.531	.550	019	CC
9. 'LOCATL OF POINTS IN CORD. PLANE'	.563	.900	.063	cc
10.'SIMPLIF, OF A RATIONAL EXPRE.'	.642	.550	.092	CC
11 'SOLV. EQUA. FROM FACTORED FORM'	.679	.500	.179	CC
12 MUL, OF MONOMIAL WITH A POLYNO.	.864	.700	.164	CC
13 'FACTOR, TRINOMIAL OVER INTEGERS'	.815	.750	.065	cc
14 'ONE UNKNOWN WITH NUM. COEFFL.'	.901	.700	.201	cc
15 'EVALUATION OF A POLYNOMIAL(1/2)'	.963	1.000	037	CC
16 TWO UNKNOWN BY ELIMINATION	.654	.800	146	cc
17 'SQ. ROOT OF PERFECT SQUARES'	.852	.600	.252	CC
18. PYTHAGOREAN THEOREM & SPECT. TR."	.580	.700	120	NC
19 'MUL, & DIV, OF FRACTIONS'	.679	.600	.079	CC
20 'GRAPHING LIN. INEQ. IN ONE UNKNOWN'	.963	.900	.063	cc
21 'COMPUTATION OF PERCENT'	.457	.600	143	CC
22 'ADD. & SUB, OF SQ.ROOTS'	.864	.800	.064	CC
23 'FACTOR, PERFECT SQ. TRINOMIALS'	.901	.800	.101	cc
24 'MUL, & DIV. OF SQ. ROOTS'	.778	.700	.078	cc
25 'APPLICATION OF EQUATIONS'	.864	.950	086	cc
26 'ONE UNKNOWN WITH NUM. COEFFL."	.728	.750	022	cc
27 'EVALUATION OF RATIONAL EXPRE.'	.926	1.000	074	cc
28 'SIMPLIF, OF SQUARE ROOTS'	.901	.900	.001	cc
29 'ADD. & SUB. OF POLYNOMIALS'	.741	.700	.041	cc
30 SIMPLIF, OF RATIONAL EXPRE.	.753	.750	.003	cc
31 PERIMETER & AREA OF TRIANGLES, SQ	.728	.750	022	cc
32. PERIMETER & AREA OF TRIANGLES, SQ	.309	.400	091	cc
33 SIMPLIF. OF A RATIONAL EXPRE.	.753	.700	.053	cc
34 'ONE UNKNOWN WITH NUM, COEFFL'	.704	.550	154	cc
35 MUL. & DIV. OF RATIONAL EXPRE.	.728	.550	.078	cc
36. ONE UNKNOWN WITH NUM. COEFFL.	.654	.600	.054	cc
37.TWO UNKNOWN BY SUBSTITUTION	.827	.800	.027	cc
38. POWERS OF 10 & SCIENTIFIC NOTAT.	.765	.600	.165	cc
39. SOLVING QUAD. EQUAT. BY FACTORING	.617	.600	.017	cc
40.'ADD. & SUB. OF RATIONAL EXPRE.'	.667	.450	.217	cc
41. VOL. OF CUBES, CYLINDERS, RECTAN.	.469	.450	.019	NN
42. APPLIC., SIMPLE TRIANGLES'	.531	.500	.031	NN
43.FINDING DISTANCES ON NUMBER LINE	.272	.450	178	cc
44. ONE UNKNOWN WITH LIT. COEFFL.	.741	.550	.191	cc
45. COMPUTATION OF PROPORTIONS	.481			NN
46. CIRCUMFERENCE & AREA OF CIRCLE	.198	.150	.048	
47. SOLVING QUAD. EQUAT. BY FACTORING	.519 .741	.350 .500	.169	cc
48. ONE UNKNOWN WITH NUM. COEFFI. 49. ONE UNKNOWN WITH NUM. COEFFI.	.481	.450	.241	œ
	.506	.350	.156	œ
50:SOLV. QUAD. EQUA. BY QUADRATIC	.300	.330	.136	

TABLE C-5
ELEMENTARY ALGEBRA TEST ALGEBRA I (TEACHER 14) P-VALUES

TTEMS	1988	1989	'89-'90	COVERAGE
1 'SIMPLIF, OF POLYNO, BY GROUPING'	.542	.615	-,073	cc
2. 'CONV. BET. FRACTIONS & DECIMALS'	.854	.692	.162	PP
3. 'ESTIM. & APPROXI. WITH RADICALS.'	.042	.038	.004	NN
4. EXPONENT, WITH INTEGRAL EXPONEN.	.312	.538	226	CC
5. 'ADD. & SUB OF DECIMALS'	.312	.500	188	PP
6. 'SQUARING A BINOMIAL'	.396	.654	258	CC
7. TSOSCELES & EQUILATERAL TRIANGLE	.187	.231	044	PP
8. 'EXPONENT. WITH INTEGRAL EXPONEN.'	.104	.000	.104	CC
9. 'LOCATI, OF POINTS IN CORD, PLANE'	.604	.615	011	CN
10, SIMPLIF, OF A RATIONAL EXPRE.	.437	.615	178	CC
11 'SOLV. EQUA. FROM FACTORED FORM'	.229	.577	348	NN
2 MUL, OF MONOMIAL WITH A POLYNO.	.625	.577	.048	CC
3 FACTOR, TRINOMIAL OVER INTEGERS	.437	.385	.052	CC
14 'ONE UNKNOWN WITH NUM, COEFFL'	.437	.462	025	CC
15 EVALUATION OF A POLYNOMIAL(1/2)	.687	.615	.072	PP
6 TWO UNKNOWN BY ELIMINATION	.083	.115	032	CN
17 'SQ. ROOT OF PERFECT SQUARES'	.271	.231	.040	NN
8. PYTHAGOREAN THEOREM & SPECI. TR.	.562	.577	015	NN
19 'MUL, & DIV, OF FRACTIONS'	.229	.385	156	PP
20 GRAPHING LIN. INEQ. IN ONE UNKNOWN	.417	.462	045	CN
21 'COMPUTATION OF PERCENT'	.146	.154	008	CP
22 'ADD. & SUB. OF SQ.ROOTS'	.062	.077	015	NN
23 'FACTOR, PERFECT SQ. TRINOMIALS'	.417	.846	429	CC
24 'MUL, & DIV. OF SQ. ROOTS'	.167	.385	218	NN
25 'APPLICATION OF EQUATIONS'	.417	.269	.148	CC
26 ONE UNKNOWN WITH NUM. COEFFL!	.146	.115	.031	CC
27 EVALUATION OF RATIONAL EXPRE.	.396	.538	142	CC
28 'SIMPLIF. OF SQUARE ROOTS'	.062	.154	092	NN
29 'ADD, & SUB, OF POLYNOMIALS'	.167	.269	102	CC
30 'SIMPLIF, OF RATIONAL EXPRE.'	.354	.538	184	CC
31 PERIMETER & AREA OF TRIANGLES, SQ	.125	.346	221	CP
32. PERIMETER & AREA OF TRIANGLES, SQ	.229	.462	233	CP
33 'SIMPLIF, OF A RATIONAL EXPRE.'	.250	.346	096	CC
34 YONE UNKNOWN WITH NUM, COEFFL!	.104	.077	.027	CC
35 'MUL, & DIV. OF RATIONAL EXPRE.'	.271	.462	191	CC
36. ONE UNKNOWN WITH NUM. COEFFL'	.162	.077	015	CC
37.TWO UNKNOWN BY SUBSTITUTION	.104	.115	011	CN
38. POWERS OF 10 & SCIENTIFIC NOTAT.	.125	.346	221	CC
39.'SOLVING QUAD. EQUAT. BY FACTORING'	.104	.192	088	NN
40. ADD. & SUB. OF RATIONAL EXPRE.	.042	.269	227	CC
41. VOL. OF CUBES, CYLINDERS, RECTAN.	.146	.308	162	NN
42. APPLIC., SIMPLE TRIANGLES	.229	.462	233	PP
43. FINDING DISTANCES ON NUMBER LINE	.042	.077	035	CP
44. ONE UNKNOWN WITH LIT. COEFFL.	.062	.115	053	CC
45. COMPUTATION OF PROPORTIONS	.021	.038	017	CP
46. CIRCUMFERENCE & AREA OF CIRCLE	.021	.038	017	PP
47: SOLVING QUAD. EQUAT. BY FACTORING	.104	.346	242	NN
48, ONE UNKNOWN WITH NUM, COEFFI.	.021	.308	287	CC
49, ONE UNKNOWN WITH NUM. COEFFL	.062	.385	323	CC
50, SOLV, QUAD, EQUA, BY QUADRATIC	.021	.154	133	NN