PATTERNS IN TEACHER REPORTS OF TOPIC COVERAGE AND THEIR EFFECTS ON MATH ACHIEVEMENT: COMPARISONS ACROSS YEARS

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Introduction¹

The conceptual and technical design of large-scale assessments which can better capture educational effects has received considerable attention in recent years (e.g., Baker & Herman, 1986; Burstein, 1989; Burstein et al., 1986; Cole, 1988; Linn, 1987, 1989; Muthen, 1989; Muthen, et al., 1988). The basic rationale for incorporating information about instructional experiences in the design and analysis of assessment data is that student ability, topic exposure, and forms of instructional exposure each contribute to student performance as measured at a given point in time.

As we have discussed in earlier reports, collecting information about content coverage as part of large-scale assessments can be valued on several grounds. First, many studies (e.g., Berliner, 1980; Burstein et al. (in press); Leinhardt & Seewald, 1981; Leinhardt, 1983; Schmidt, 1983) show that various forms of measuring content coverage are invaluable in accounting for student performance. Second, measures of instructional coverage have served as a means of evaluating the match between the content of tests and the subject matter experiences that students have had (e.g., Leinhardt & Seewald, 1981). Such measures also are useful in examining the sensitivity of test items to differences in instructional experiences of individual students and groups of students.

The purpose of this study is to investigate the degree of consistency of teachers' content coverage reports with logical expectations about the contents of a course with a given title and student composition for two consecutive years and to detect the effects of content coverage by comparing student performance patterns associated with teachers' reports of content coverage for 1988 and 1989 data collected in the context of an ongoing examination of instructional assessment in secondary school mathematics. The results of the data analysis for 1988 was reported earlier (Burstein, Chen & Kim, 1988). This study followed the same procedures using 1989 data, and compared the results across two years. We consider the validity of certain means of gathering information about students' instructional experiences and view student test performance as corroborating evidence. Evidence that reported content coverage patterns are similar across years may suggest that the chosen means of collecting such data has functioned as expected under the "steady state" curricular conditions prevalent in participating schools. Any deviations in reporting patterns across years should be dictated either by (a) the performance of a teachers' students the previous year or (b) differences in class composition across years.

Data

The data were collected from teachers who volunteered to participate in the Mathematics Diagnostic Testing Program (MDTP). Under this project, the University of California and California State University systems have developed a series of four diagnostic tests (Algebra Readiness, Elementary Algebra, Intermediate Algebra, and Precalculus) to be used voluntarily in secondary and middle schools in California in an effort to improve mathematics education. In this study, analyses are based on teacher and student data from approximately 300 sections (176 sections 3 districts, 8 schools in 1988 and 112 sections 3 districts, 10 schools in 1989) of mathematics, spanning courses in Pre Algebra, Math A, Math B, Algebra I, and Geometry. To compare p-values across 1988 and 1989, the Algebra Readiness and Elementary Algebra (1987 form of Elementary Algebra for 1989 data) tests developed by MDTP were used.

¹ Karen Gold, Robert Linn, and Joan Herman provided useful suggestions regarding this study; however, the problems that remain are solely the responsibility of the authors.

Instrumentation

In our instrumentation, teachers are presented with different math topics and are asked to indicate how these topics are covered in each mathematics course they teach, using the following set of response options:

A. "New": Taught as new content

B. "Extended": Reviewed and Extended

C. "Review": Reviewed only

D. "Assumed": Assumed as prerequisite knowledge & neither taught nor reviewed.

E. "Taught Later": Taught later in the school curriculum

F. "Not in Curriculum": Not in the school curriculum

G. "Don't Know": Not taught now and don't know if in school curriculum.

These seven response alternatives are adapted from Opportunity to Learn questions and topic specific teacher questionnaires used in the Second International Mathematics Study.2

The questionnaire included topics which were identified as included in any of the four tests developed by MDTP or in the secondary school mathematics grid developed as part of an earlier study of the content validity of MDTP tests (Burstein, Aschbacher, Chen, Lin, & Qi, 1986). Thus the questionnaire was expected to span to the course material for college-preparatory secondary school mathematics, necessitating an extensive list of topics (97 topics classified into 12 distinct subgroups): integers (4 topics); fractions, decimal, ratio, proportion, and percent (14); exponents, radicals, and square roots(14); polynomials (12); algebraic equations (11); inequalities (3); rational expressions (4); probability and statistics (2); geometry (15); absolute value (2); functions (10); and trigonometry (6).

Methods for Analyzing Patterns of Topic Coverage

There is no clear operational standard for examining the degree of consistency between teachers' content coverage and the effects of content coverage. In this study, as in Burstein, Chen, & Kim (1989), patterns of responses were examined that should align with logical expectations about the contents of a course with a given title and student composition across two years. And also p-values matched with teachers' responses on content coverage were computed.

The first sets of analyses with the teacher data involved the percentage of teacher responses regarding their topic coverage. We examine the responses within and between courses in the 12 broader topic categories. These patterns should be consistent with logical expectation for the topic within a given course, and when a topic clearly aligns with a given course, virtually all teachers claiming to teach that course should be stating that the topic is taught as New(A) or perhaps Extended (B). Percentage of responses (topic by type of coverage) were tabulated for course sections assigned to six categories (Lower than Pre-Algebra, Math A, Math B, Pre-Algebra, Algebra I, Geometry) for 1988 and 1989 in Table 1 (Attachment 1). Note that in addition to percentage tabulations of actual responses, certain combinations of responses (e.g., Taught [A+B+C], Taught + Extended [A+B], Extended + Review [B+C], Review + Assumed [C+D], Not Taught and Not Assumed [E+F+G+Missing] were also tabulated. As shown in Table 1, these percentage data describe the

² This data is a national sample of United States eigth-grade students mathematics achievement tests conducted by IEA (the International Association for the Evaluation of Educational achievement) in 1981-1982.

characteristics of both the apparent topical emphases in given courses and whether these emphases are different across sections of the course.

The second sets of analyses report on an attempt to identify which topics are "Core" for a given course. We proceeded with a strategy to identify from the 1988 and 1989 empirical data those topics that were taught almost uniformly within a course type. If 80% of teachers classified a topic as Taught as New (response A) or Extended (B) this topic was assumed to be a Core topic. Similarly topics were classified as Prior (C+D), and Not taught (E+F+G) if 80% of teachers' responses were in the indicated category. Topics not falling in any of these categories were also identified. For example, if more than 80% of teachers in Lower than Pre-Algebra classes responded that they taught a topic as New and Extended (A+B), then it was marked as "C" (Core). The results are reported in Table 2 (Attachment 2).

The third set of analyses relates the teacher topic coverage response data and its relationship to student performance. The descriptive results of what teachers claimed to teach at various levels are interesting in and of themselves, but the validity of such data might be questioned. Therefore, we decided to ascertain whether the specific response choices corresponded in a systematic way with performance on MDTP and SIMS Benchmark³ test items measuring a given subtopic. The three tests administered to students in the course types were considered here. Those are the MDTP Algebra Readiness and Elementary Algebra tests and the six short forms of the A level of the SIMS Benchmark tests. Depending on the course in which students are enrolled, they will have taken either the MDTP Algebra Readiness (Lower than Pre Algebra, Math A, Math B, Pre Algebra) or Elementary Algebra (Algebra I and Geometry) tests and one of the six randomly assigned forms of the SIMS Benchmark test. Performance on test items in a given topic area should be consistent with teachers' report of coverage of these topics. Table 3 (Attachment 3) shows the results of these analyses.

Results

Across courses and topics in general, the patterns of response are consistent with what might be the expected curriculum patterns in mathematics courses at this level across 1988 and 1989. In Lower than Pre Algebra, nothing was assumed to have been taught before and the vast majority of the topics were judged to be taught later or not in the curriculum in both 1988 and 1989. Only operations with common and decimal fractions and ratio, proportion, and percent problems were taught as Core by more than 80% of teachers in both years.

In Math A and Math B, almost nothing was assumed to have been taught before, but the subtopics taught in Lower than Pre-Algebra were reviewed. And more than 80% of these teachers taught as Core the topics taught as Core in Lower than Pre-Algebra, plus the subtopics such as exponents, powers, perfect squares, addition and subtraction of square roots in 1988. More than 80% of teachers taught those topics as Prior and Core in 1989. Teachers were more likely to teach higher level subtopics, such as linear equations, Pythagorean theorem as Core in 1989 compared to 1988. Teachers' responses on these topics must probably differ because these courses are newly created courses in California and are under development.

In Pre-Algebra almost all teachers taught or extended the topics within the subcategories integers, fractions/ratio/proportion/percent, and exponents, but otherwise there was much diversity in both years. Some teachers apparently treated

³ SIMS Benchmark tests contained 46 items selected from the SIMS pool administered at grade 8. These items were assigned to one of the six forms with two items common across all forms and the remainder allocated to forms to achieve a rough balance in content and difficulty using SIMS performance levels as a guide regarding the latter

Pre-Algebra as beginning Algebra with light introductions to Algebra topics, while others considered it the final opportunity to make sure all arithmetic topics were well understood.

Topic coverage in Algebra I concentrated on the traditional core of introductory algebra (exponents, polynomials, algebraic equations, inequalities, rational expressions, absolute value). More than 80% of teachers responded that these topics were taught as Core in both years. Topics that differentiated among subsets of Algebra I sections reflect time devoted to extending and reviewing common and decimal fractions versus those involving enriched preparation for future courses (e.g., geometry topics, function concepts).

In Geometry, there was essentially a universal core of topics. Any differentiation associated with whether higher level arithmetic topics were reviewed or assumed, whether the Algebra core was reviewed, or whether special geometry/trigonometry topics (e.g., transformations, vectors) were introduced. More than 80% of teachers taught all subtopics in Geometry as Core, although transformations and vectors were taught as Core only by 36% (1988) and 45% (1989) of the teachers. These results showed that the prevalence and type of coverage of topics were consistent with their typical position within the curriculum across both years.

The pattern of performance on items from the MDTP tests, classified according to topic and specific teachers' reports of content coverage, agreed somewhat with expectations, but generally were uneven. Item p-values were highest when a topic was claimed to be taught as Reviewed Only in three tests across both years. P-values were lowest when topics were indicated as Not in Curriculum and Don't Know in MDTP Algebra Readiness both years. P-values, the Assumed as Prerequisite for Algebra readiness in 1988, were quite low, although in 1989 the performance was high. These apparent differences are exceptional; very few teachers (typically no more than 1 or 2) chose Assumed as Prerequisite for any one item on these tests, so the p-values were not very stable for this response alternative on this test. For the SIMS Benchmark items, the simple rank ordering of average p-values appears confusing because of high p-values for Taught Later, Not in Curriculum, and Don't Know for both years. But only one teacher chose Don't Know responses for 13 of the 16 items. Not in Curriculum responses for 10 of the 12 items in 1988. Two teachers chose Not in Curriculum responses for 23 out of the 27 items in 1989 that fell in this response category. Because of the limited number of respondents, inference from these data are hazardous. Otherwise, the patterns of performance were associated with response alternatives as expected. Further, even though the patterns of performance in the SIMS Benchmark did not show clear patterns of performance associated with responses, when there was sufficient data to warrant some confidence in performance data, the patterns of performance associated with given response options were roughly as expected.

Implications

Our results showed that a questionnaire approach to soliciting data on types of topic coverage seems to give plausible information about content emphases in instruction. The merits of using teachers' reports of content coverage lie in their feasibility and efficiency. Completion of our instrument required 30 minutes or less. However, some patterns in the results were aberrant, raising questions about the sensitivity of the measure in its current form and about how much confidence can be placed in seemingly simple assessments of the type considered here.

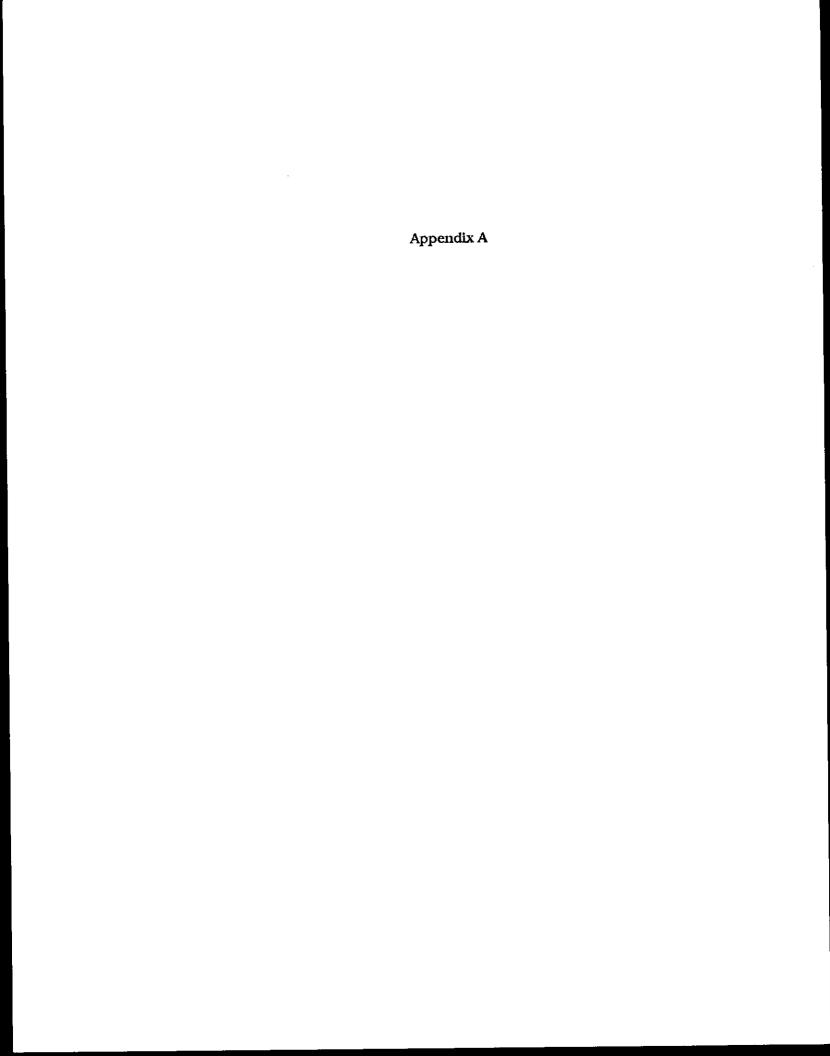
Further research is needed to refine the approach and its validation methodology. Of particular interest are questions of what constitutes a reasonably sound relationship between teacher reports and student performance. Whether expected

relationships are similar across different types of classes is another issue for exploration.

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MDTP 88/89 - TEACHER QUESTIONNAIRE - TOPIC COVERAGE TOPIC BY TOPIC (12 CATEGORIES), PERCENTAGE

+ + + + 0	<u>Σ</u>	279 .142	003	.754	.986	.884 .927	1.00	.924 .975	.567	.724	.930	1.00	1.00	.722 .704
+	C+D	. 070	.088 .286	.021	0.00	0.00	00.0	0.00	0.00	.037	00.00	0.00	0.00	.025
	A+B	.651	.849 .712	.231	.014	.073		.025	.198 .433	.239	0.00	0.00	0.00	.253 .249
	B+C	.413	.520 .524	.096	.033	0.00	0.00	0.00	0.00	. 102	070	0.00	0.00	. 122
4+8	Ŷ	.858	.937	.246 .274	.109 .014	.116	0.00	.076	.198	.276 .344	.070	0.00	0.00	.278 .296
MISS	Σ	.025	.003	.005	0.00	0.00	.209	.209	.209	.209	.209	.209	.209	.005
KNOW	ပ	00.0	0.00	.025	0.00	0.00	0.00	0.00	.058	00.00	00.0	0.00	0.00	.001
NOT	1 AND 1 A	900.	0.00	.252	.256	.342	.367	.233	.163	.300	.350	.367	.465 .533	.206
TAUG HT L	A LEK	.050	00.0	.475 .469	.519	. 585	.535 .633	.483	.372	.356	419 467	.633	.326	.366
ASSU	۵	.012	0.00	0.00	0.0	0.00	0.00	0.00	0.00	0.00	99.	0.00	0.00	0000
REV I EWED	ပ	.058	.088	.015	0.00	0.00	0.00	0.00	0.00	.037	.070	0.00	0.00	.024
EXTE NDED	80	.355	.238	.081	.033	0.00	0.00	0.00	0.00	.028	0.00	0.00	0.00	.062
NEW	∢	.297	474	.238	.076 .014	.116	00000	.076 .008	.198	.211 .242	0.00	0.00	0.00	. 156
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TOPIC		1. INTEGERS	2. FRACTIONS	EXPONENTS	POLYNOMIALS	5. ALGEBRAIC EQU.	6. INEQUALITIES	7. RATIONAL EXPO.	PROB. & STATS.	9. GEOMETRY	10. ABSOLUTE	11. FUNCTIONS	12. TRIGONOMETRY	
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MDTP 88/89 - TEACHER QUESTIONNAIRE - TOPIC COVERAGE TOPIC BY TOPIC (12 CATEGORIES), PERCENTAGE

ய ம ர ர	Σ +	0.00	.086	.686 .452	.733 .444	.576	.733	.700	.700	.880	.900	.867	1.00	.672 .419
	0+0	.100	.233	.071	0.00	0.00	00.00	0.00	0.00	0.00	0.00	0.00	0.00	.131
	A+B	.900	.681	.243	.5567	. 164 . 424	.267 .667	.833	300	.120	.667	.100	0.00	.450
	8+C	.200	.333	.057	0.00	0.00	0.00	0.00	0.00	.133	0.00	0.00	0.00	.165
4	t +	1.00	.914	.243 .548	267 556	164 424	.667	.833	300	. 578	.100	.133	0.00	.318 .574
MISS	Σ	0.00	0.00	.229	.056 .056	0.00	00.00	00.00	0.00	.400	0.00	0.00	0.00	.007
KNOW	U	0.00	0.00	00.00	0.00	0.00	0.00	0.00	0.00	.013	0.00	0.00	0.00	00.00
NOT	Z Z F	0.00	.014	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	.220
TAUG HT L	A EK	0.00	0.00	.190	.056	.436 .364	.333	.300	300	. 467 . 178	.500	.533	.600	.353
ASSU MED	٥	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	.010
REVI EWED	ပ	00.0	.233 .857	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	.038 .124
EXTE NOED	æ	.100	.100	.057	0.00	0.00	0.00	0.00	0.00	.040	0.00	0.00	0.00	.033
NEW	∢	.833	.581	.186 .548	.556	.303	.667 .667	.300	1.00	.080	.100	.100	0.00	.247 .409
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MDTP88/89- TEACHER QUESTIONNAIRE - TOPIC COVERAGE TOPIC BY TOPIC (12 CATEGORIES), PERCENTAGE

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Q+3		.250	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	. 199
A+B) :	.850 .750	.071	.414 .452	.333	. 145 . 394	.200	.150	.800	.533	0.00	0.00	0.00	.371
g C+)	1.00	.929	0.00	0.00	0.00	0.00	0.00	0.00	.333	0.00	0.00	0.00	.296
4 + B	ပို	1.00	1.771	414. 476.	.333	. 145 . 455	.333	.150	.800	.533	00.00	0.00	0.00	. 515
MISS	Σ	0.00	.229	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	.003
NOT KNOW	ပ	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
NOT IN C	Г.	0.00	0.00	.400 .262	.800	.800	.800	.800	0.00	.244	.333	.333	.333	.220
TAUG HT L	Г Г П	0.00	0.00	.014	0.00	.055	0.00	.050	.200	.222	.200	.200 .467	.611	.206
ASSU	٥	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
REVI EWED	ပ	.150	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	.006 .144
EXTE NOED	80	.850	0.00	0.00	0.00	0.00	0.00	500	0.00	.160	500	0.00	0.00	.171
NEW	⋖	0.00	0.00	.414 .452	.183	. 145 . 182	.200	.150	.800	0.00	0.00	0.00	0.00	.220
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TOPIC		I, INTEGERS	2. FRACTIONS	EXPONENTS	4. POLYNOMIALS	5. ALGEBRAIC EQU. 1	6. INEQUALITIES	7. RATIONAL EXPO.'8	PROB. & STATS. 188	9. GEOMETRY	10. ABSOLUTE	11. FUNCTIONS	12. TRIGONOMETRY	
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COURSE		MATH B												COURSE MEAN

MOTP88/89- TEACHER QUESTIONNAIRE - TOPIC COVERAGE TOPIC BY TOPIC (12 CATEGORIES), PERCENTAGE

+ + 5	∑ +	.019	.002	. 549	.778 .756	.741	,684 ,564	.500	.564 .846	.434 .462	.538	.974 1.00	.962	.530
	0+0	.231	.374	.013	0.00	0.00	0.00	0.00	0.00	.010	0.00	0.00	0.00	.090
	A+B	.846 .769	.625	.544 .357	.222	371	.316 .410	.500 .462	.436 .154	.528	.603	026	.038	.387 .374
	B+C	.513	.810 .495	. 104	.004	.023	0.00	0.00	.359	.313	0.00	0.00	0.00	.208
97.9	φ + +	.981	.995	.557	. 199	.259 .420	.316 .436	.500	.436 .154	.538	.603	0.00	.038	.489 .439
M1SS ING	Σ	0.00	0.00	0.00	.017	.009 .154	0.00	0.00	0.00	0.00	0.00	0.00	0.00	.003
NOT	၁	0.00	0.00	0.00	0.00	.014	0.00	0.00	.154	.014	0.00	00.00	0.00	.001
NOT IN C	באאט ה	00.00	0.00	.209	.130	.203	.205	. 141 . 154	.308	.126	.077 .154	.313	.295	.131
TAUG HT L	ATER E	.013	.002	.332	.630	.594 .210	.590	.340	.231	.294 .154	.231	.615 .462	.603	.230
ASSU MED	٥	0.00	.004 .060	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	.001
REV! EWED	ပ	.135	.247	.013	0.00	0.00	0.00	0.00	0.00	.010	0.00	000	0.00	.082
EXTE NDED	æ	.096	.247	.064	,004 ,006	.023	0.00	0.00	.359	.173 .067	0.00	0.00	0.0	.059
NEW	∢	.673	. 185	.480	.218	.357	.316 .410	.500	.038	.253	.603	.026	.103	.315
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T0P I C		1. INTEGERS	2. FRACTIONS	3. EXPONENTS	4. POLYNOMIALS	5. ALGEBRAIC EQU'88	6. INEQUALITIES	7. RATIONAL EXPO	8. PROB. & STATS	9. GEOMETRY	10. ABSOLUTE	11. FUNCTIONS	12. TRIGONOMETRY	
10	-		2. FR	3. EX	4. PC	5. AL	6.	7. R/	8.	9.0	10.	1.	12.	
COURSE		PRE-ALGEBRA												COURSE MEAN

MDTP88/89 - TEACHER QUESTIONNAIRE - TOPIC COVERAGE TOPIC BY TOPIC (12 CATEGORIES), PERCENTAGE

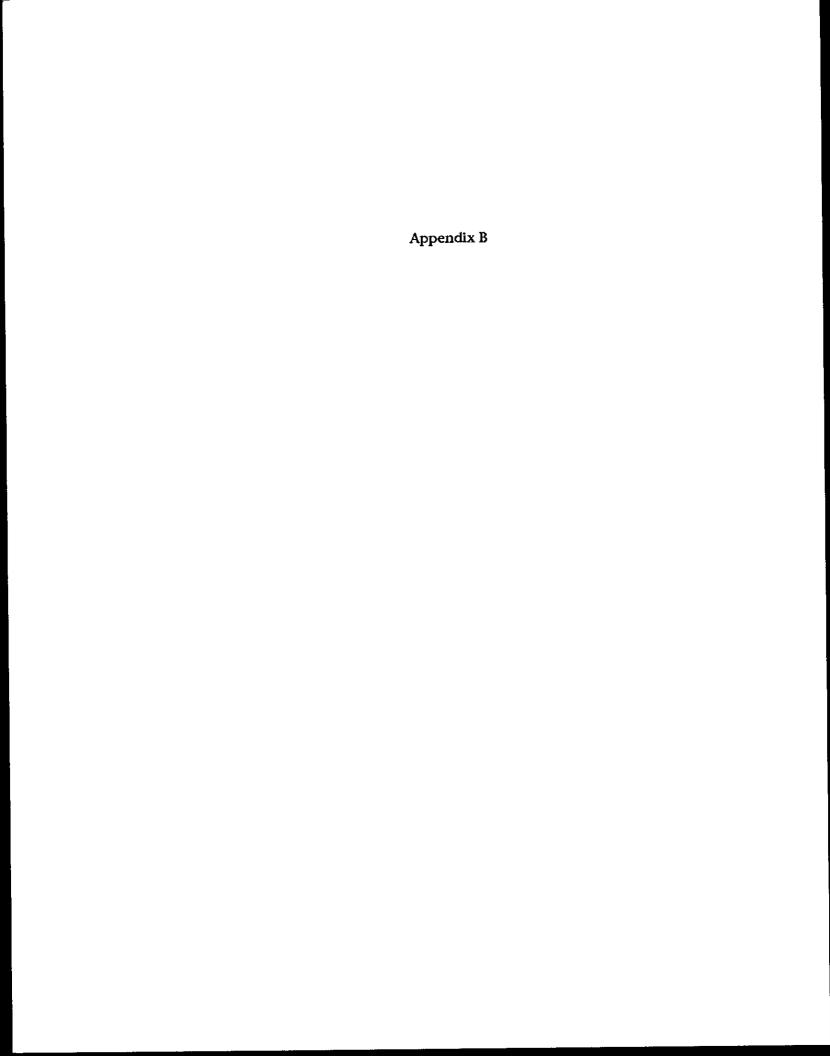
	+ + + + + + + •	.039	0.00	.209	.010	.082	.083	0.00	.703	.573	.090 .080	.792	.932	.301
	· C +	.281 .430	.460 477	.025 .074	0.00	0.00	0.00	0.00	0.00	.112	0.00	.062	00.00	.109
	A+8	.570	.540	.828	.956 .943	.918 .873	.917	.937 .960	.200	315	906.	.262	.040	.616 .570
	B+C	044. 694.	.621 .769	.105 .174	.053	.080 .084	.083	.094 0.00	.109	. 125	040	.062	0.00	.186 .198
	A+8 +C	.820	.725 .886	.848 .769	.956	.918	.917 .720	.937	.297	.342 .349	906.	.325	.068 .040	.652
	MISS ING	.039	0.00	.080	0.00	00.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	.003
	NOT KNOW	0.00	0.00	0.00	0.00	0.00	0.00	0.00	.047	.008	.062	0.00	0.00	000.
	NOT IN C URR I	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	.012	0.00	.025	.005	.005
	TAUG HT L ATER E	0.00	0.00	141.	.010	780.	.083	0.00	.656 .160	.552	031	.650	.927 .360	.264 .139
	ASSU MED D	.141	.097 .097	.023	0.00	0.00	0.00	0,00	0.00	.085	0.00	0.00	0.00	.059
	REVI EWED C	.290	.185	.020	0.00	0.00	0.00	0.00	0.00	.027	0.00	.062	0.00	.050
	EXTE NDED B	.328	.435	.085	.053	.080 .084	.083	.094 0.00	.109	.098	.040	0.00	0.00	.136
	NEW A	.352	.105	.743 .594	.844 .890	.838	.833	.960	.080	.200	.840	. 192	.005	479. 454.
•		88 89	88° 89	*88 *89	188 189	98,0¢	\$ 188 189	PO 88 189	15,88 189	88° 89	88 89 89	188 189	RY'88 '89	188 189
	T0P1C	1. INTEGERS	2. FRACTIONS	EXPONENTS	4. POLYNOMIALS	5. ALGEBRAIC EQU	6. INEQUALITIES	7. RATIONAL EXPO	8. PROB. & STATS	9. GEOMETRY	10. ABSOLUTE	11. FUNCTIONS	12. TRIGONOMETRY	
	-	-	2. F	ъ. П	4.	5. A	6. 1	7. #	ε. Γ	9.6	10.	Ξ.	12.	
		Ξ												2
	COURSE	ALGEBRA 1,2 (OR ALGEBRA												COURSE MEAN

MDTP88/89 - TEACHER QUESTIONNAIRE - TOPIC COVERAGE TOPIC BY TOPIC (12 CATEGORIES), PERCENTAGE

H H T	Σ.	0.00	.006	.221	.095	.212	.227 .746	. 182	.909	.145	.318 .405	.786	.857	.303
	Q+O	.595	.724 .612	.519 .374	.602	.537	.621	.636	0.00	.042	.409	.114	0.00	.380
	A+B	.193 .405	.269	.351 .405	.091	.231	.032	. 182 . 095	.091 .048	.812	.273 .190	.086	. 197 . 143	.321
	B+C	.409 .452	.503	.552	.561 .504	.545 .545	.333	.409 .476	.091	. 154	.357	.029	0.00	.378
44	4 + + +	.432 .619	.545 .755	.701	.598	.597	.333	.571	.091 .048	.790	. 548 . 548	.155	.197	.524 .553
MISS	Σ	0.00	0.00	0.00	0.00	.025	.045 .190	.045	0.00	00.00	.045	.045	0.00	.002
NOT	ပ	0.00	0.00	.045	00.00	.058	0.00	0.00	136	015	00.00	.005	0.00	.032
NOT 1N C	UKK T	0.00	0.00	.029 .054	0.00	.033	.091	00.00	.136	.006	.091	.050	.238	.027
TAUG HT L	ATER	0.00	.006	.055	.068	.050	.091	.045	591 429	.079	.091	.686	.381	.167 .134
ASSU MED	۵	.568	.231	.169	.337	. 190	. 048	.409 .190	0.00	.009 010	.227	.059	.045	.227 .143
REV! EWED	Ç	.239 .214	.381	.259	.360	.256	. 182	.227 476	0.0	033	.357	.055	0.00	203
EXTE NDED	80	.238	.327	.245	.028	. 194 . 199	.152 0.00	.182	.091	.091	.091	00.0	0.00	. 147 . 141
NEW	∢	.023	.042	. 149	.038	.037	0.00	0.00	0.00	.638	. 190	.091	. 197	174
		88° 89	* 88 69	88 60	88° 89	2U'88 189	\$ 188 189	88,04 89	15'88 '89	88° 98	188 189	188 189	RY'88 '89	88 89
ပ		1. INTEGERS	FRACTIONS	EXPONENTS	4. POLYNOMIALS	ALGEBRAIC EQU	6. INEQUALITIES	RATIONAL EXPO	PROB. & STATS	9. GEOMETRY	10. ABSOLUTE	11. FUNCTIONS	12. TRIGONOMETRY	
TOP 1C		IN I	FRA(POL	, ALG	N.			. GEO	0. AB	1. FU	2. TR	
		- :	2.	m,	±	5.	9	7.	&	6			-	
COURSE		GEOMETRY			•									COURSE MEAN

MDTP 88 - TEACHER QUESTIONNAIRE - TOPIC COVERAGE TOPIC BY TOPIC (12 CATEGORIES), PERCENTAGE

ы 4 Т	Σ +	.510 .467
	C+D	.116
	A+B	.375
	B+C	.201
94	υ +	.445 .485
MISS	Σ	.073
NOT KNOW	O	.014
NOT NOT	ς Σ	.112
TAUG HT L	A 17 17 17 17	.311
ASSU MED	٥	.045
REVI EWED	ပ	.070
EXTE NDEO	80	.115
NEW	∢	.259
TOP IC		188 189
10		
COURSE		TOTAL



1988 TEACHER CONTENT COVERAGE BY COURSES - BY SUBTOPIC (80% Teachers' agreement on each topic)

ITEMS	LOWER THAN PRE ALGEBRA	МАТН А	матн в	PRE ALGEBRA	ALGEBRA 1	GBOMETRY
'BASIC OPERATIONS WITH SIGNED NO.'	*	*	*	C(38)	*	P(19)
THE RESIDENCE OF THE PROPERTY	*	C(12)	C(5)	C(38)	C(27)	P(19)
2 'PRIME FACTORIZATION' 3 'FINDING DISTANCES ON NUMBER LINE'	*	*	*	C(35)	*	*
. TOTAL STRUCTURE OF DIVISION FTV!	•	C(15)	*	*	*	*
THE PARTY OF THE ACTIONS!	C(36)	•	C(5)	*	*	P(19)
A DALL OF THE A CITY ON EL	C(36)	*	C(5)	*	*	P(19)
TO THE PARTY OF THE ACTIONS!	C(36)	*	C(5)	*	•	P(19)
TO A COLONIC!	*	*	C(5)	*	*	*
	C(37)	*	C(5)	*	*	P(19)
9 'ADD. & SUB OF DECIMALS'	C(37)	*	C(5)	*	*	P(19)
10 'MUL, & DIV. OF DECIMALS'	C(38)	*	C(5)	*	*	*
11 'ESTIMATION & APPROXIMATION'	C(38)	•	C(5)	*	*	P(18)
12 'CONV. BET. FRACTIONS & DECIMALS'	C(38)	*	C(5)	*	*	P(18)
13 'CONV. BET. FRACTIONS & PERCENT'	C(38)	*	C(5)	*	*	P(18)
14 'COMPUT. WITH DECI & FRAC, ROUND'		*	C(5)	C(32)	*	*
15 'COMPUTATION OF PERCENT'	C(38)	*	C(5)	C(33)	*	*
16 'CONCEPT OF PROPORTION'	C(35)	•	C(5)	C(33)	C(28)	*
17 'COMPUTATION OF PROPORTIONS'	C(35)	*	C(5)	C(33)	C(28)	*
18 'APPLIC. OF RATIO OR PROPORTIONS'	C(35)	C(13)	C(5)	*	C(31)	*
19 'APPLIC. LAWS OF EXPONENTS'	*	*	C(5)	C(33)	C(29)	*
20 POWERS OF 10 & SCIENTIFIC NOTAT.		4	C(5)	*	C(29)	*
21 'EXPONENT, WITH INTEGRAL EXPONEN.'	•	*	C(5)	*	C(27)	•
22 'SQ. ROOT OF PERFECT SQUARES'	•	*		*	C(26)	*
23 'SIMPLIFICATION OF SQ. ROOTS'	•	*	C(5)	*	C(26)	*
24 'ADD. & SUB. OF SQ. ROOTS'	•	•	C(5)	*	C(26)	*
25 'MUL. & DIV. OF SQ. ROOTS'	* ************************************		C(5)	*	*	*
26 'CONV. BET. RADICALS & RAT. EXPO.'	N(34)	N(9)	*	*	*	*
27 'RATIONALIZ. OF NUMERA. & DENOMI.'	N(34)	N(9)		•	*	*
28 'ADD. AND SUB. OF RADICAL EXPRE. '	N(34)	N(9)	*	*		*
29 NUM, CALCU. W/ EXPONENTS & RAD. '	N(34)	-	*	*	*	*
30 'ALGE. CALCU. W/ EXPONENTS & RAD.'	N(34)	-				*
31 'FACTORING & SIMPLI. ALGE. EXPRE.'	N(34)	*	N(5)	N(34)	· (2/27)	
32 'ESTIM. & APPROXI. WITH RADICALS.'	N(34)	N(9)	*		C(27)	
33 'ALGE OPERATION OF LITERAL SYMBOL'	*			•	C(32)	Ţ
34 'SIMPLIF. OF POLYNO. BY GROUPING.'	N(34)	*	*	*	C(32)	.
35 'ADD. & SUB. OF POLYNOMIALS'	N(34)	*			C(32)	*
36 'EVALUATION OF A POLYNOMIAL(1/2) '	N(34)	*		*	C(32)	-
37 'MUL. OF MONOMIAL WITH A POLYNO. '	N(34)	*	*	*	C(32)	*
38 'MUL. OF TWO BINOMIALS'	N(34)	*	*	N(33)	C(32)	*
39 'DIVISION OF POLYNOMIALS'	N(34)	*	*	N(36)	C(31)	*
40 'SQUARING A BINOMIAL'	N(34)	*	*	N(36)	C(31)	*
41 'FACTOR. POLYNOMIALS'	N(34)	*		N(30)	C(32)	*
42 FACTOR, TRINOMIAL OVER INTEGERS '	N(34)	*	*	N(34)	C(31)	
43 FACTOR, PERFECT SQ. TRINOMIALS '	N(34)	*	*	N(34)	C(31)	*
44 'SIMPLIF. OF COMPLEX NUMBERS'	N(34)	N(9)	N(5)	N(35)	*	*
45 'ONE UNKNOWN WITH NUM. COEFFI.'	•	*	*	*	C(32)	*
46 'ONE UNKNOWN WITH LIT. COEFFI.'	*	*	*	*	C(32)	•

C: Core

Given in parenthesis is the number of sections when computing more then 80% Teachers' agreement.

P: Prior

N: Not Taught
*: Not specified

1988 TEACHER CONTENT COVERAGE BY COURSES - BY SUBTOPIC (80% Teachers' agreement on each topic)

47 'SIMPLE LIN. EQUA. IN ONE UNKNOWN' 48 TWO UNKNOWN BY ELIMINATION' 49 TWO UNKNOWN BY SUBSTITUTION' 50 'APPLICATION OF EQUATIONS' 51 'GENERATING EQUATIONS FROM DESCR.' 51 'GENERATING EQUATIONS FROM DESCR.' 52 'SOLV. EQUA. FROM FACTORED FORM' 53 'SOLVING QUAD.EQUAT.BY FACTORING' 54 'SOLV. QUAD. EQUA. BY QUADRATIC' 55 'GRAPHS OF QUADRATIC RELATIONS' 56 'ONE UNKNOWN WITH NUM. COEFFI.' 57 'SOLUT. OF QUADRATIC INEQUALITIES' 58 'GRAPHING LIN. INEQ. IN ONE UNKNO' 59 'SIMPLIF. OF A RATIONAL EXPRE.' 60 'EVALUATION OF A RATIONAL EXPRE.' * * * * * * * * * * * * *	
48 TWO UNKNOWN BY ELIMINATION' 49 TWO UNKNOWN BY SUBSTITUTION' 50 'APPLICATION OF EQUATIONS' 51 'GENERATING EQUATIONS FROM DESCR.' 52 'SOLV. EQUA. FROM FACTORED FORM' 53 'SOLVING QUAD.EQUAT.BY FACTORING' 54 'SOLV. QUAD. EQUA. BY QUADRATIC' 55 'GRAPHS OF QUADRATIC RELATIONS' 56 'ONE UNKNOWN WITH NUM. COEFFI.' 57 'SOLUT. OF QUADRATIC INEQUALITIES' 58 'GRAPHING LIN. INEQ. IN ONE UNKNO' 59 'SIMPLIF. OF A RATIONAL EXPRE.' N(34) N(9) * ** ** ** ** ** ** ** ** **	
49 TWO UNKNOWN BY SUBSTITUTION' 50 'APPLICATION OF EQUATIONS' 51 'GENERATING EQUATIONS FROM DESCR.' 52 'SOLV. EQUA. FROM FACTORED FORM' 53 'SOLVING QUAD.EQUAT.BY FACTORING' 54 'SOLV. QUAD. EQUA. BY QUADRATIC' 55 'GRAPHS OF QUADRATIC RELATIONS' 56 'ONE UNKNOWN WITH NUM. COEFFI.' 57 'SOLUT. OF QUADRATIC INEQUALITIES' 58 'GRAPHING LIN. INEQ. IN ONE UNKNO' 59 'SIMPLIF. OF A RATIONAL EXPRE.' N(34) N(9) * ** ** ** ** ** ** ** ** **	
50 'APPLICATION OF EQUATIONS' 51 'GENERATING EQUATIONS FROM DESCR.' 52 'SOLV. EQUA. FROM FACTORED FORM' 53 'SOLVING QUAD.EQUAT.BY FACTORING' 54 'SOLV. QUAD. EQUA. BY QUADRATIC' 55 'GRAPHS OF QUADRATIC RELATIONS' 56 'ONE UNKNOWN WITH NUM. COEFFI.' 57 'SOLUT. OF QUADRATIC INEQUALITIES' 58 'GRAPHING LIN. INEQ. IN ONE UNKNO' 59 'SIMPLIF. OF A RATIONAL EXPRE.' N(31) * * * * * * * * * * * * *	
51 'GENERATING EQUATIONS FROM DESCR.' N(31) * N(5) * C(30) * 52 'SOLV. EQUA. FROM FACTORED FORM' N(34) N(9) * N(39) C(28) * 53 'SOLVING QUAD. EQUAT.BY FACTORING' N(34) N(9) * N(39) C(28) * 54 'SOLV. QUAD. EQUA. BY QUADRATIC' N(34) N(9) N(5) N(39) C(28) * 55 'GRAPHS OF QUADRATIC RELATIONS' N(34) N(9) N(5) N(39) * * 56 'ONE UNKNOWN WITH NUM. COEFFI.' N(34) * * C(32) * 57 'SOLUT. OF QUADRATIC INEQUALITIES' N(34) N(9) * N(34) * * C(32) * 59 'SIMPLIF. OF A RATIONAL EXPRE.' * * * C(30) *	
52 'SOLV. EQUA. FROM FACTORED FORM' 53 'SOLVING QUAD.EQUAT.BY FACTORING' 54 'SOLV. QUAD. EQUA. BY QUADRATIC' 55 'GRAPHS OF QUADRATIC RELATIONS' 56 'ONE UNKNOWN WITH NUM. COEFFI.' 57 'SOLUT. OF QUADRATIC INEQUALITIES' 58 'GRAPHING LIN. INEQ. IN ONE UNKNO' 59 'SIMPLIF. OF A RATIONAL EXPRE.' N(34) N(9) N(34) N(9) N(134) N(
53 'SOLVING QUAD.EQUAT.BY FACTORING' N(34) N(9) * N(39) C(28) * SOLV. QUAD. EQUA. BY QUADRATIC' N(34) N(9) N(5) N(39) C(28) * SOLV. QUADRATIC RELATIONS' N(34) N(9) N(5) N(39) * SOLV. QUADRATIC RELATIONS' N(34) N(9) N(5) N(39) * SOLV. QUADRATIC RELATIONS' N(34) N(9) N(5) N(39) * SOLV. QUADRATIC INEQUALITIES' N(34) N(9) N(34) * C(32) * SOLV. QUADRATIC INEQUALITIES' N(34) N(9) * N(34) * SOLV. QUADRATIC INEQUALITIES' N(34) N(9) N(9) N(5) N(39) C(28) * SOLV. QUADRATIC INEQUALITIES' N(34) N(9) N(5) N(39) C(28) * SOLV. QUADRATIC INEQUALITIES' N(34) N(9) N(5) N(39) C(28) * SOLV. QUADRATIC INEQUALITIES' N(34) N(9) N(9) N(5) N(39) * SOLV. QUADRATIC INEQUALITIES' N(34) N(9) N(9) N(9) N(9) N(9) N(9) N(9) N(9	
54 'SOLV. QUAD. EQUA. BY QUADRATIC ' N(34) N(9) N(5) N(39) C(28) * 55 'GRAPHS OF QUADRATIC RELATIONS' N(34) N(9) N(5) N(39) * 56 'ONE UNKNOWN WITH NUM. COEFFI.' N(34) * C(32) * 57 'SOLUT. OF QUADRATIC INEQUALITIES' N(34) N(9) N(34) * 58 'GRAPHING LIN. INEQ. IN ONE UNKNO' N(34) * 59 'SIMPLIF. OF A RATIONAL EXPRE.' * * C(30) *	
55 'GRAPHS OF QUADRATIC RELATIONS' 56 'ONE UNKNOWN WITH NUM. COEFFI.' 57 'SOLUT. OF QUADRATIC INEQUALITIES' 58 'GRAPHING LIN. INEQ. IN ONE UNKNO' 59 'SIMPLIF. OF A RATIONAL EXPRE.' N(34) N(9) N(5) N(39) * * C(32) * C(32) * C(32) * C(30) *	
56 'ONE UNKNOWN WITH NUM. COEFFI.' N(34) * * * C(32) * 57 'SOLUT. OF QUADRATIC INEQUALITIES' N(34) N(9) * N(34) * * 58 'GRAPHING LIN. INEQ. IN ONE UNKNO' N(34) * * C(32) * 59 'SIMPLIF. OF A RATIONAL EXPRE.' * * * C(30) *	
57 'SOLUT. OF QUADRATIC INEQUALITIES' N(34) N(9) * N(34) * * 58 'GRAPHING LIN. INEQ. IN ONE UNKNO' N(34) * * C(32) * 59 'SIMPLIF. OF A RATIONAL EXPRE.' * * * C(30) *	
58 'GRAPHING LIN. INEQ. IN ONE UNKNO' N(34) * * * C(32) * 59 'SIMPLIF. OF A RATIONAL EXPRE.' * * * C(30) *	
59 'SIMPLIF. OF A RATIONAL EXPRE.' * * * C(30) *	
61 'ADD. & SUB. OF RATIONAL EXPRE.' N(32) * * * C(30) *	
62 'MUL. & DIV. OF RATIONAL EXPRE.' N(32) * N(5) * C(30) *	
	(19)
	(19)
65 'GRAPH READING' * * * * C(26) *	
66 'LOCATI. OF POINTS IN CORD. PLANE' * * N(5) * C(26) *	
67 'DISTANCE BET. TWO POINTS IN COR.' * N(9) N(5) * *	
	(21)
69 'CIRCUMFERENCE & AREA OF CIRCLE' * * * * * C((21)
70 'VOL. OF CUBES, CYLINDERS, RECTAN.' * * N(5) * * C((21)
	(21)
	(21)
	(21)
	(21)
75 'PYTHAGOREAN THEOREM & SPECI. TR.' * N(9) N(5) * * C((21)
	(21)
77 'PROOFS(FORMAL DEDUCTIVE DEMONST.' N(31) N(9) N(5) N(39) N(28) C((21)
78 TRANSFORMATIONS(TRANSLATION.' N(31) N(9) N(5) N(39) N(30) *	
79 'VECTORS' N(31) N(9) N(5) N(39) N(30) *	
80 'SIMPLIF. & EVALU. OF EXPRESS.' N(31) * N(5) * C(29) *	
81 'SOLUTION OF EQUATIONS' $N(31)$ $N(9)$ $N(5)$ * $C(29)$ *	
82 FUNCT. CONCEPT & USE OF NOTATION' N(34) * N(5) N(36) * *	
83 FUNCT. EVALUATION USING SUBSTIT.' N(34) * N(5) N(36) * *	
84 'COMPOSITION OF FUNCTION' $N(34)$ $N(9)$ $N(5)$ $N(37)$ *	
85 'GRAPHING OF FUNCTION' $N(34)$ $N(9)$ $N(5)$ $N(37)$ *	
· · · · · · · · · · · · · · · · · · ·	(18)
	(18)
The state of the s	(18)
	(18)
70 DODOCIO: OI DODITO	(18)
,, output at 10 at	(18)
92 'FIND. ALGEBRAIC EXPRESS' N(34) N(9) N(5) * N(30) *	
	(17)
94 FIND. SIDE LENGTHS IN SPEC.TRIA.' N(34) N(9) N(5) N(37) N(29) *	
•• ••••••••••••••••••••••••••••••••••••	(18)
· · · · · · · · · · · · · · · · · · ·	(18)
97 'PROOF OF TRIGONOMETRIC IDENTITIE' N(34) N(9) N(5) N(39) N(30) N	(18)

1989 TEACHER CONTENT COVERAGE BY COURSES - BY SUBTOPIC (80% Teachers' agreement on each topic)

*******	ITEMS	LOWER THAN PRE ALGEBRA	МАТН А	матн в	PRE ALGEBRA	ALGEBRA 1	GEOMETRY
<u> </u>	BASIC OPERATIONS WITH SIGNED NO.	C(22)	*	*	*	*	P(19)
2	PRIME FACTORIZATION'	C(22)	C(6)	*	C(12)	*	*
3	'FINDING DISTANCES ON NUMBER LINE'	*	C(6)	*	C(11)	*	C(19)
4	USING DEFINITION OF DIVISIBILITY	C(21)	C(6)	C(3)	•	*	*
5	'ADD. & SUB. OF FRACTIONS'	*	P(6)	P(3)	*	*	*
6	'MUL. & DIV. OF FRACTIONS'	*	P(6)	P(3)	*	*	*
7	'ORDER & COMPARISON OF FRACTIONS'	*	P(6)	P(3)	*	*	P(20)
8	'SIMPLIF. OF COMPLEX FRACTIONS'	*	P(6)	P(3)	*	*	*
9	'ADD. & SUB OF DECIMALS'	*	P(6)	P(3)	*	*	*
	'MUL. & DIV. OF DECIMALS'	*	P(6)	P(3)	*	*	*
	'ESTIMATION & APPROXIMATION'	C(24)	P(6)	P(3)	*	*	*
	'CONV. BET. FRACTIONS & DECIMALS'	#	P(6)	P(3)	*	*	*
	'CONV. BET. FRACTIONS & PERCENT'	*	P(6)	P(3)	*	*	*
	'COMPUT. WITH DECI & FRAC, ROUND.'	C(24)	P(6)	P(3)	*	*	*
	'COMPUTATION OF PERCENT'	C(21)	P(6)	P(3)	C(12)	*	*
	'CONCEPT OF PROPORTION'	C(21)	*	•	C(13)	*	*
	'COMPUTATION OF PROPORTIONS'	C(21)	*	*	C(12)	*	*
	'APPLIC. OF RATIO OR PROPORTIONS '	C(21)	*	+	C(12)	*	*
	'APPLIC. LAWS OF EXPONENTS'	*	C(6)	C(3)	*	C(23)	*
		*	C(6)	C(3)	*	*	*
	'POWERS OF 10 & SCIENTIFIC NOTAT.'		C(6)	C(3)	*	C(21)	P(17)
	'EXPONENT, WITH INTEGRAL EXPONEN.'		*	*	C(10)	*	*
	'SQ. ROOT OF PERFECT SQUARES'	·	*	*	*	*	*
	'SIMPLIFICATION OF SQ. ROOTS'	•	*		*	C(22)	*
	'ADD. & SUB. OF SQ. ROOTS'	•	N(6)	*	*	C(22)	*
	'MUL, & DIV, OF SQ. ROOTS'	N(25)	N(6)	N(3)	*	*	*
	'CONV. BET. RADICALS & RAT. EXPO.'	N(25) N(25)	*	*	*	C(18)	*
	RATIONALIZ. OF NUMERA. & DENOMI.	N(25)	N(6)	N(3)	N(11)	*	*
	'ADD. AND SUB. OF RADICAL EXPRE. '		*	*	*	C(18)	*
	NUM. CALCU. W/ EXPONENTS & RAD.	N(25)	N(6)	N(3)	•	*	*
	'ALGE. CALCU. W/ EXPONENTS & RAD.'	N(25)	*	*	*	*	*
	"FACTORING & SIMPLI. ALGE. EXPRE."	N(25)	*		*	*	*
	ESTIM. & APPROXI. WITH RADICALS.	N(25)			C(9)	C(22)	*
	'ALGE OPERATION OF LITERAL SYMBOL'	N(25)		•	*	C(24)	P(19)
	'SIMPLIF. OF POLYNO. BY GROUPING.'	N(25)	*	*		C(24)	P(19)
	'ADD. & SUB. OF POLYNOMIALS'	N(25)	*	*	•	C(24)	*
	EVALUATION OF A POLYNOMIAL(1/2)	N(25)	•	*	*	C(24)	P(19)
	'MUL. OF MONOMIAL WITH A POLYNO.'	N(25)	*		N(10)	C(24)	P(19)
	S'MUL. OF TWO BINOMIALS'	N(25)	•		N(10)	C(24)	*
	DIVISION OF POLYNOMIALS'	N(25)	•		N(10)	C(24)	P(19)
	'SQUARING A BINOMIAL'	N(25)	*		N(10)	C(24)	P(19)
	'FACTOR, POLYNOMIALS'	N(25)	N1/2)	*		C(24)	P(19)
	2 FACTOR. TRINOMIAL OVER INTEGERS '	N(25)	N(2)	±	N(10)		P(19)
	3 'FACTOR, PERFECT SQ. TRINOMIALS'	N(25)			N(10)	C(24)	* (12)
	'SIMPLIF. OF COMPLEX NUMBERS'	N(25)	N(6)		N(10) *	C(21)	*
	ONE UNKNOWN WITH NUM. COEFFI.	*	C(6)	-	•	C(24)	*
	ONE UNKNOWN WITH LIT. COEFFI.	N(22)	*	-	-	C(24)	*
	'SIMPLE LIN. EQUA. IN ONE UNKNOWN'	¥	C(6)	-	4	C(24)	*
	TWO UNKNOWN BY ELIMINATION'	N(25)	N(6)	*	-	C(23)	
	TWO UNKNOWN BY SUBSTITUTION'	N(25)	N(6)	*	∓	C(23)	P(19)
50	'APPLICATION OF EQUATIONS'	N(24)	*	C(3)	7	C(24)	₹

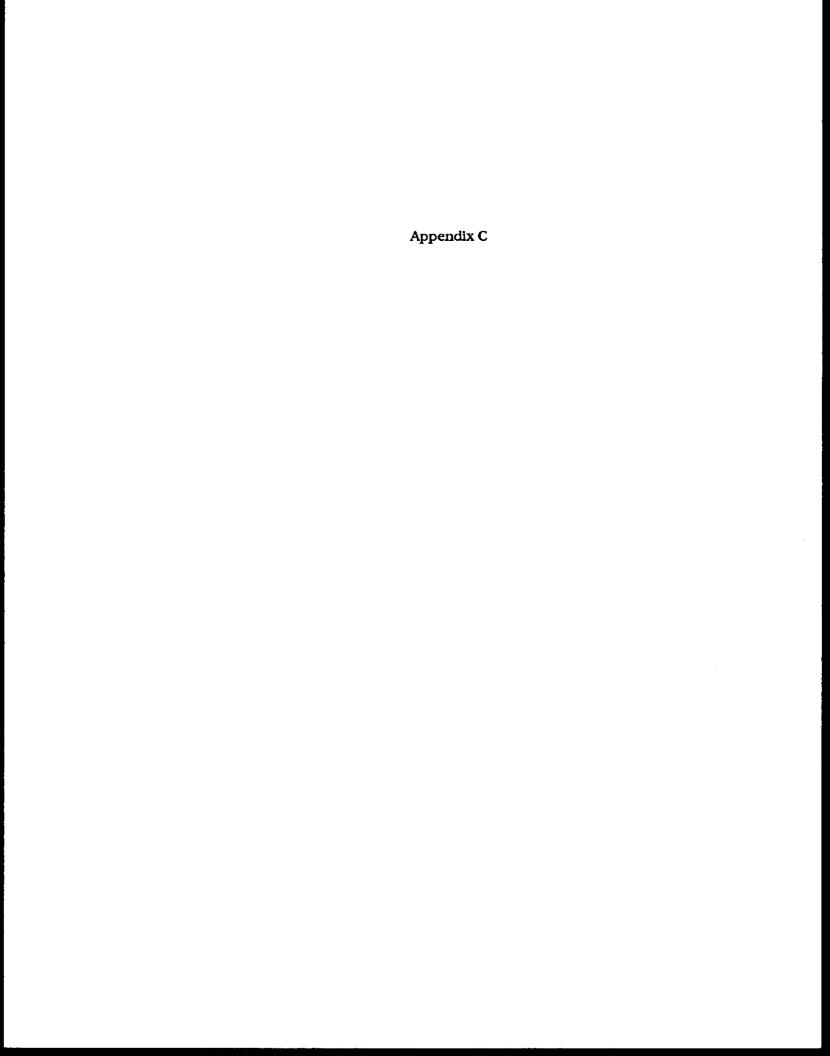


Table 3. Average P-values by teachers' reports of topic coverage on the MDTP Algebra Readiness, Elementary Algebra tests and the SIMS Benchmark test.

Teachers' Report of —		Averag	e P-values (Nur	nber of Test Items)*		
Topic Coverage		DTP READINESS		IDTP ARY ALGEBRA	SIMS BENCHMARK		
	'89	'88	'89	'88	'89	'88	
A. Taught as New	.34(50)	.35(50)	.40(48)	.33(46)	.42(39)	.33(46)	
B. Extended & Reviewed	.34(44)	.34(46)	.40(31)	.35(44)	.40(32)	.35(47)	
C. Reviewed only	.35(34)	.34(43)	.41(40)	.37(40)	.43(28)	.36(46)	
D. Assumed as Prereq.	.34(17)	.28(4)	.41(44)	.37(15)	.42(37)	.35(49)	
E. Taught Later	.34(25)	.35(35)	.38(23)	.35(30)	.42(29)	.35(31)	
F. Not in Curriculum	.29(19)	.34(17)	.35(4)	.00(00)	.41(27)	.32(12)	
G. Don't know	.00(0)	.28(8)	.36(13)	.00(00)	.00(0)	.33(16)	
H. No Response	.30(16)	.31(19)	.41(8)	.43(4)	.41(27)	.34(23)	

^{*} The average P-value for each response choice is determined by a multi-step process. First, individual test items are assigned to topic categories. Then, the performance of students on each item is assigned to topic coverage categories based on the responses of their teachers. Finally, the P-values for each item that appears in a given topic coverage category are averaged across items. For example, the average p-value for Review Only on the MDTP Algebra Readiness test is .344 across the 43 items where at least one teacher chose "Reviewed Only" to describe coverage of the topic.